#### JMBC Workshop "Statics and dynamics of soft and granular materials" Drienerburght, University of Twente, February 25 - March 1, 2013

Speakers: Dirk van der Ende - Nico Gray - Detlef Lohse - Stefan Luding - Martin van Hecke Martin van der Hoef - Devaraj van der Meer - Peter Schall - Vicenzo Vitelli



Many materials, often grouped together using the term 'soft matter', share common characteristics and behavior: For example, the materials consist of macroscopic particles, larger than the molecules that build up the world around us. They jam when flow is about to stop, and unjam just before flow starts. The static ('solid') situation is often characterized by a high degree of disorder, inhomogeneity and anisotropy, while the dynamic ('fluid') situation is frequently dominated by dissipative interaction forces leading to a dissipation time scale that interacts with other time scales in the system. Finally, there is the role of the interstitial fluid that resides between the particles and may mediate thermal (Brownian) motion, in the case of colloids, or hydrodynamic interactions (drag) in the case of macroscopic grains. This course, aimed at graduate students, will provide an introduction to this type of materials and discuss many of the phenomena mentioned above both as an overview and in the context of actual research.

	MONDAY February 25, 2013	TUESDAY February 26, 2013	WEDNESDAY February 27, 2013	THURSDAY February 28, 2013	FRIDAY March 1, 2013
09:00 - 10:45		Granular avalanches (Nico Gray)	Simulation of granular two-phase flows 1 (Martin v/d Hoef)	Rheology and microstructure of dispersions (Dirk v/d Ende)	Granular matter and interstitial fluids (v/d Meer/Luding)
		Student talks			
0:45 - 11:15	Welcome	coffee & tea	coffee & tea	coffee & tea	coffee & tea
1:15 - 12:15	Introduction (Devaraj v/d Meer)	Particle segregation in granular free-surface flows (Nico Gray)	Simulation of granular two-phase flows 2 (Martin v/d Hoef)	Student talks	Impact on granular solids (Detlef Lohse)
2:15 - 13:30	lunch	lunch	lunch	lunch	
3:30 - 15:15	Mechanical metamaterials 1 (Martin v Hecke)	From particle description to continuum rheology (Stefan Luding)	Shocks in fragile matter 1 (Vicenzo Vitelli)	Jamming and glassy behavior in colloids and grains 1 (Peter Schall)	
5:15 - 15:45	coffee & tea	coffee & tea	coffee & tea	coffee & tea	
5:45 - 17:30	Mechanical metamaterials 2 (Martin v Hecke)	What is rheology about? (Dirk v/d Ende)	Shocks in fragile matter 2 (Vicenzo Vitelli)	Jamming and glassy behavior in colloids and grains 2 (Peter Schall)	
8:30 - 21:00				Conference dinner	

## What is soft Matter?

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## **Soft Matter physics is:**

the physics (statics/dynamics) of a system consisting of many particles at a scale on which quantum effects are not important.

#### **Soft Matter includes:**



#### and many biological materials.





## The tools of Soft Matter physics

All the tools of physics that do not contain the words "quantum" or "high energy": COPETHNECKAR QUANK

- (Nonlinear) Mechanics **V1**
- **V2 Classical fields**
- V5 & V9 (Far from equilibrium) Statistical physics MEXAHIKA
- **Fluid Mechanics V6**
- **V7 Elasticity**
- Electromagnetism **V8**
- **V10 Kinetic Theory**

This is 8 out of 10 volumes of Landau & Lifshitz famous "Course of Theoretical Physics"

## Soft and granular matter may behave...

#### ... as a solid

#### ... as a liquid

#### ... or as a gas

## Soft and granular matter may behave...

#### or, even worse, as all three simultaneously!

#### Impact on a granular solid

#### Ball dropped onto loose, very fine sand



#### Impact on a granular solid

#### Ball dropped onto loose, very fine sand



#### Impact on a granular solid

#### Ball dropped onto loose, very fine sand



What sets these materials apart from their molecular counterparts ?

To some or large extent, they:

1. are athermal

2. interact through contact forces

3. have dissipative interactions

4. are inhomogeneous

#### 1. Granular matter is athermal

#### **Definition:**

Granular matter = many body system in which the typical particle size > 10 µm

$$\frac{1}{2}mv_{\text{thermal}}^2 = \frac{3}{2}k_BT \implies \text{(at room temperature)}$$

$$v_{\text{thermal}} = \sqrt{\frac{3k_BT}{\frac{4}{3}\pi r^3\rho}} \approx \sqrt{\frac{10^{-20}}{10^{-11}}} \approx 3 \cdot 10^{-5} \text{ m/s}$$

Thermal energy is negligible for such particles !

## When does thermal motion matter?



Droplet (radius *a*) in liquid with viscosity  $\eta$  and density  $\rho_l$ . Flow with shear rate  $\dot{y}$ .

#### **Péclet number:**



$$D_0 = \frac{k_B T}{6\pi\eta a}$$

(Stokes-Einstein FDR)

Péclet number (sedimentation):

$$\operatorname{Pe}_{\rm s} = \frac{4}{3}\pi \, \frac{\Delta \rho \, g \, a^4}{k_B \, T}$$

$$\mathrm{Pe_s} \approx 1 \Rightarrow a \approx 500 \,\mathrm{nm}$$



#### 2. Contact forces

#### **Dominant for granular materials at rest**



"Chaotic" network of contact points and forces !

## **Static granular matter: Force Chains**



#### **Static granular matter: Force Chains**





(Bob Behringer, Duke)

## In stalling flow, force chains manifest themselves as arches



### **Reynolds dilatancy**



**Osborne Reynolds (1885):** 

"A strongly compacted granular medium dilates under pressure".





## **Metamaterials**





When compressed vertically, ordinary materials expand horizontally.

**v** > 0



When compressed vertically, tailored metamaterials compress horizontally.

**v** < 0



When compressed vertically, tailored metamaterials compress horizontally.

**v** < 0

#### **Stability of foams**



#### Jamming

A granular material with a packing fraction above a critical value  $\varphi_{J}$  is stable.



At  $\varphi_J$  the packing is marginally stable: any stress will destroy the packing

## Jamming diagrams



Andrea Liu, Sid Nagel Nature (1998)



Martin van Hecke, J. Phys.: Cond. Matt. (2010)



Dapeng Bi, Jie Zhang, Bulbul Chakraborty, Bob Behringer, Nature (2011)

![](_page_36_Figure_0.jpeg)

#### Finite temperature: glassy behavior

![](_page_37_Figure_1.jpeg)

#### System quenched in a jammed or glass state

#### Finite temperature: glassy behavior

![](_page_38_Figure_1.jpeg)

## Close to point J: Very loose contact networks

#### response to uniform compression

![](_page_39_Picture_2.jpeg)

#### close to $\phi_J$ : displacement field has non-affine response

![](_page_40_Picture_0.jpeg)

#### close to $\varphi_J$ : displacement field has non-affine response

#### 3. Dissipative interactions

**Dissipative interactions may arise:** 

- as a result of motion through another medium (see 4)
  - Brownian motion (fluctuation-dissipation)
  - dissipation in medium (viscosity, turbulence)
- as a result of contact forces:
  - friction
  - inelastic collisions

transfer of kinetic energy into other degrees of freedom.

![](_page_42_Figure_0.jpeg)

Grains have many internal degrees of freedom through which kinetic energy is dissipated. (sound, heat, deformation)

## 4. Inhomogeneous

Soft Matter is usually inhomogeneous. There are two main causes:

- 1. The inhomogeneity is caused by the (unavoidable) presence of an interstitial fluid (*intrinsic*).
  - colloids are particles subject to Brownian motion and hydrodynamic interactions with the embedding fluid.
     network are modeled as Brownian particle environment
  - polymers are modeled as Brownian particle-springs
- 2. The inhomogeneity is due to inhomogeneity of the material (*external*).
  - granular materials can be bidisperse or polydisperse
  - clay is a material made up of clay (nanoscale) and silica particles

### Vibrated bidisperse mixture

![](_page_44_Picture_1.jpeg)

#### **Segregation !**

#### "Brazil Nut Effect"

![](_page_45_Picture_1.jpeg)

## **Three explanations BNE**

- **1. percolation:**
- small grains percolate the empty spotsbetween the large ones.
- 2. exclusion:
- while vibrating small grains fill space below the large ones, not vice versa.
- 3. convection:
- interaction with walls trigger convection rolls.

![](_page_46_Figure_7.jpeg)

large grains can follow the upward, but not the downward flow.

## **Three explanations BNE**

- **1. percolation:** small grains percolate the empty spots between the large ones.
- **2. exclusion:** while vibrating small grains fill space below the large ones, not vice versa.
- 3. convection: interaction with walls trigger nvoction rolls. Tuesday morning: Nico Gray Granular avalanches & particle segregation arge grains can follow the upward, but not the downward flow.

## Role of intersitial air: single particle

$$F_{drag} = 3\pi\eta dV$$

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$$F_{g} = \frac{1}{6}\pi d^{3}\rho_{p}g$$

$$d =$$
 particle diameter  
 $V =$  typical particle velocity  
 $\eta =$  air viscosity (2.10<sup>-5</sup> Pa·s)  
 $\rho_p =$  part. density (2.5.10<sup>3</sup> kg/m<sup>3</sup>)  
 $g =$  grav. acceleration (10 m/s<sup>2</sup>)

 $\rho_p g$ 

$$B \equiv \frac{F_{drag}}{F_g} = \frac{18\eta V}{\rho_p g d^2}$$

$$B \approx 1 \to d \approx \sqrt{\frac{18\eta V}{\rho_p g}}$$

$$V \approx 1 \text{ m/s} \rightarrow d \approx 120 \ \mu \text{m}$$

$$V \approx \sqrt{2gd} \rightarrow d \approx 16 \ \mu \mathrm{m}$$

### Role of interstitial air: packed particle

$$F_{f \to s} = 2k \frac{1-\varepsilon}{\varepsilon^3} F_{drag}$$

$$\int \int F_g = \frac{1}{6}\pi d^3 \rho_p g$$

 $\varepsilon = 1 - \varphi = \text{porosity} (\approx 0.5)$ k = Kozeny constant ( $\approx 5$ )

$$B_p \equiv \frac{F_{f \to s}}{F_g} \approx 40 \frac{18 \eta V}{\rho_p g d^2}$$

$$B_p \approx 1 \to d \approx \sqrt{40} \sqrt{\frac{18\eta V}{\rho_p g}}$$

 $V \approx 1 \text{ m/s} \rightarrow d \approx 760 \ \mu\text{m}$  $V \approx \sqrt{2gd} \rightarrow d \approx 190 \ \mu\text{m}$ 

## **Faraday heaping**

Vertically vibrated granular layer: Numerical simulation of heaping with a hybrid GD-CFD code

![](_page_50_Picture_2.jpeg)

![](_page_51_Picture_0.jpeg)

### Interstitial liquids: suspensions

![](_page_52_Picture_1.jpeg)

#### a granular suspension: cornstarch on a shaker

## Walking on cornstarch

![](_page_53_Picture_1.jpeg)

#### Walking on cornstarch

Friday morning: Stefan Luding / Devaraj van der Meer Granular matter and interstitial fluids

## **Macroscopic vs microscopic** Viscoplastic Bingham Plaștic Shear Stress

![](_page_55_Figure_1.jpeg)

![](_page_56_Figure_0.jpeg)

Why is Soft Matter a booming subject in physics ?

There are many reasons, but one has been absolutely crucial:

![](_page_57_Picture_2.jpeg)

#### **Some numerical techniques**

- Brownian dynamics
- Monte Carlo
- molecular dynamics
- Iattice Boltzmann
- Event driven hard sphere dynamics
- Hard sphere dynamics
- Soft sphere dynamics
- Two or multiple fluid models
- Multi-particle collision dynamics
- Hybrid MD lattice Boltzmann
- Stochastic rotation dynamics
- Hybrid granular dynamics computational fluid dynamics

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Hybrid granular dynamics computational fluid dynamics

Tuesday afternoon: Stefan Luding From particle description to continuum rheology

# Thank you!