

# Sound wave propagation in granular materials

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Multi-Scale-Mechanics / TS / CTW / UTwente

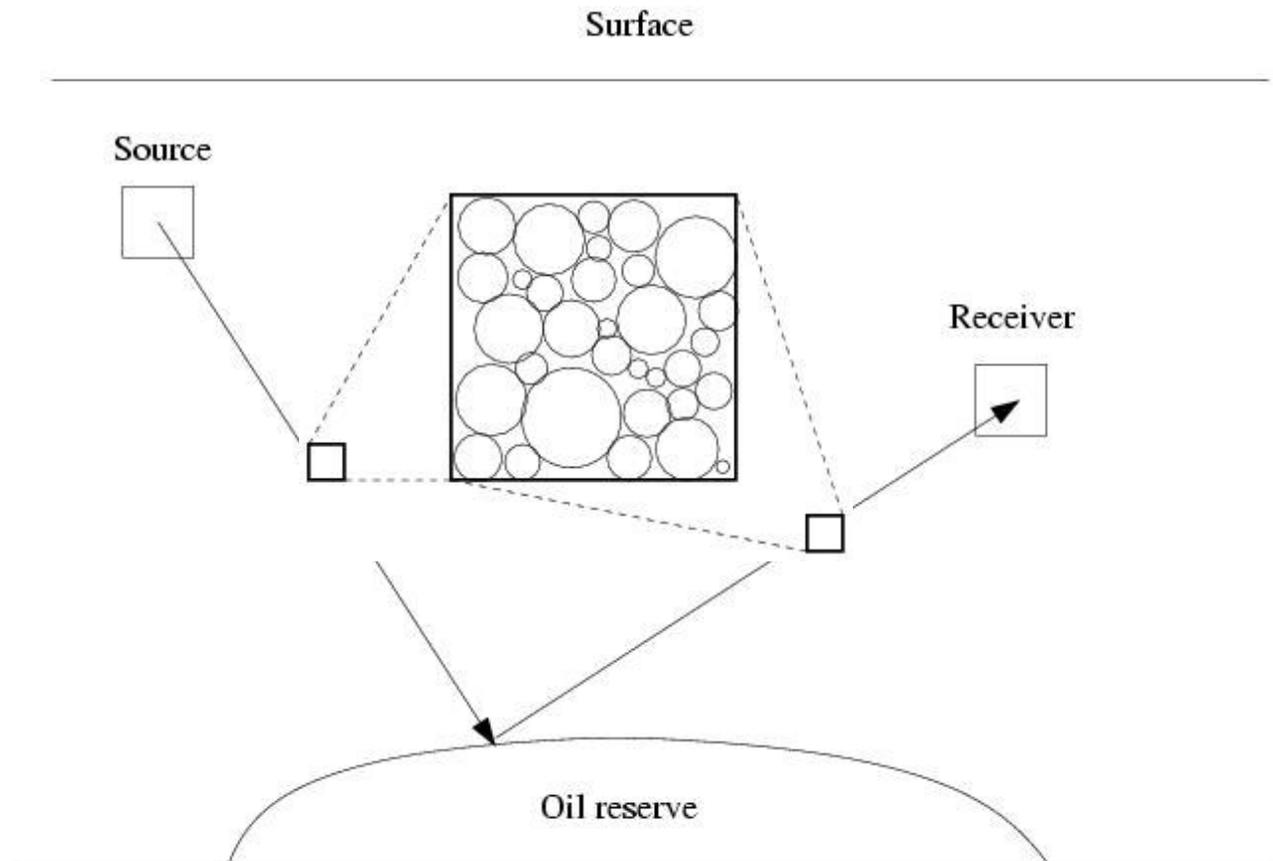


"JMBC Granular matter course"

February 2008

# Applications

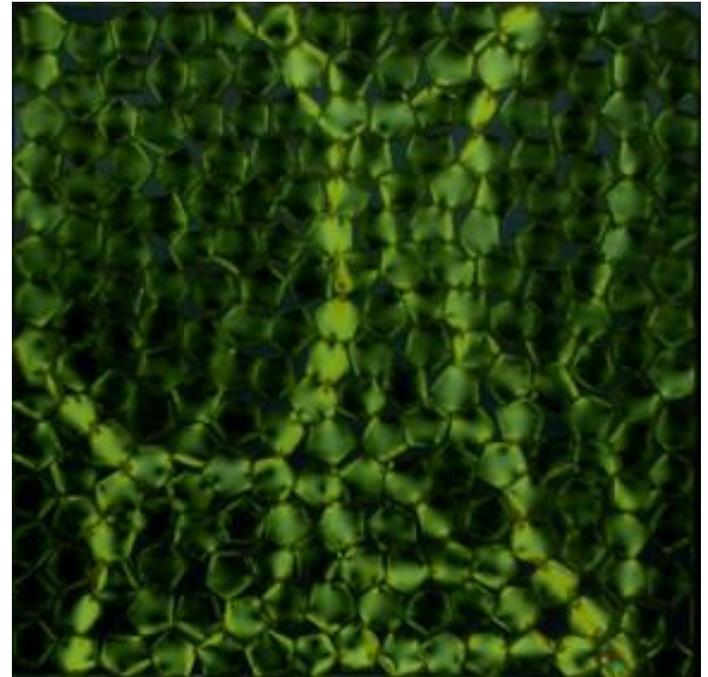
- Seismology
- Oil exploration
- ...



# Granular matter

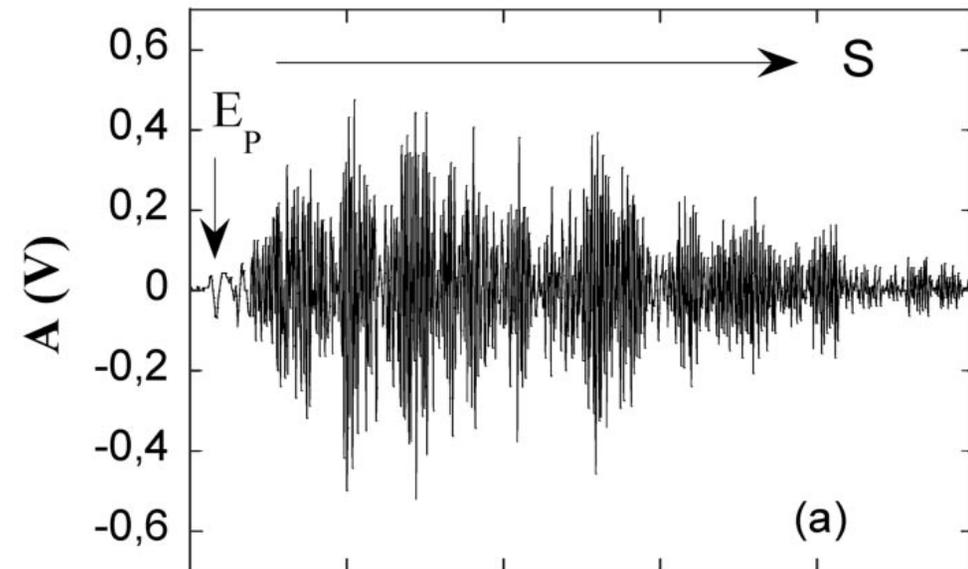
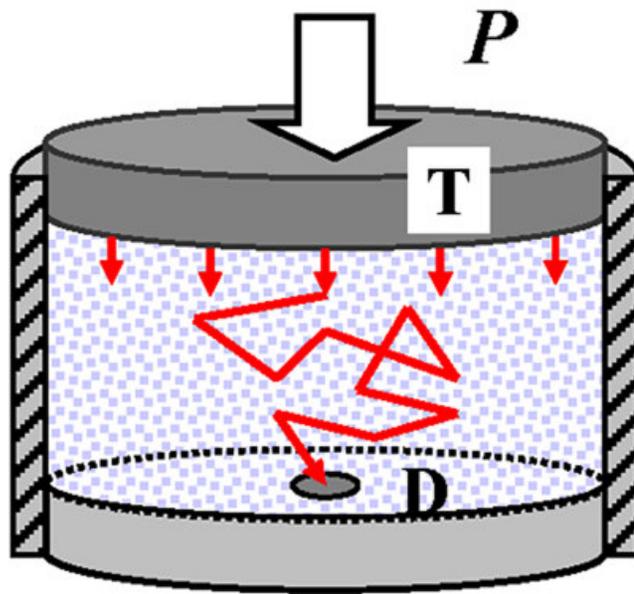
## Assembly of grains:

- Dense
- Friction (Rotations)
- Inhomogeneous
- Non-linear behaviour



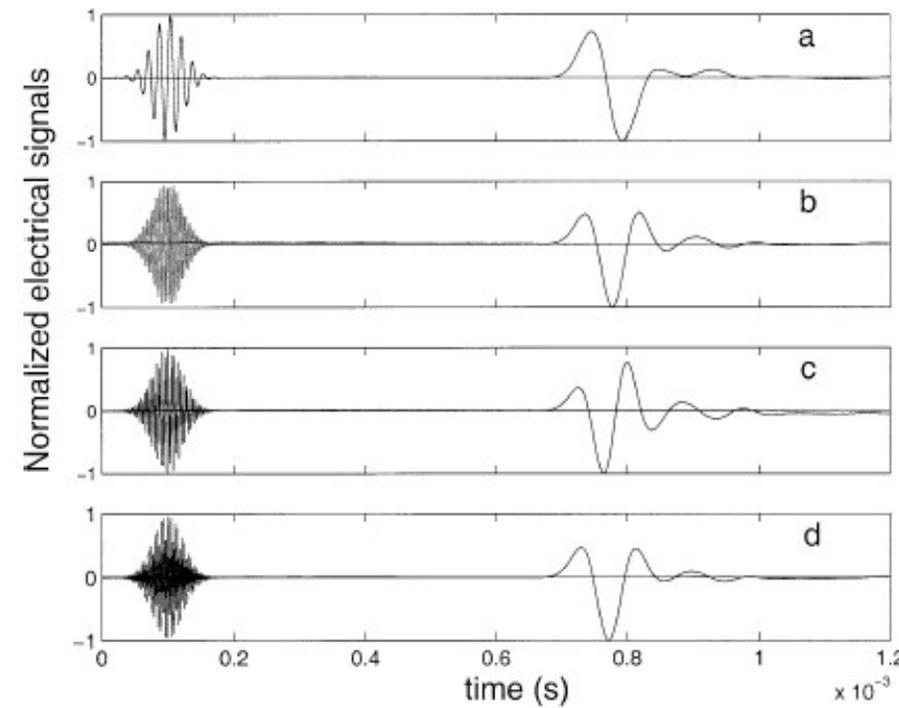
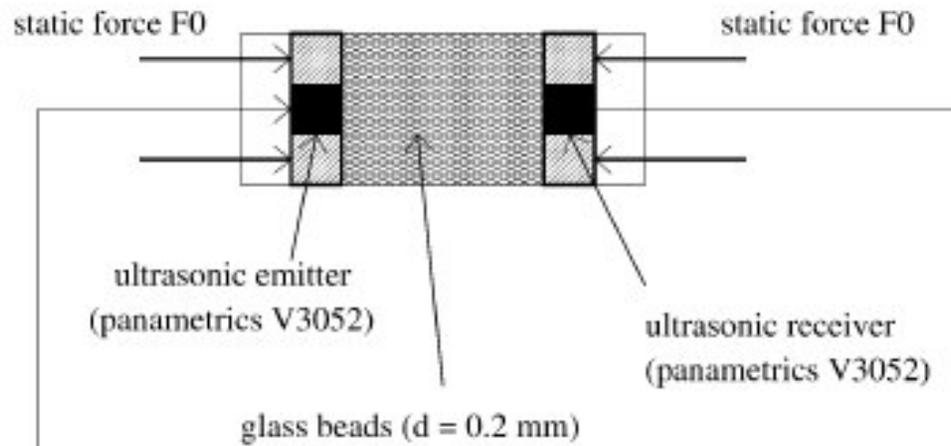
# Codalike Multiple Scattering of Elastic Waves in Dense Granular Media

X. Jia, PRL, 2004



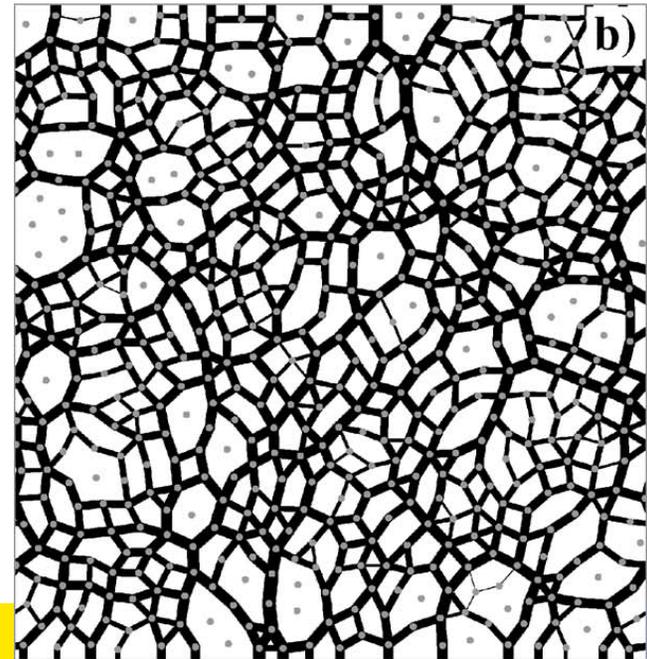
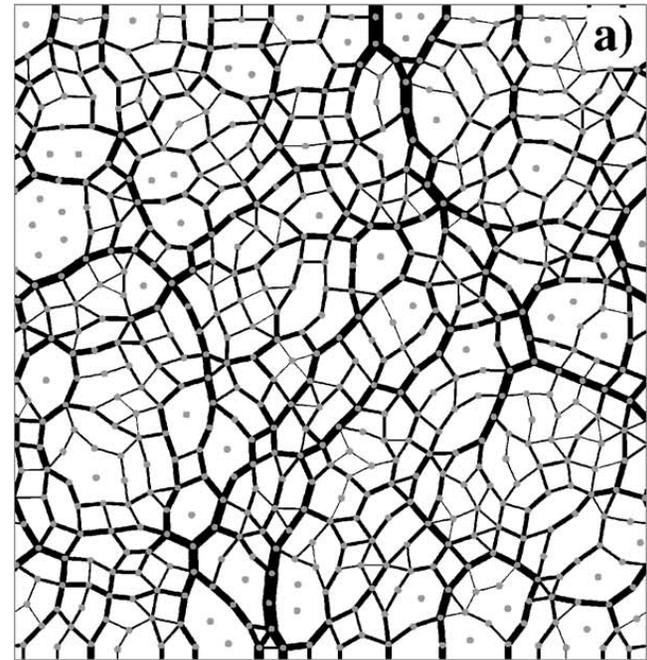
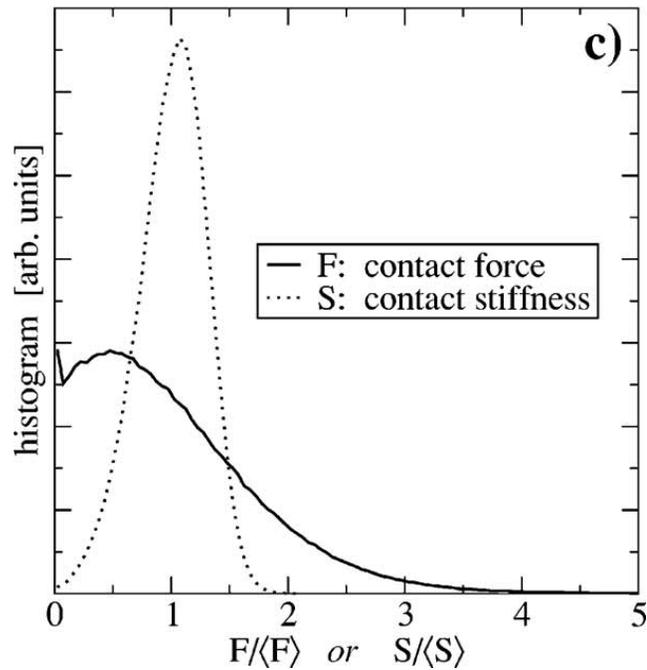
# Self-demodulation acoustic signatures for nonlinear propagation in glass beads

V. Tournat *et al*, C.R.Mecanique, 2002

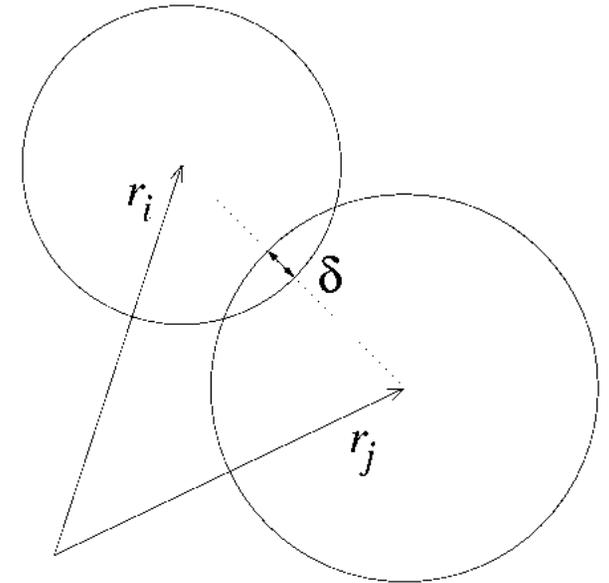


# Elastic wave propagation in confined granular systems

Somfai et al, Phys. Rev. E, 2005



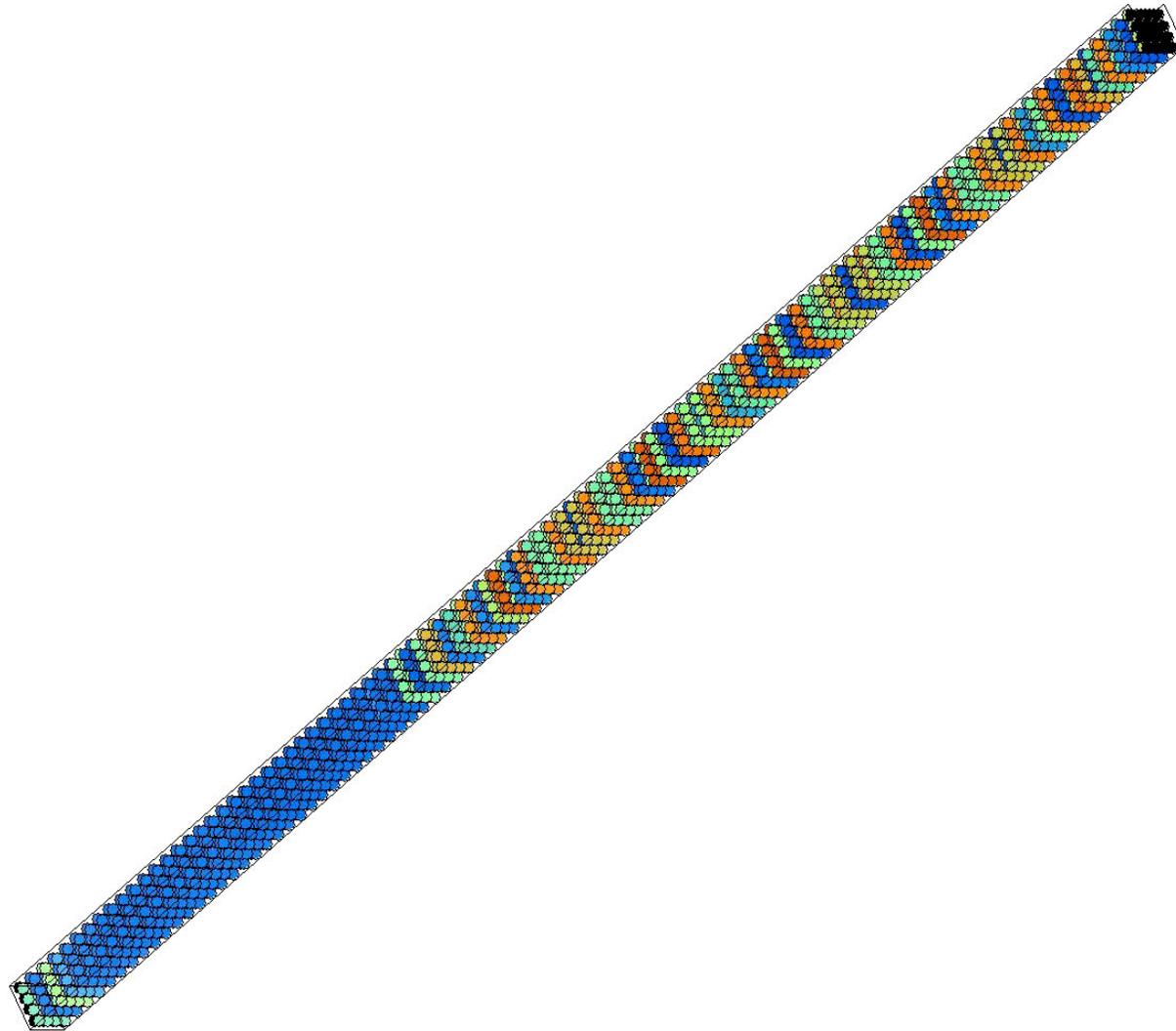
# Discrete Element Method



*The equation of motion is solved for all particles according to the contact forces and torques.*

- Normal part :  $f = k_N \cdot \delta$     **repulsive** and **attractive** forces  
(**dissipation**)
- Tangential part :    **Sliding** -( $k_T$ ), **Rolling**  
and **Torsion**- resistance

# P-wave animation



# Towards complexity

## Modes

- P-waves
- S-waves
- R-waves
- ...

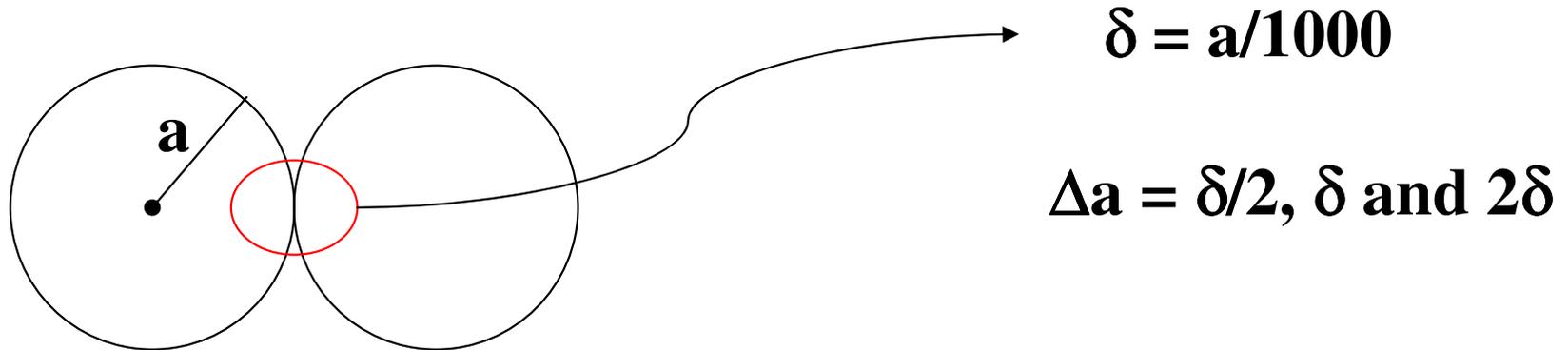
## Micro-Parameters

- Damping
- Friction (Rotations)
- Cohesion
- Contact law
- ...

## Structure

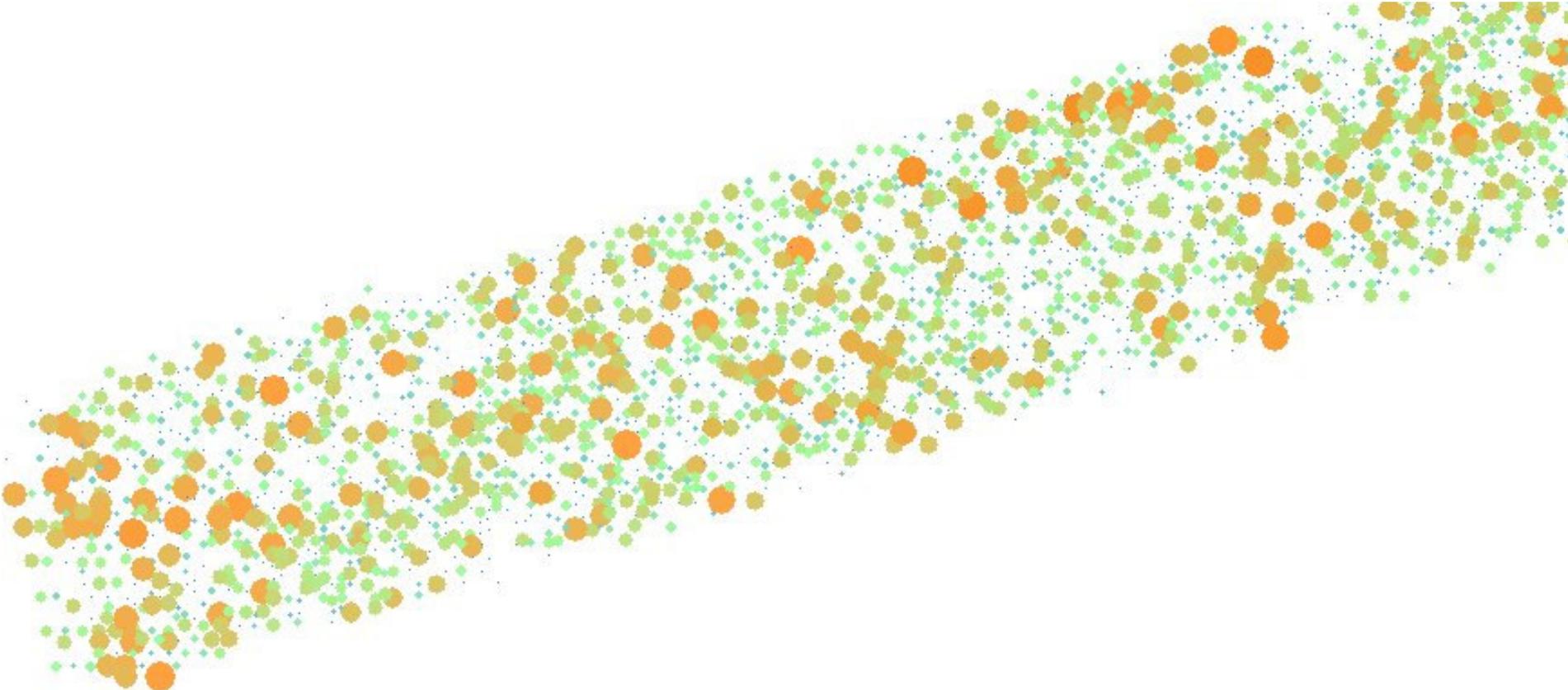
- Mono- poly-disperse
- (Dis-)ordered
- ...

# Weak polydispersity

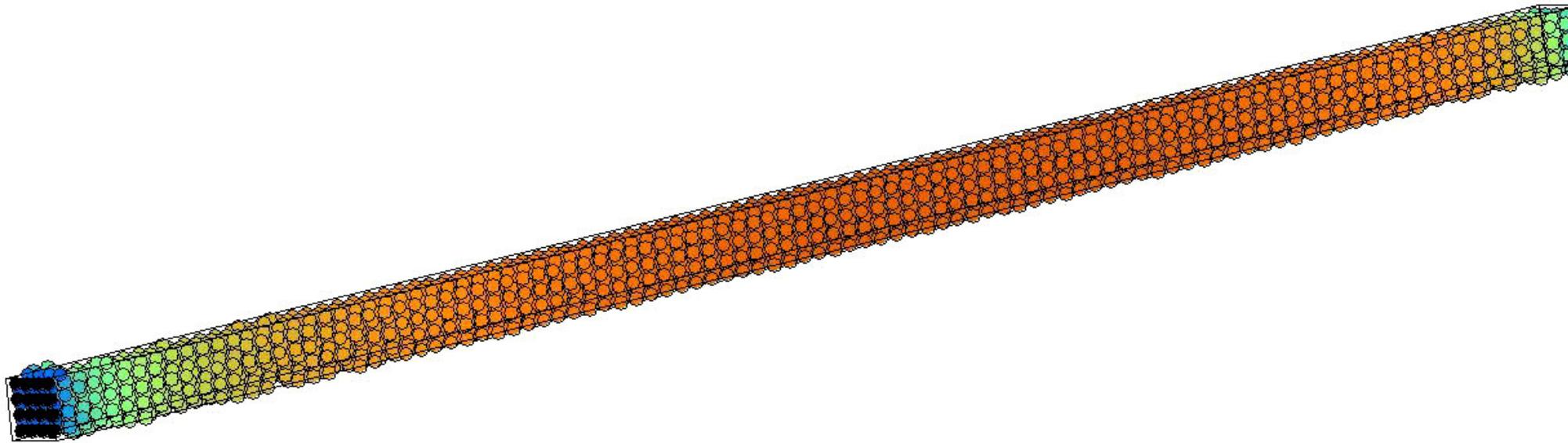


- The system is practically unchanged at the grain level
- Distribution of weak and strong contacts  
and most important opening of contacts

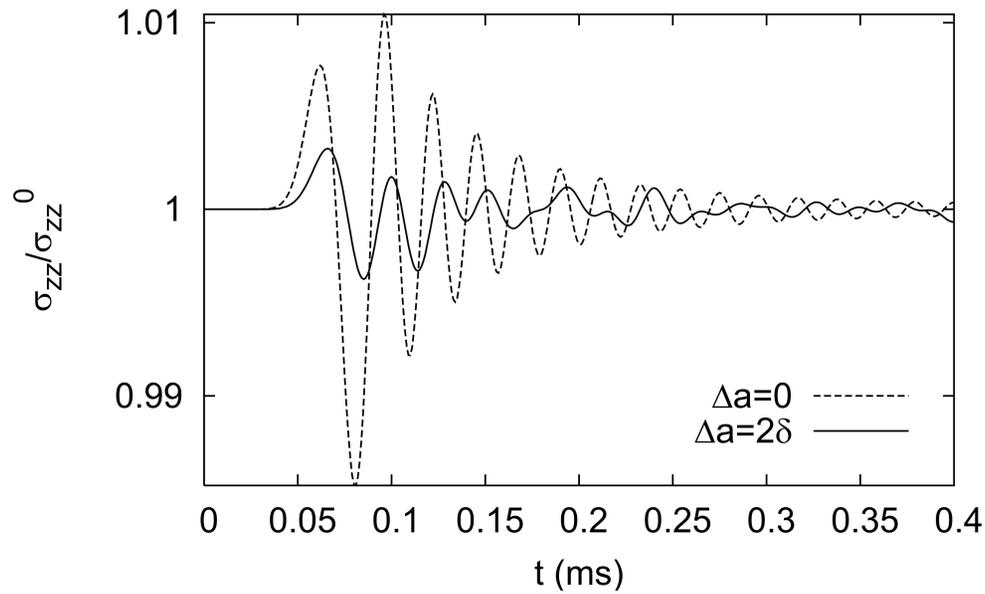
# Contacts



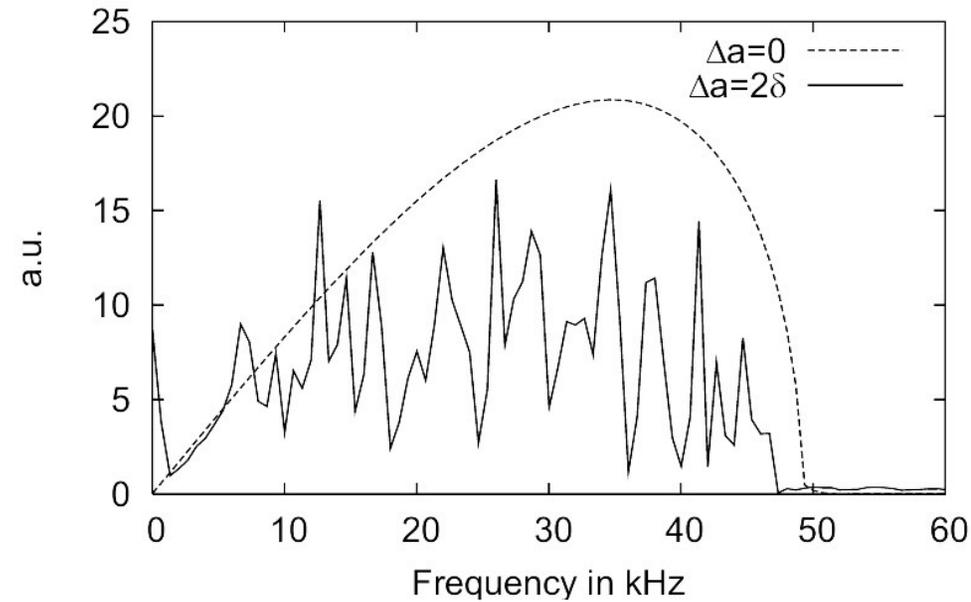
# P-wave animation



# Signals Analysis

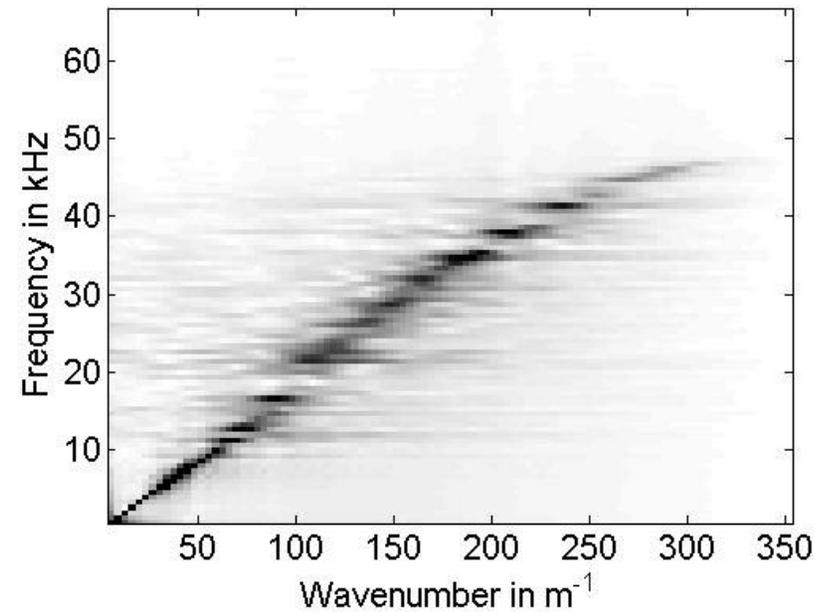
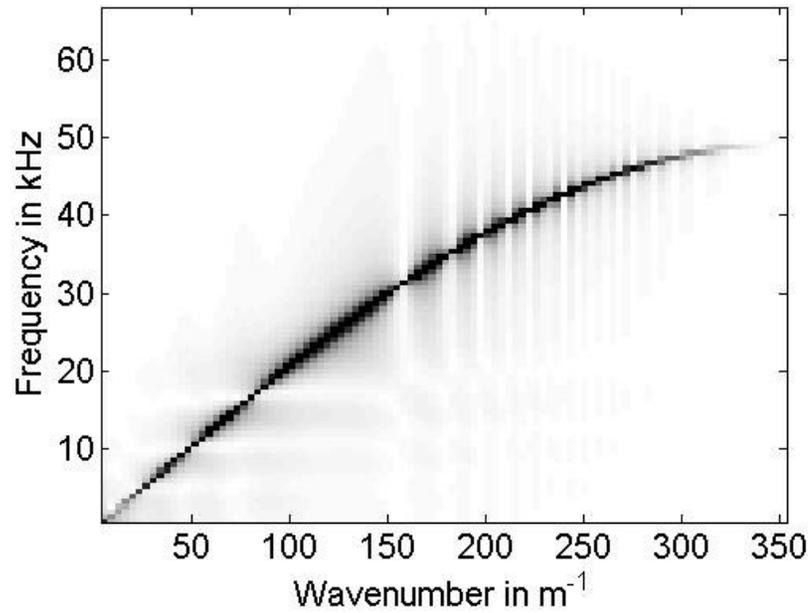


Stress-time signal

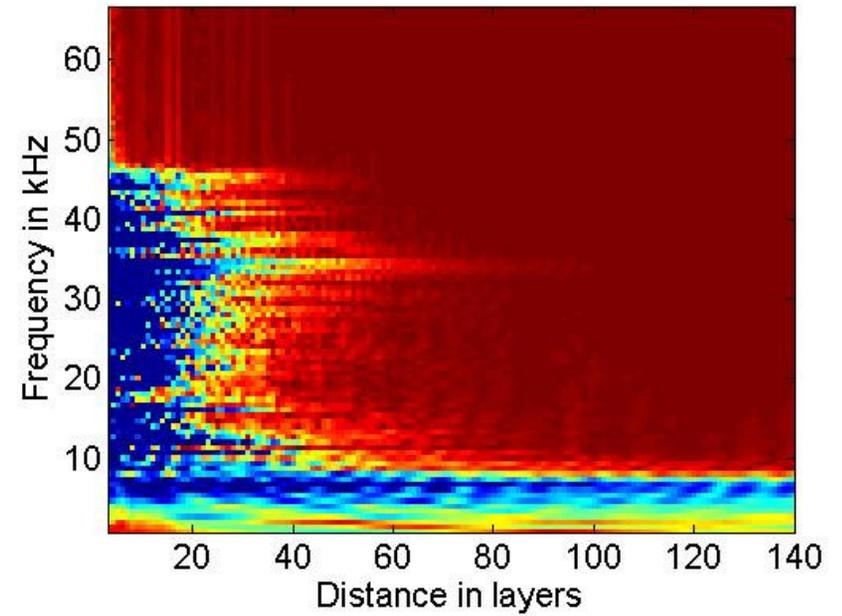
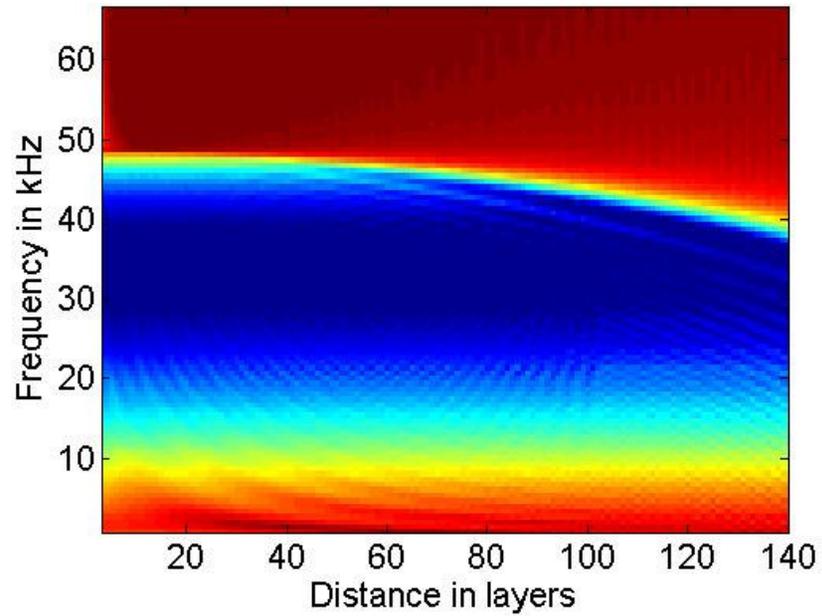


Power-spectrum

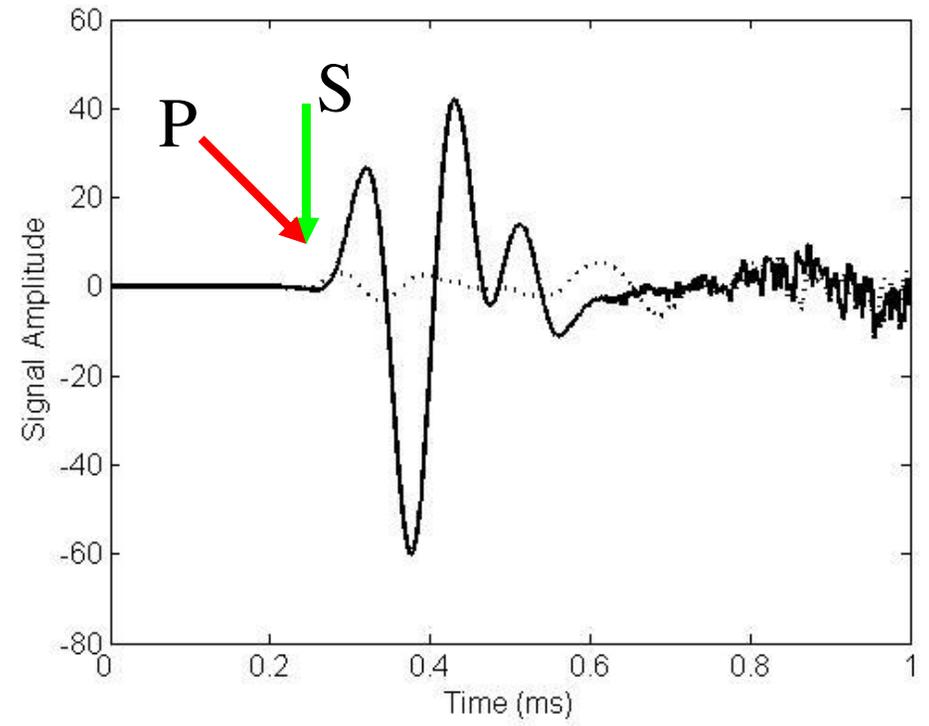
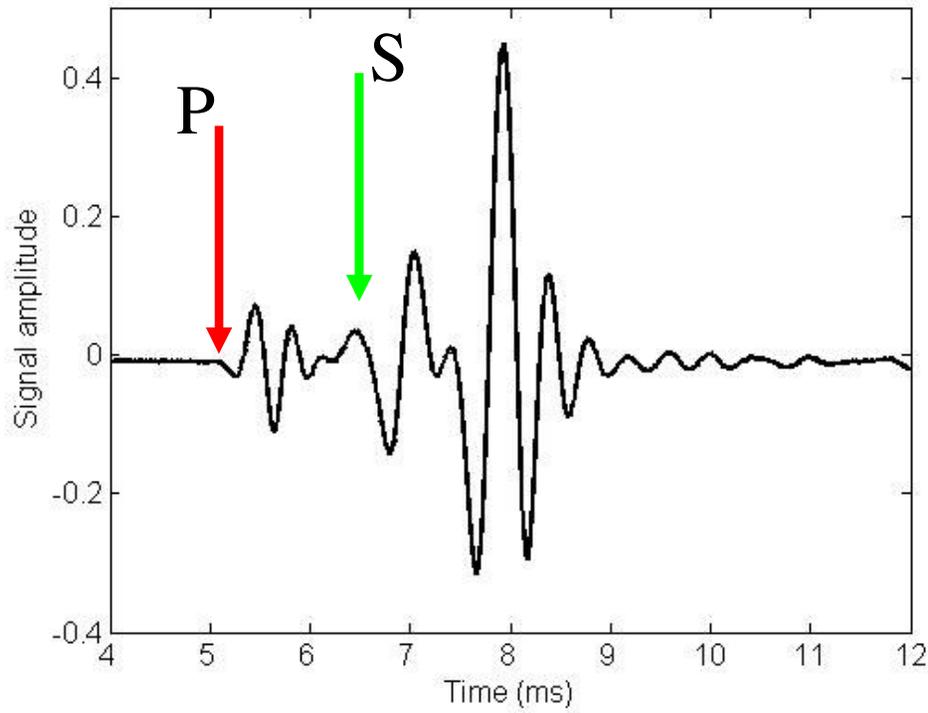
# Dispersion relations



# Frequency-space Diagrams



# Experiment versus Simulation



# Conclusions

- The model is able to mimic some well-known phenomena of the wave propagation in granular matter.
- When complexity increases not all features are understood, however in some cases the influence of parameters is characterized.

# Perspectives

- What is predictable from the initial system?

**Micro-parameters and structure > Macro/continuum**

- Experiments