

JMBC Workshop

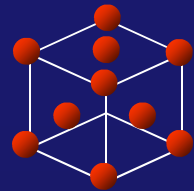
Jamming and glassy behavior in colloids

3. Insight from Colloidal Glasses

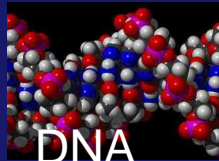
Peter Schall

University of Amsterdam

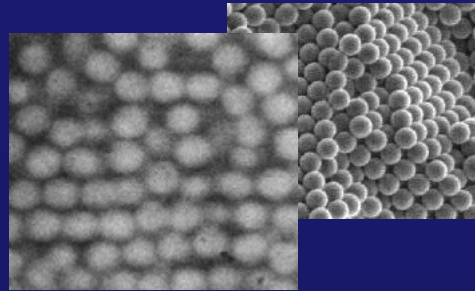
Colloidal suspensions



Atoms



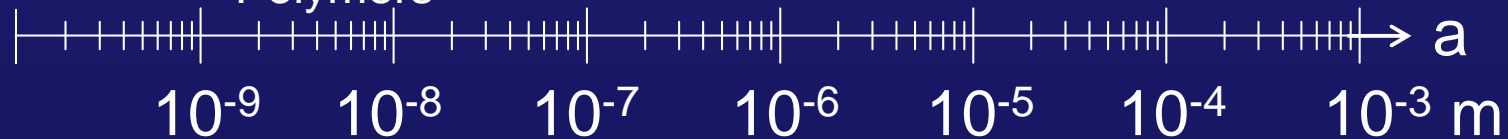
DNA
Polymers



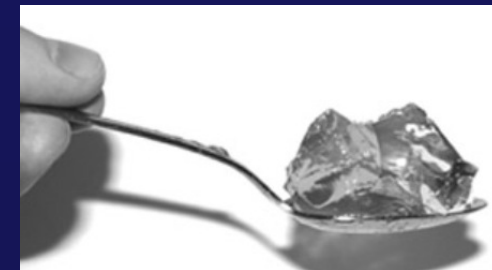
Colloids



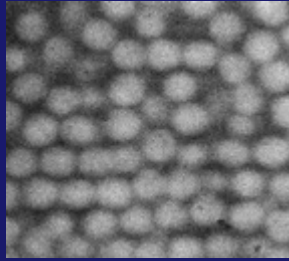
Granular



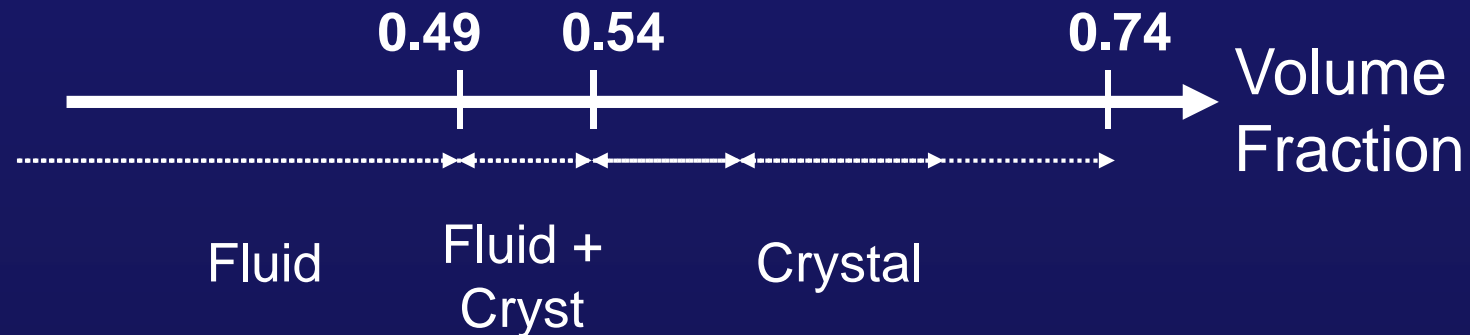
Why important ?



Colloidal Hard Spheres

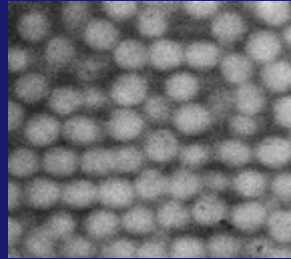


Hard-sphere Phase Diagram

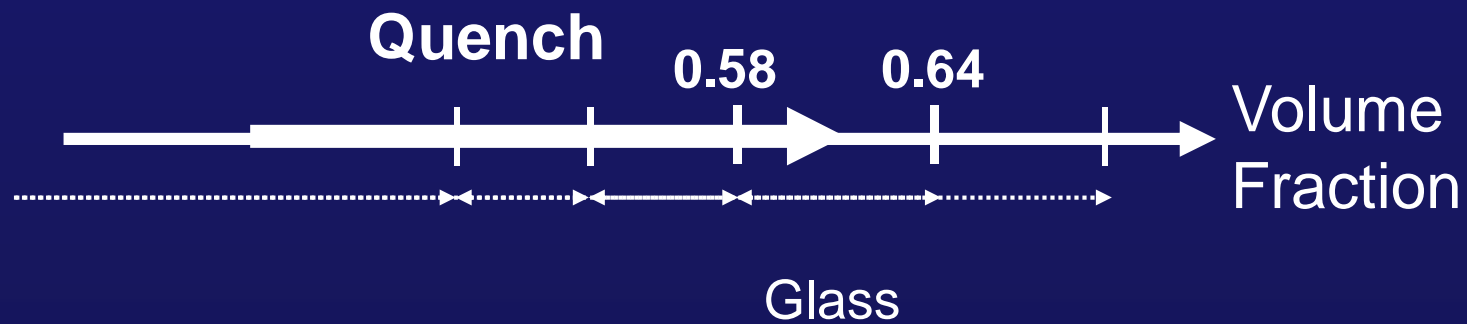


(Alder, Wainwright 1957)

Colloidal Hard Spheres

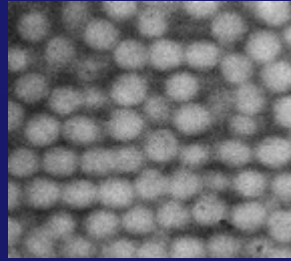


Hard-sphere Phase Diagram



(Alder, Wainwright 1957)

Colloidal Hard Spheres



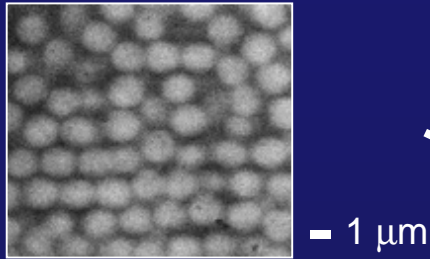
Scaling of the Moduli

Elastic Modulus \sim Energy / a^3



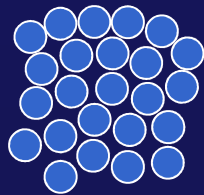
Colloidal suspensions

Colloidal Glasses

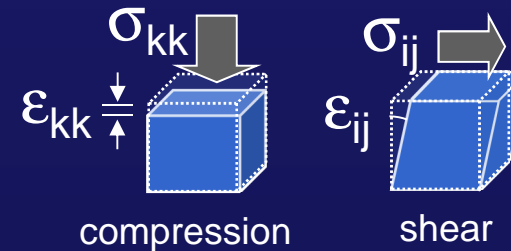


1. Thermal Energy
 kT

2. Structure: Glass
no long-range order



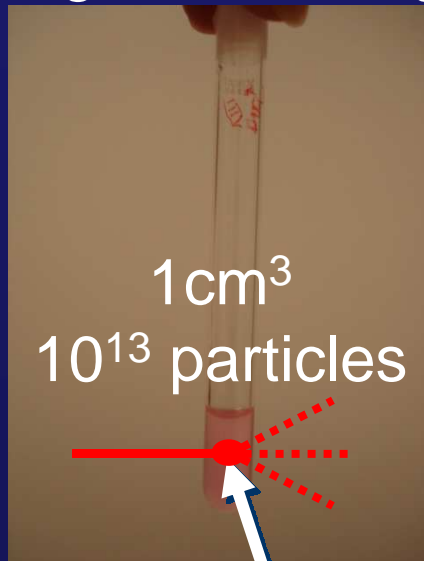
3. Dense system
Elastic modulus



Observation of Colloids

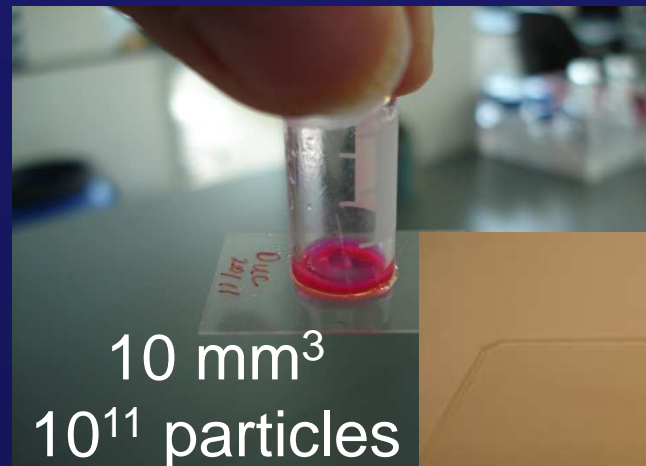
Colloidal Systems Length Scale

Light scattering

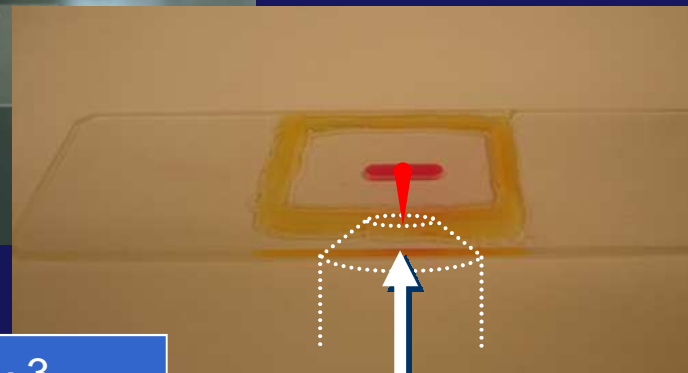


1mm^3
 10^9 particles

Microscopy



$10^6\ \mu\text{m}^3$
 2×10^5 particles



$\phi \sim 0.59$

Diameter $1.3 \mu\text{m}$

Lig

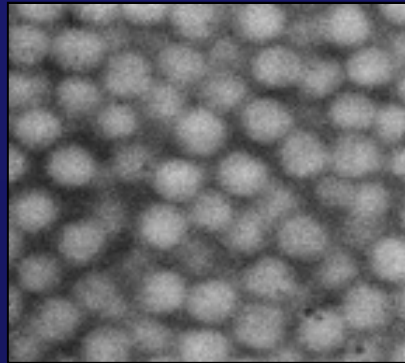
10

1mm^3
 10^9 particles

$10^6 \mu\text{m}^3$
 2×10^5 particles

Colloids: 3D Analogue Computers

Colloidal Systems Time Scale

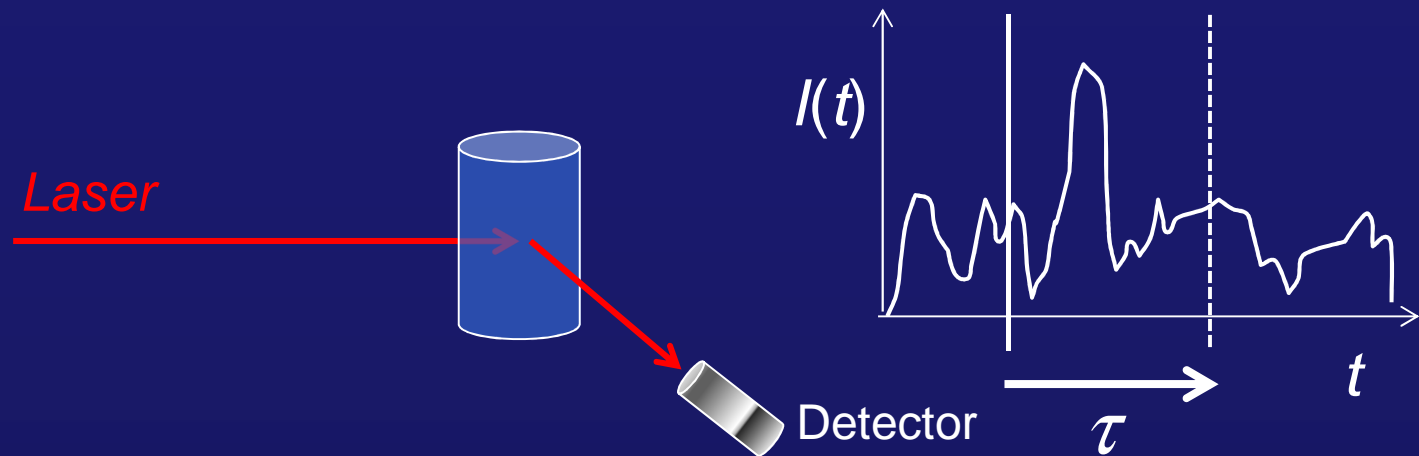


Collision time
 $\tau = (1/100) \text{ s}$

Total “simulation“ time : 10 h \approx 3million τ

Time increment : 1 min \approx 6000 τ

Light Scattering

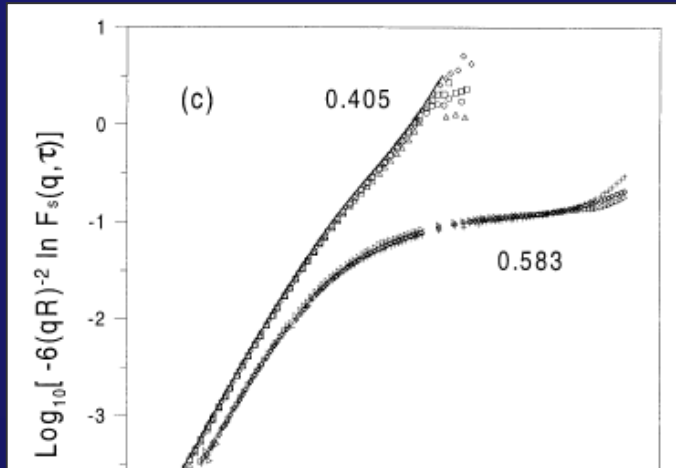


Time Auto Correlation Function

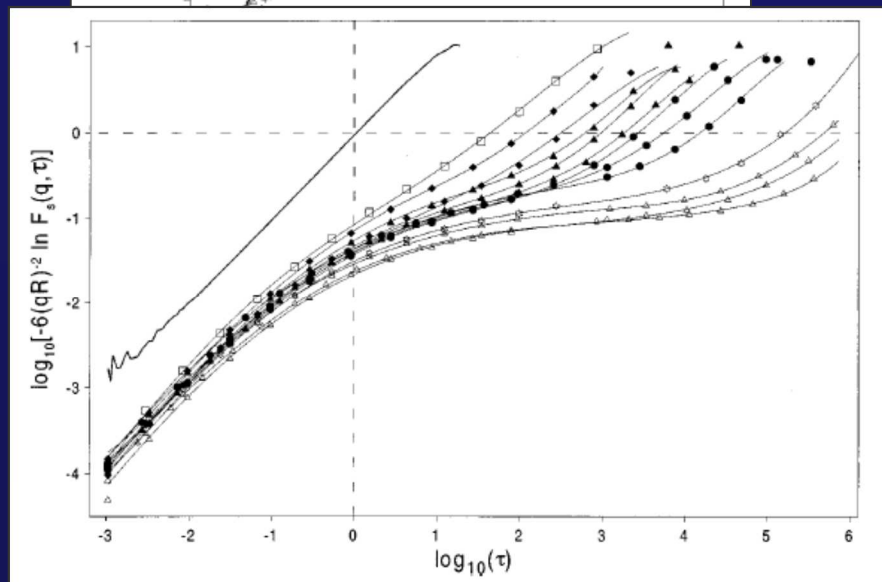
$$C(\tau) = \langle I(t)I(t + \tau) \rangle$$

$$C(\tau) \propto \exp(-Dq^2\tau)$$

Light Scattering

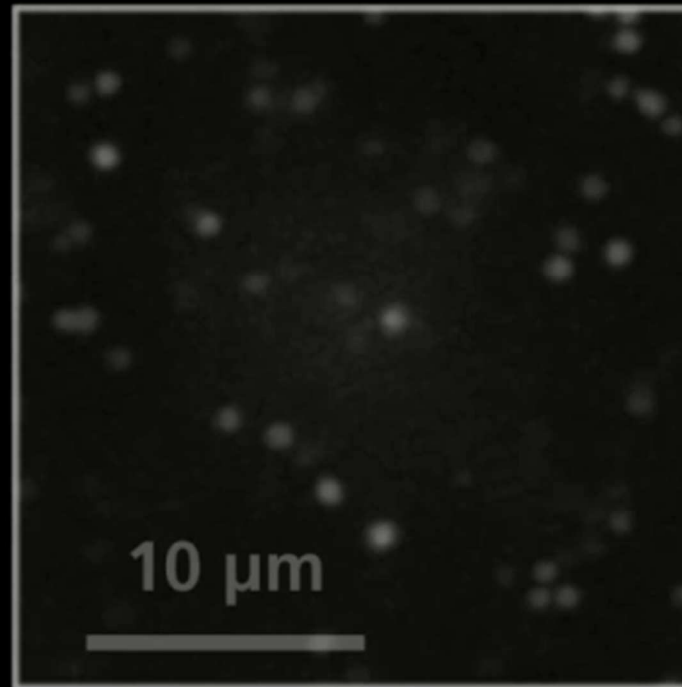


- Light scattering
van Megen *et al.* (PRE 1998)

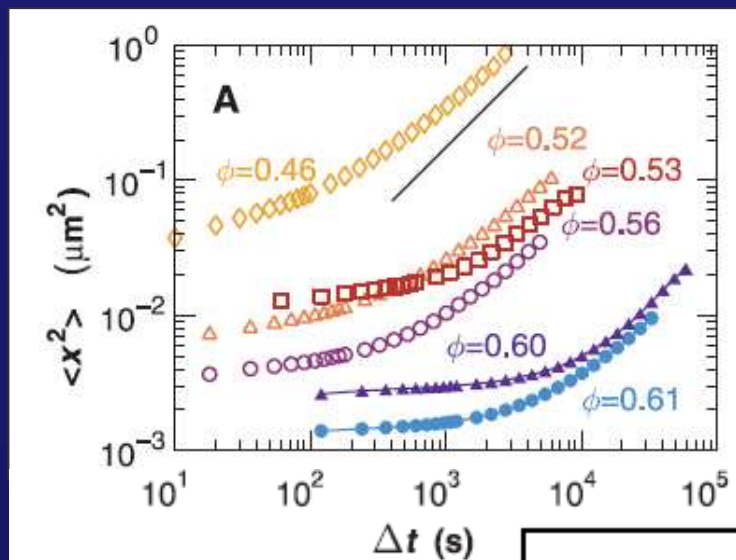


Colloidal glass transition
 $\phi_g \sim 0.57$

Confocal
Microscope
Image

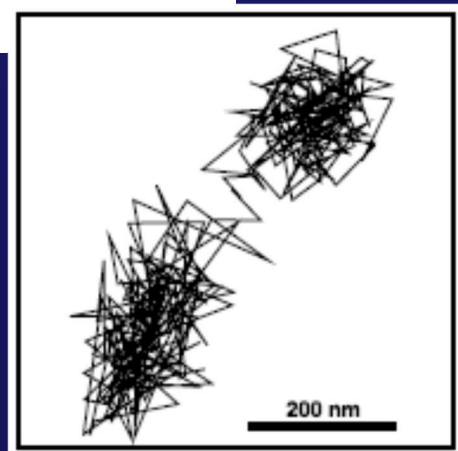


Colloidal Glasses

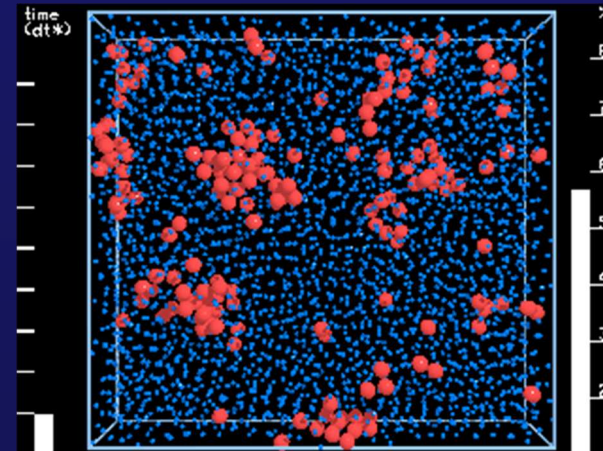


- Microscopy

Weeks, Weitz *et al.* (Science, 2000)

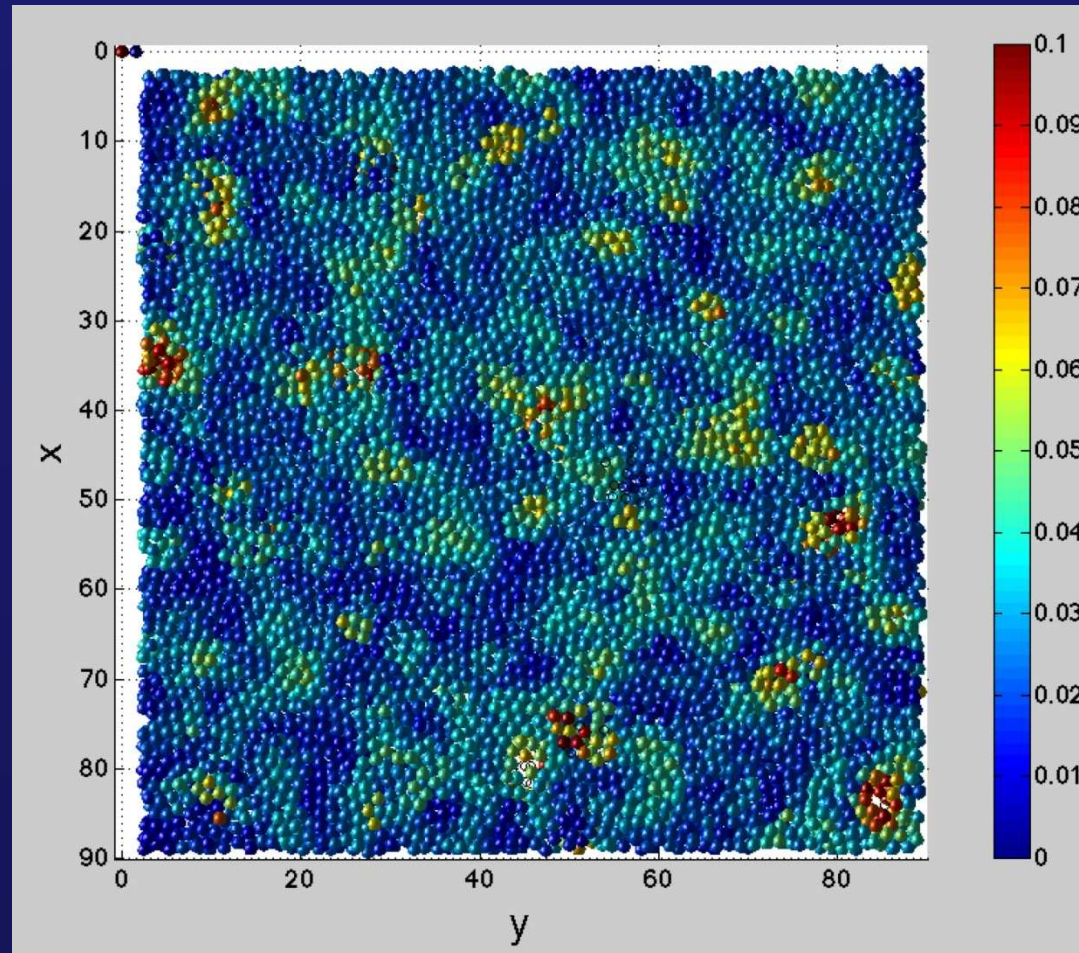


Caging



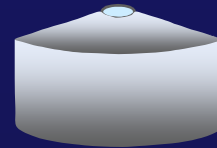
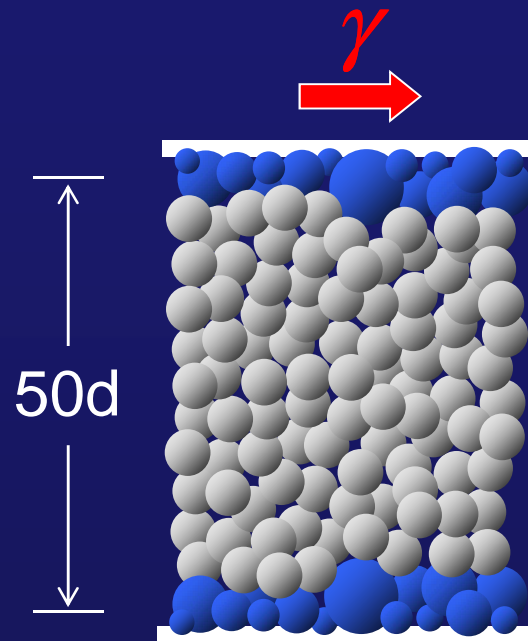
Dynamic heterogeneity

Free volume distribution



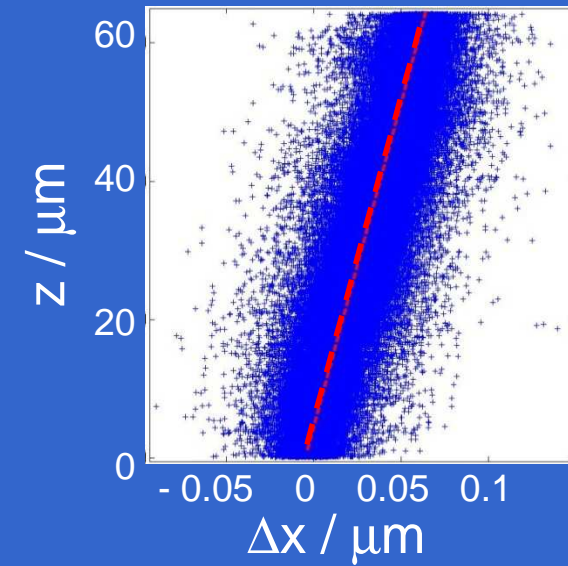
➔ Heterogeneous!

Application of str

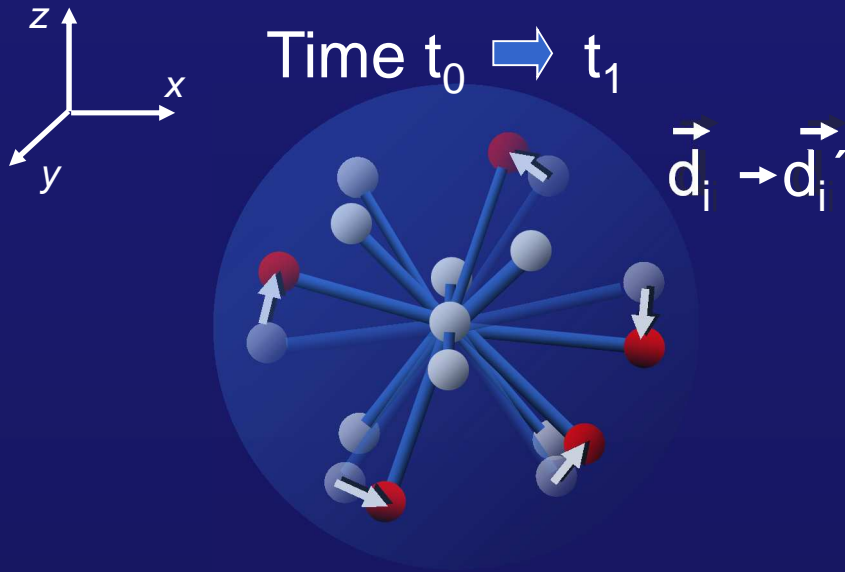


Confocal microscopy

Particle displacements



Strain and non-affine displacements



Affine transformation : γ

$$\vec{d}_i^{\text{aff}} = \vec{d}_i + \gamma \vec{d}_i$$

$$D_{\min}^2 = \sum_{\text{neighbors}} \left(\underbrace{\vec{d}_i' - \vec{d}_i}_{\text{actual change}} - \underbrace{\gamma \vec{d}_i}_{\text{affine change}} \right)^2$$

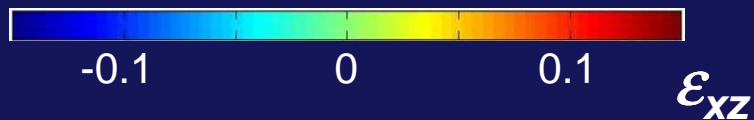
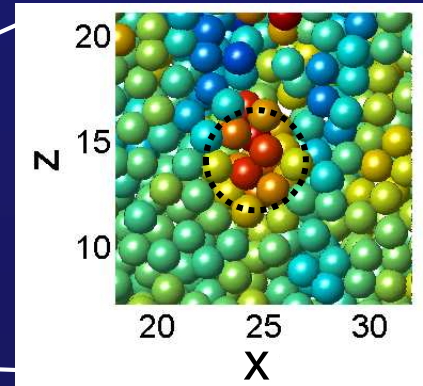
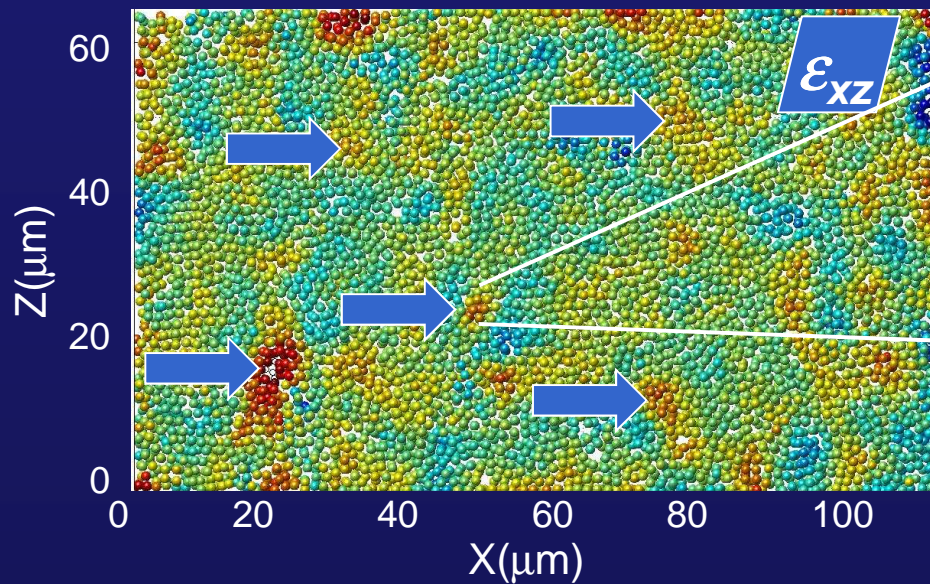
Symmetric part of γ

$$\text{Strain tensor } \varepsilon_{ij} = \begin{pmatrix} \varepsilon_{xx} & \varepsilon_{xy} & \varepsilon_{xz} \\ \varepsilon_{yx} & \varepsilon_{yy} & \varepsilon_{yz} \\ \varepsilon_{zx} & \varepsilon_{zy} & \varepsilon_{zz} \end{pmatrix}$$

STZ in colloidal glasses

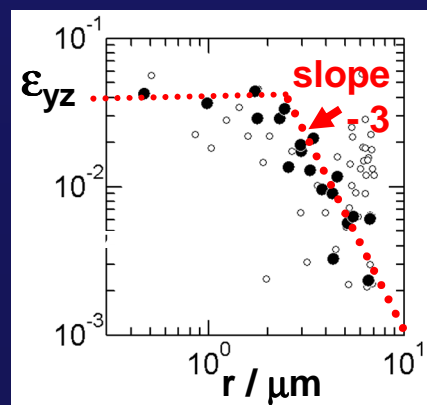
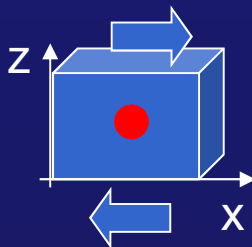
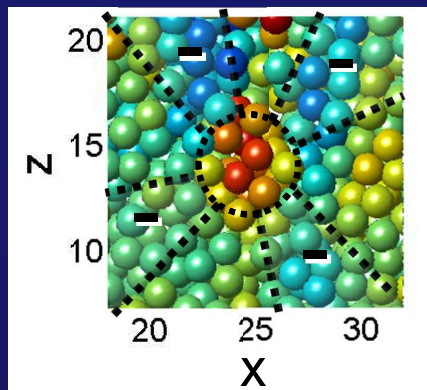
$$\dot{\gamma} \sim 1 \times 10^{-5} \text{ s}^{-1}$$
$$\dot{\gamma} \tau \sim 0.1$$

Affine part



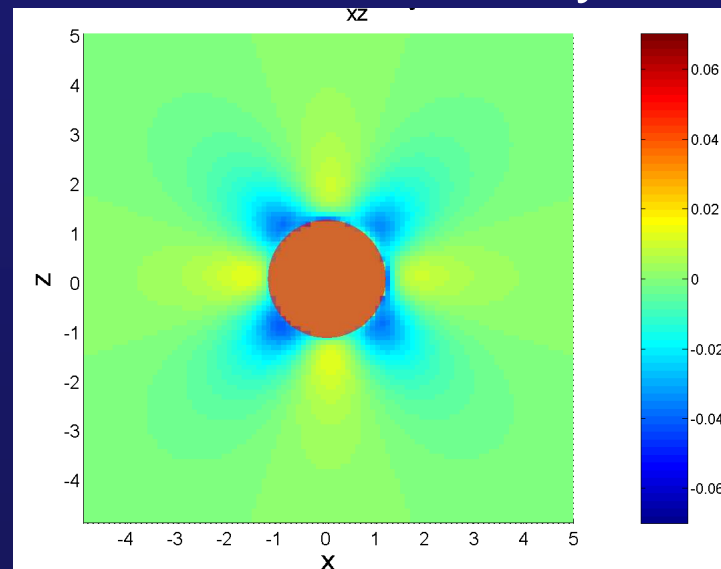
STZ in colloidal glasses

Incremental strain



$$\epsilon_{yz} \sim \frac{1}{r^3}$$

Continuum elasticity

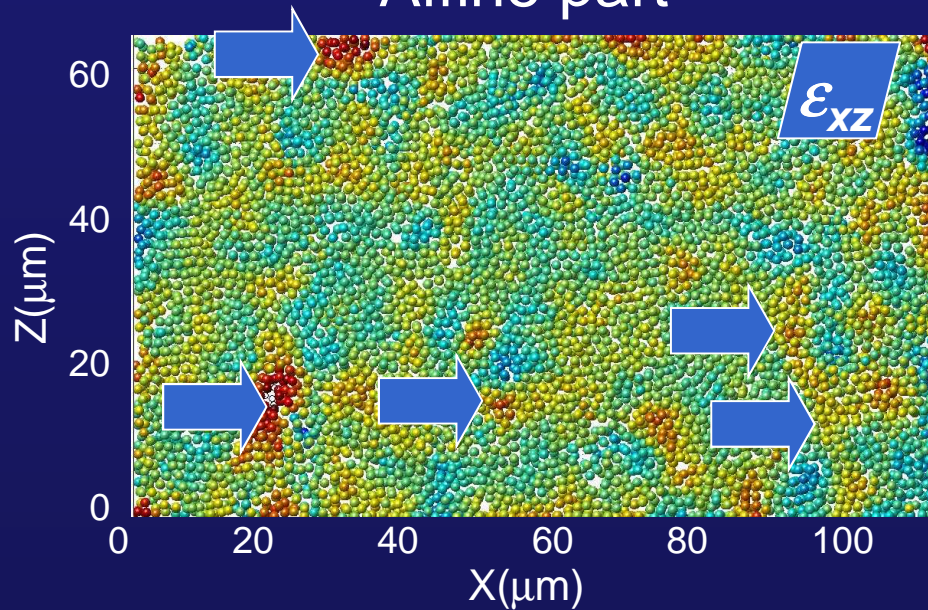


(PS, Weitz, Spaepen, Science 2007)

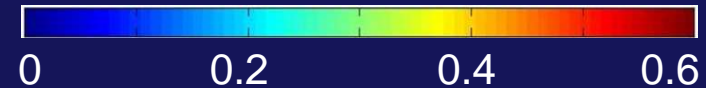
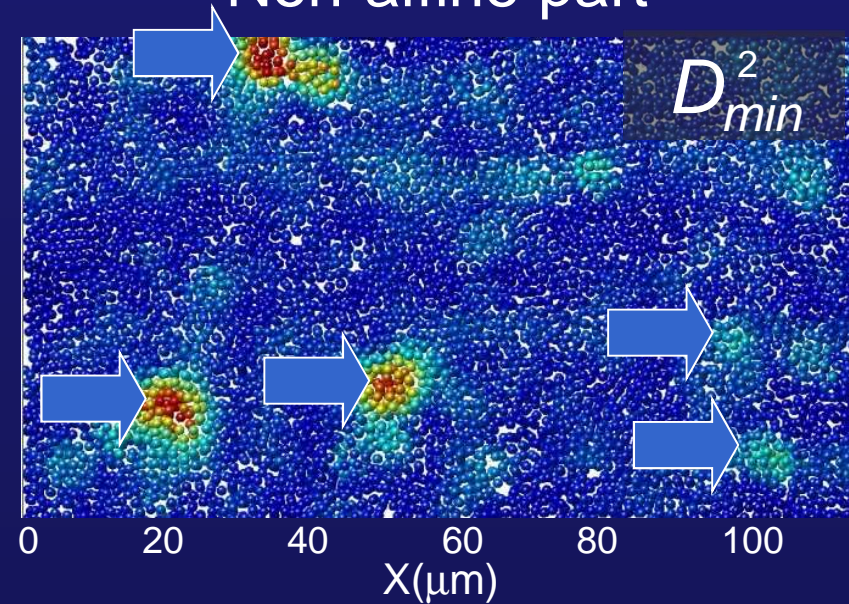
STZ in colloidal glasses

$$\dot{\gamma} \sim 1 \times 10^{-5} \text{ s}^{-1}$$
$$\dot{\gamma} \tau \sim 0.1$$

Affine part



Non-affine part

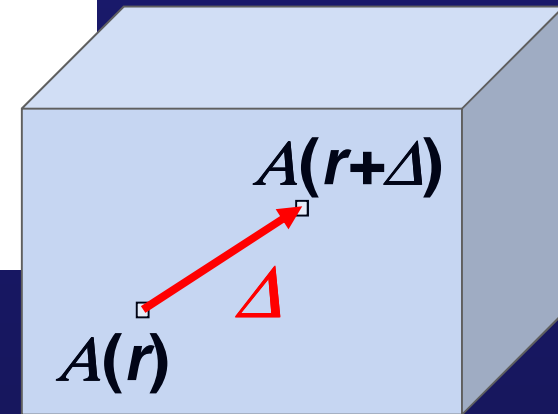


Spatial Correlations

$$C_A(\Delta) = \frac{\langle A(\bar{r})A(\bar{r} + \Delta) \rangle - (\langle A \rangle)^2}{\langle (A)^2 \rangle - (\langle A \rangle)^2}$$

Δ : *difference vector*

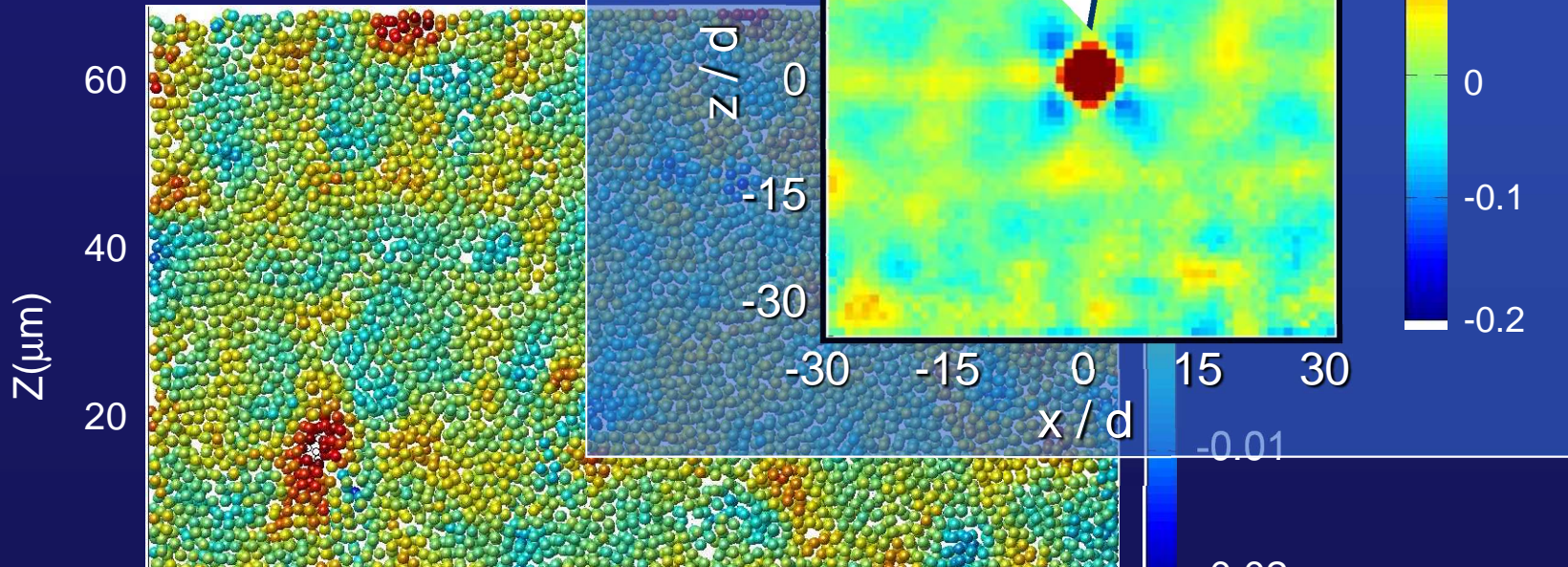
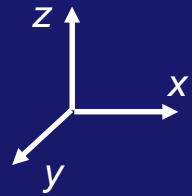
$\langle \rangle$: *spatial average*



Strain correlation : $A = \epsilon_{xz}$

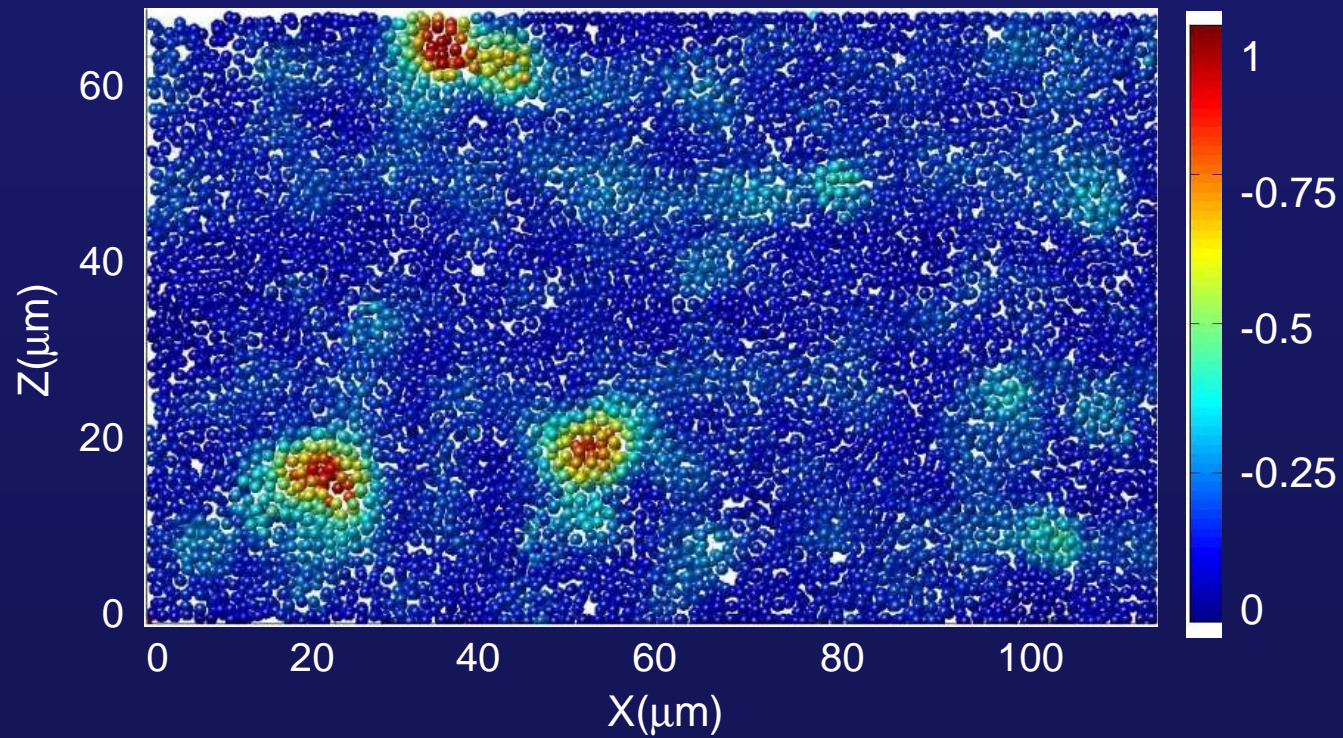
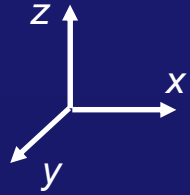
Non-affine correlation : $A = D^2_{min}$

Affine part: Shear Strain ϵ_{xz}

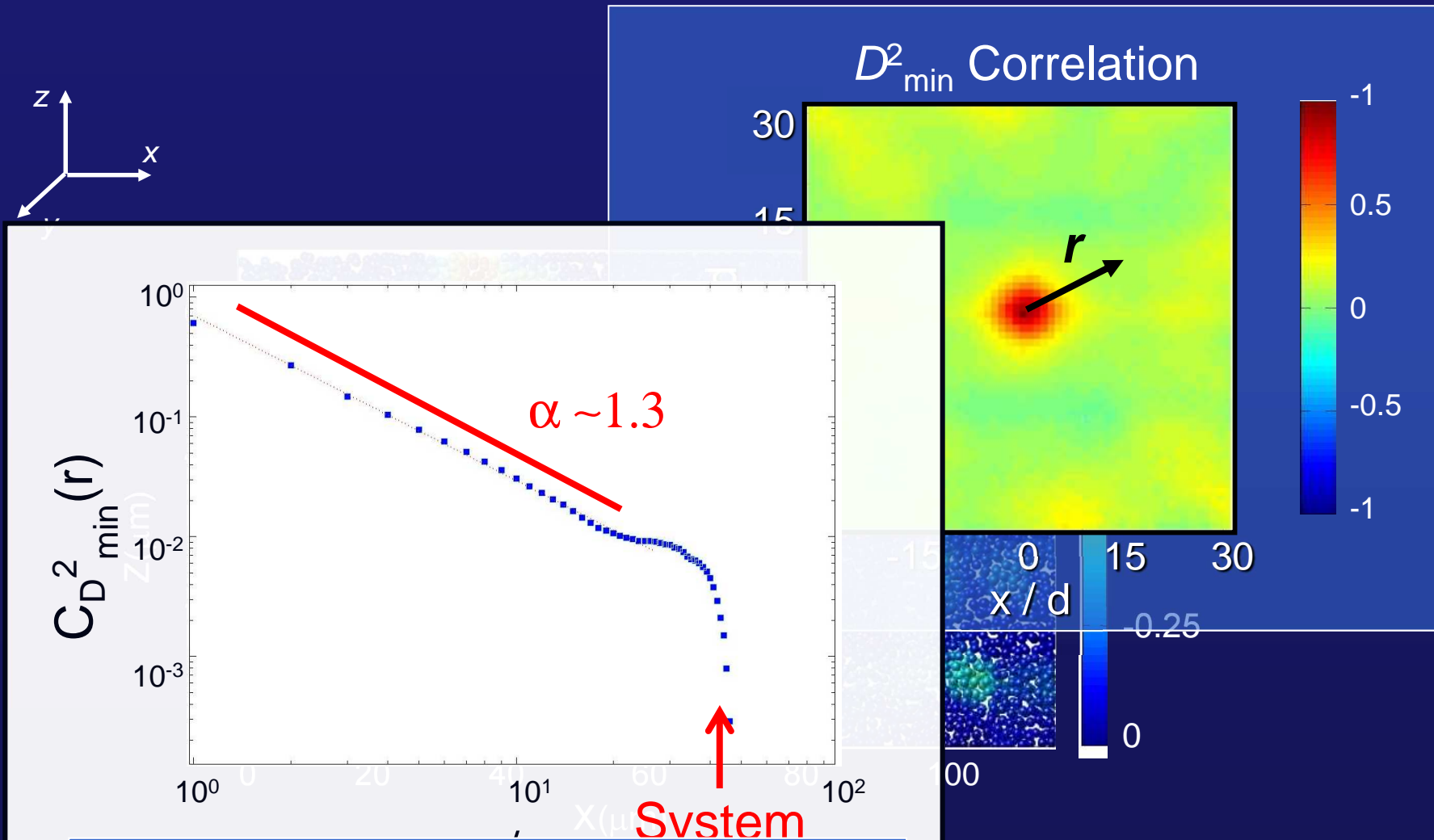


Elastic interactions
→ Self organization of STZ

Non-affine part



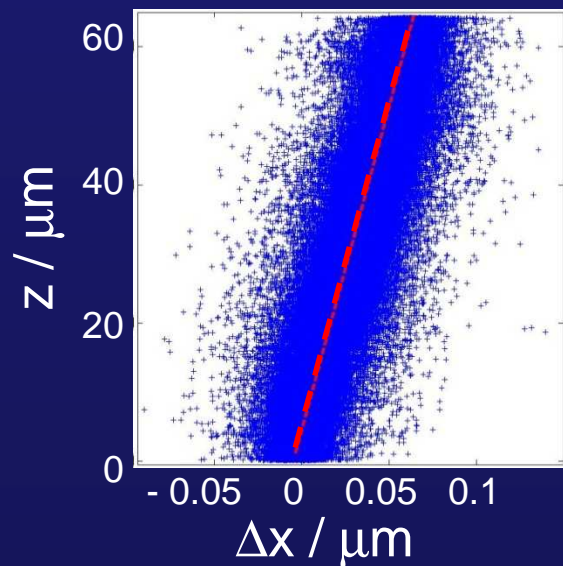
Non-affine part



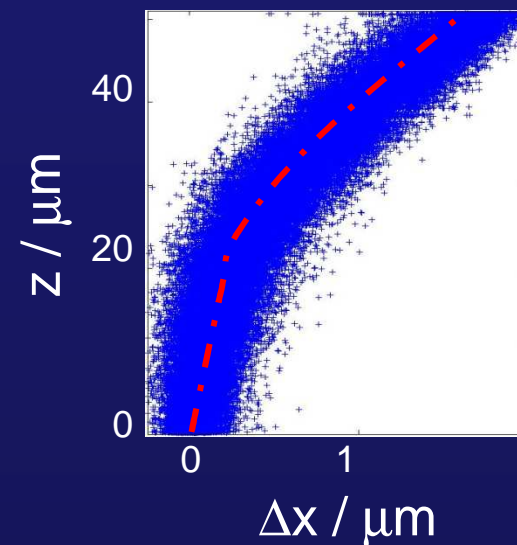
Power-law scaling
up to system size

Solid-Liquid transition: Shear banding

Homogeneous



Inhomogeneous

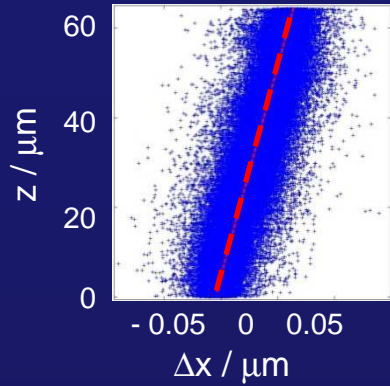


$\dot{\gamma}_c$

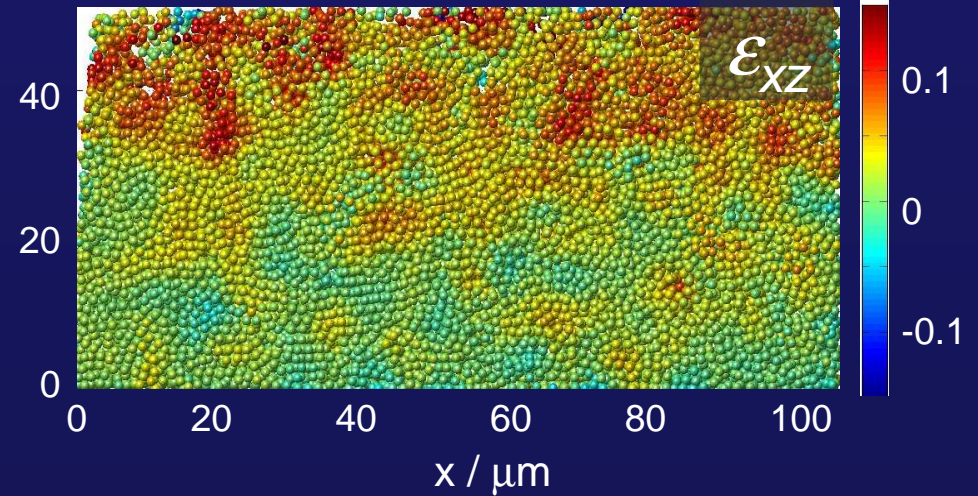
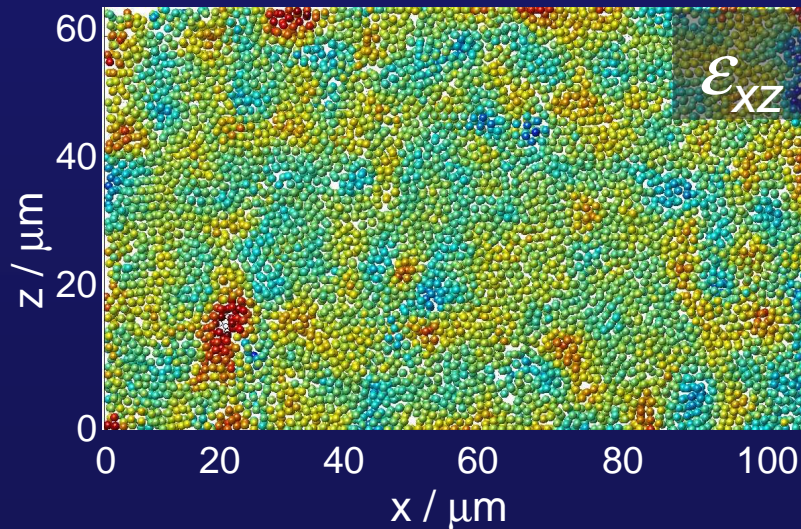
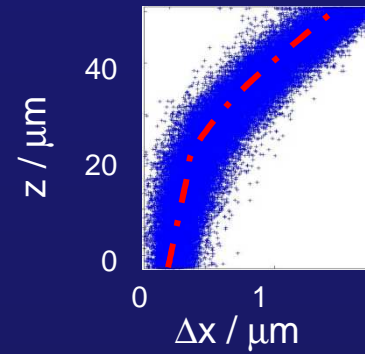
$\dot{\gamma} \text{ (s}^{-1}\text{)}$

Shear banding transition

Homogeneous



Inhomogeneous

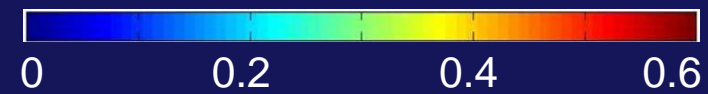
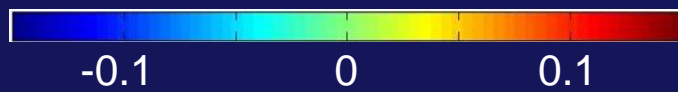
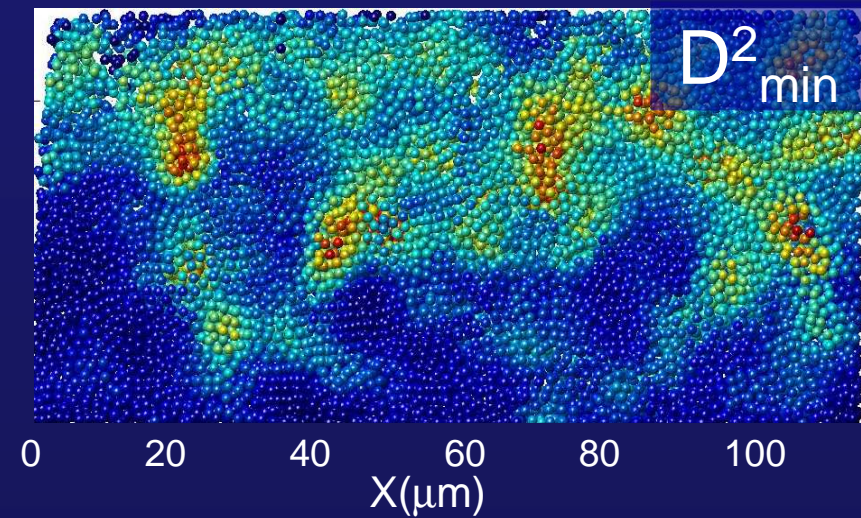
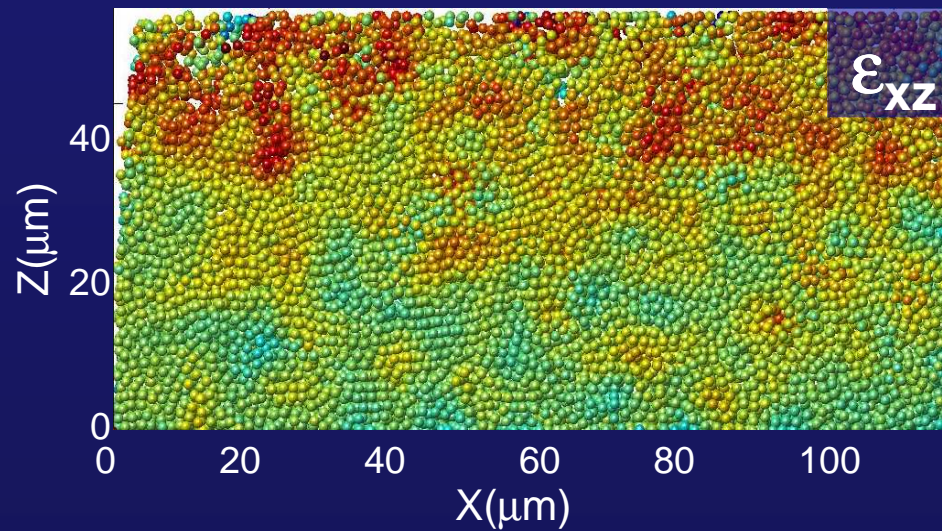
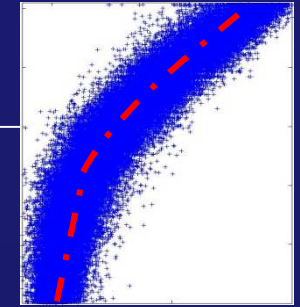


$\dot{\gamma}_c$

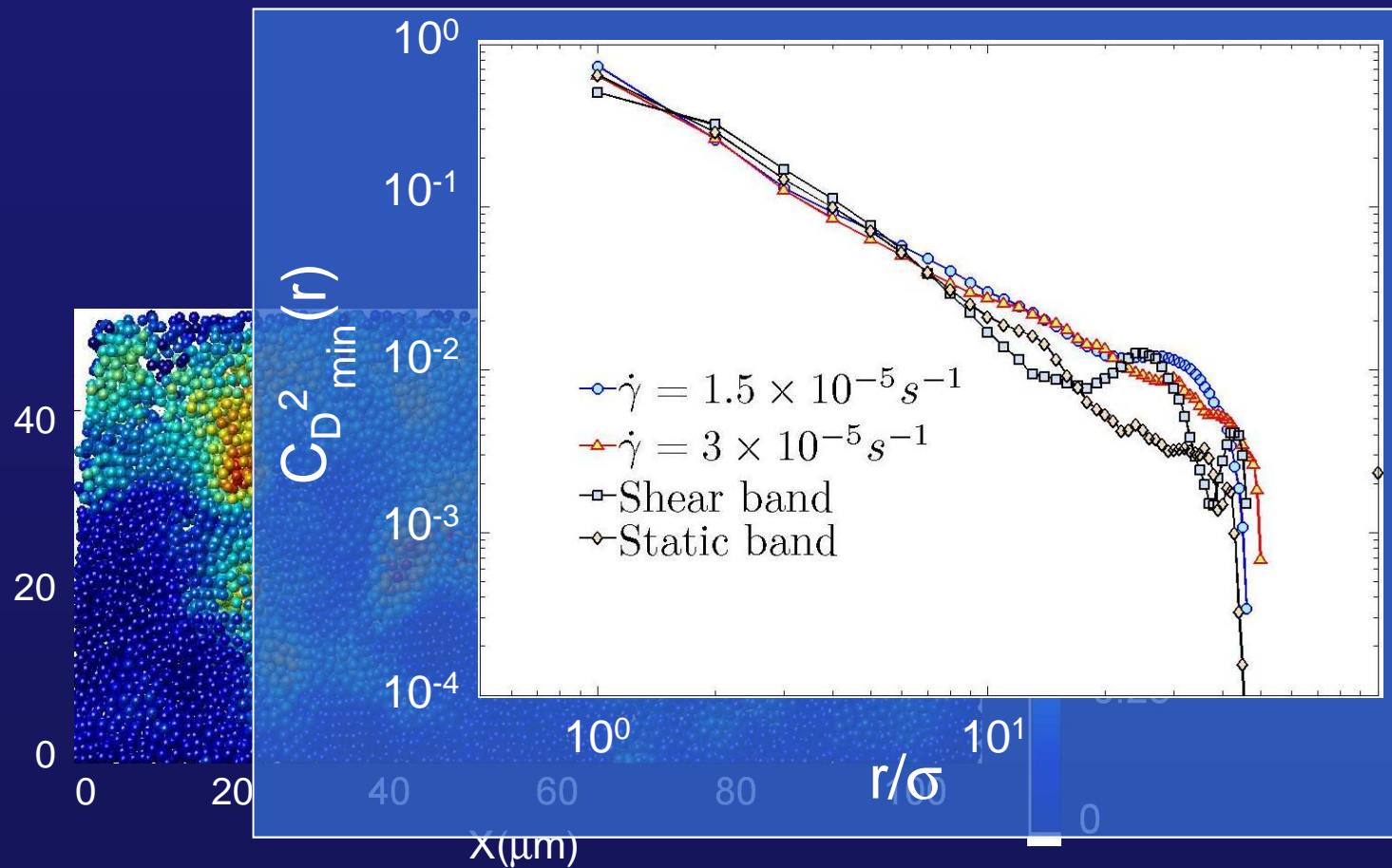
$\dot{\gamma} \text{ (s}^{-1}\text{)}$

Shear banding

$$\dot{\gamma} \sim 1 \times 10^{-4} \text{ s}^{-1}$$

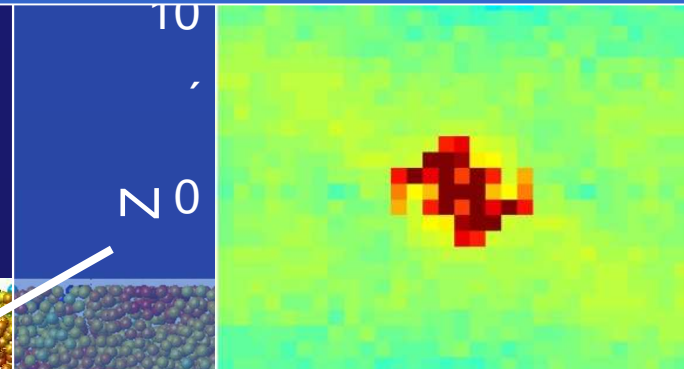


Spatial distribution of Flow ?

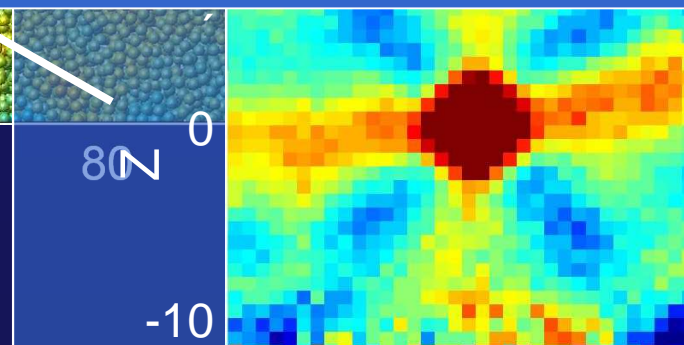
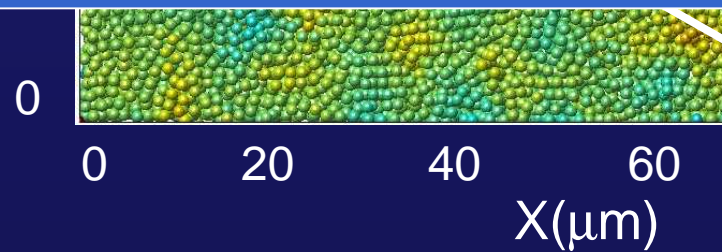


Strain Correlation function

No quadrupolar symmetry
liquid like

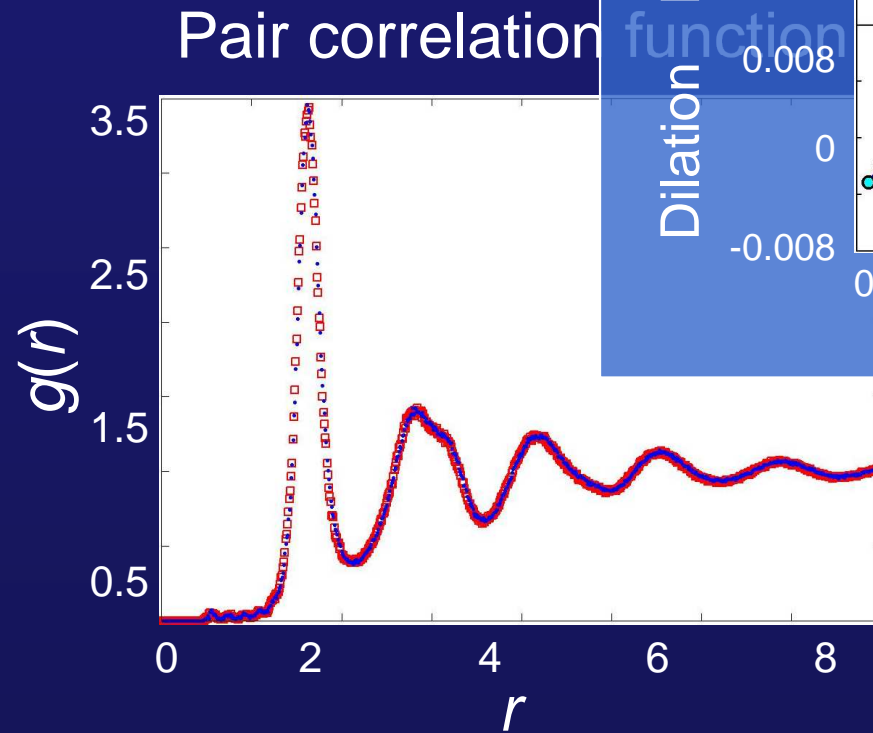


Fundamental Solid \rightarrow Liquid transition
Origin ?

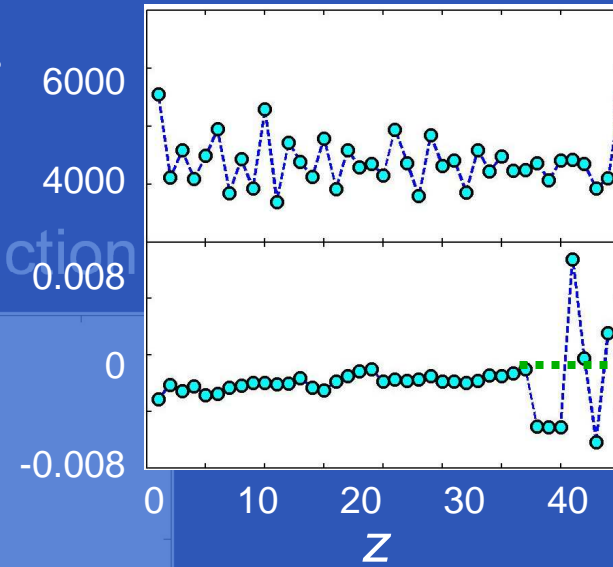


Quadrupolar symmetry
solid like

Structural transition ?

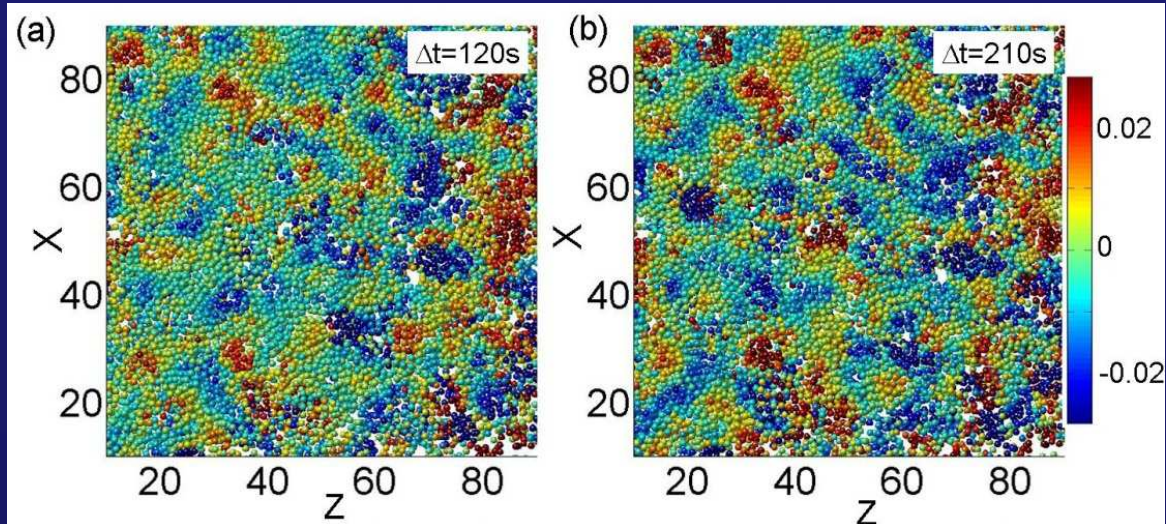


Dilation Density

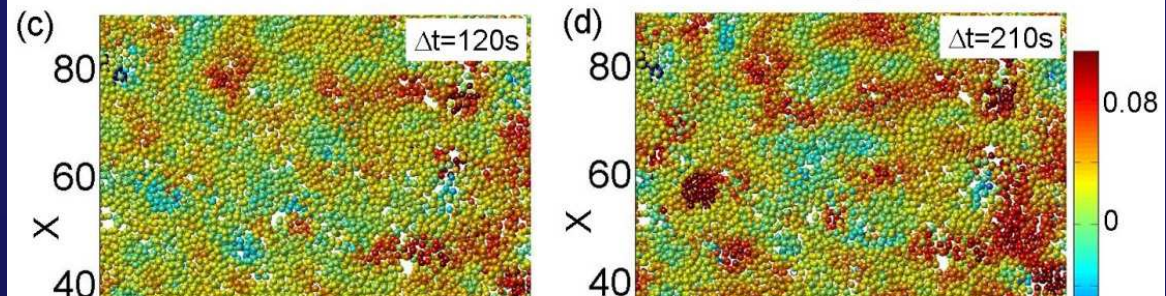


Shear banding

Dilation

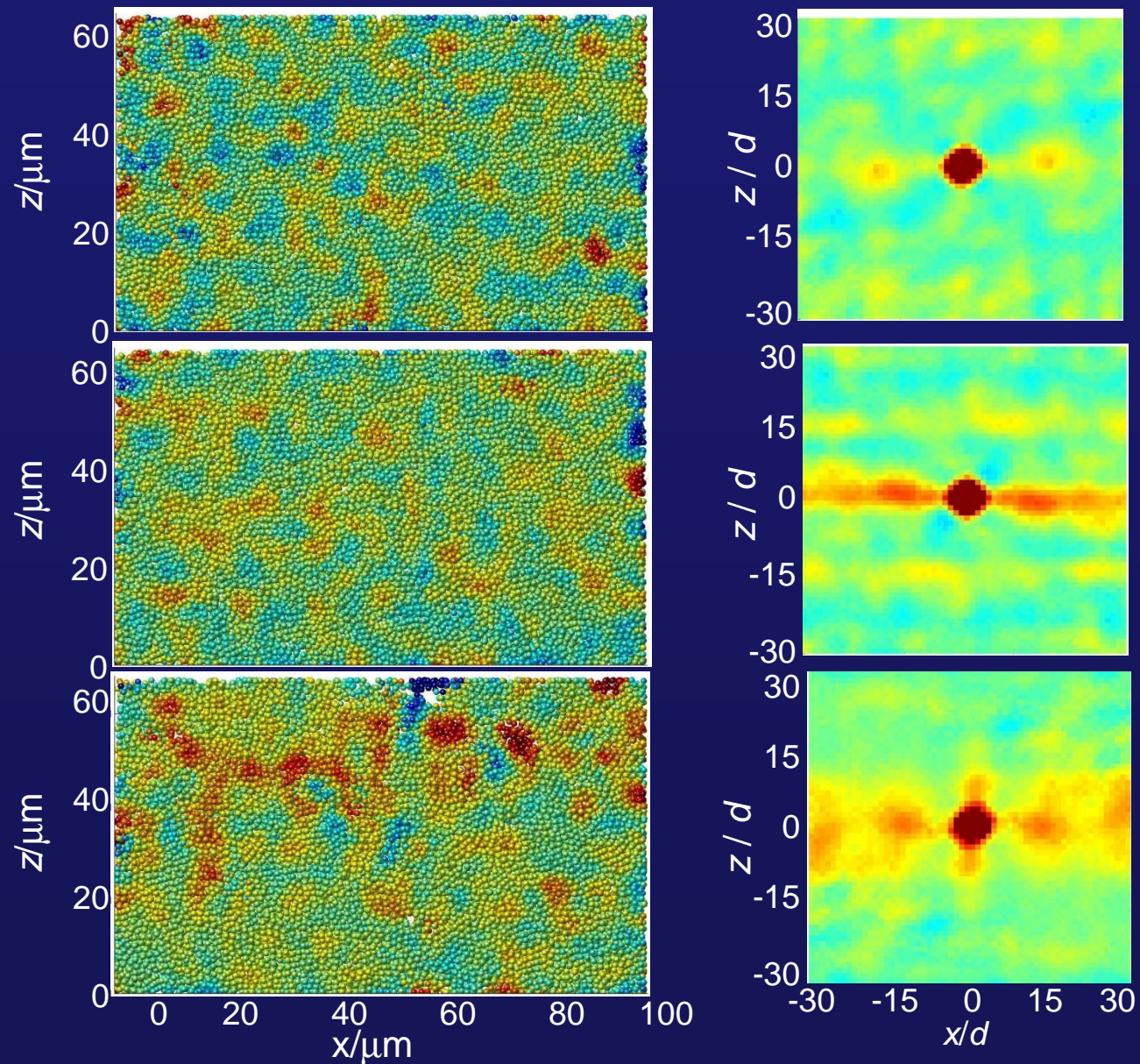


Shear



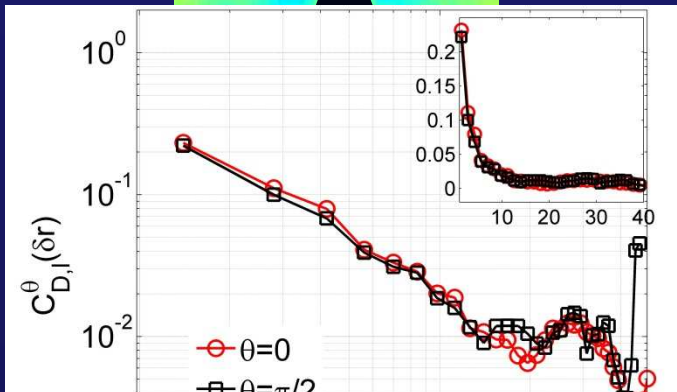
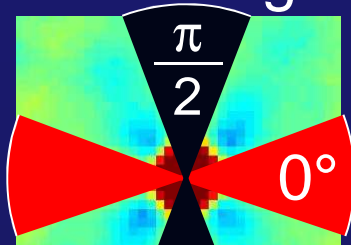
Very weak correlation between
dilation and shear, $C_r \sim 0.01!$

Increasing Strain rate

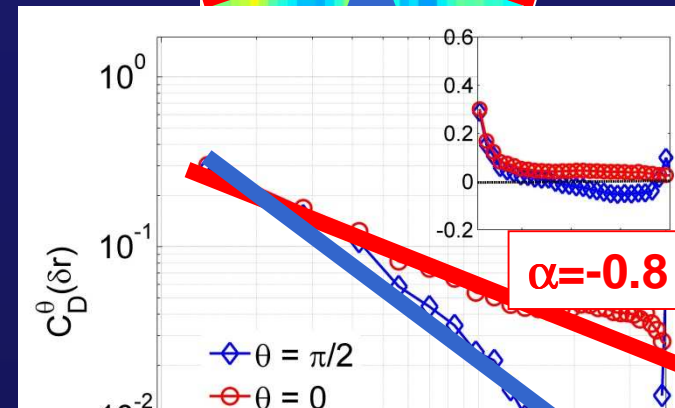
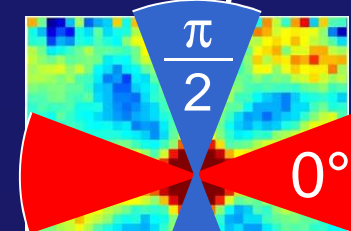


Anisotropy of Strain correlations

weakly driven:
Thermal regime

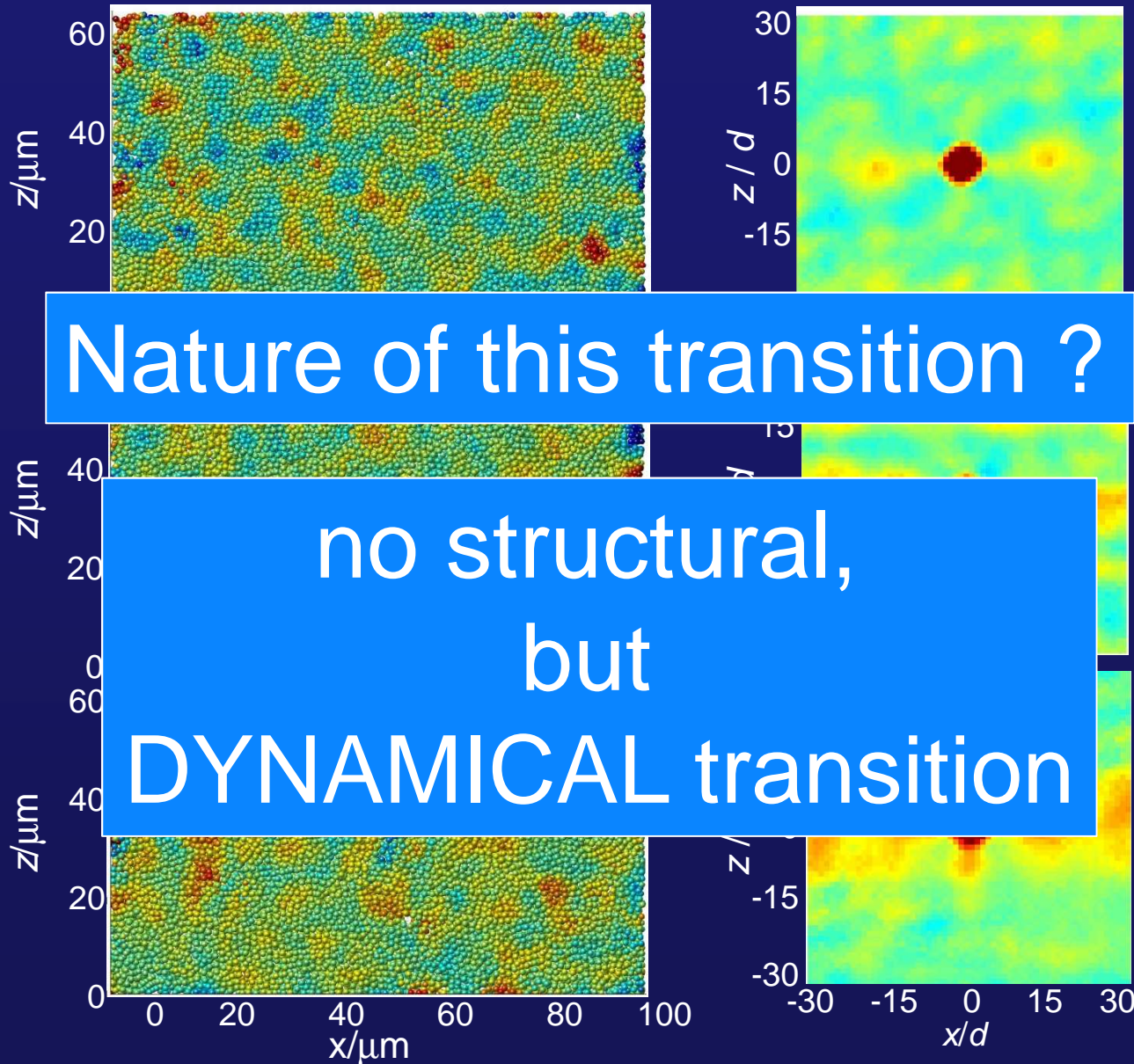


strongly driven:
Stress regime



New correlations with
anisotropic, stress-dependent scaling

Shear banding transition



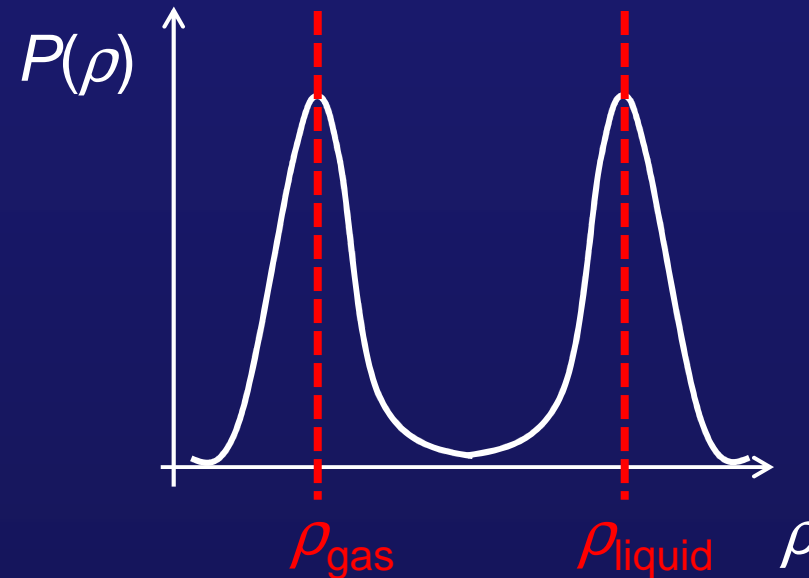
Nature of this transition ?

no structural,
but
DYNAMICAL transition

First order transition ?

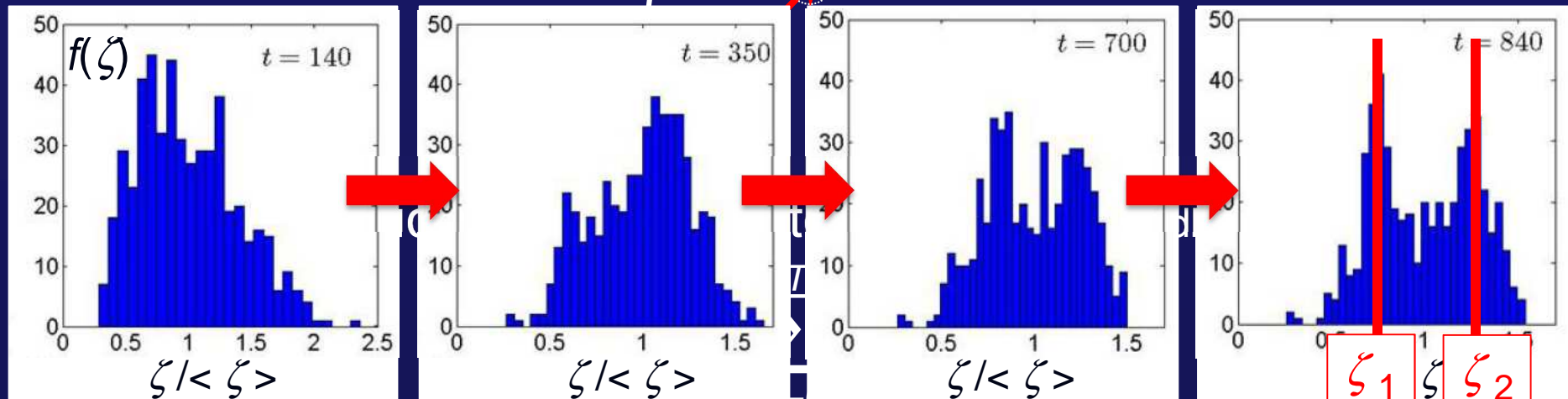
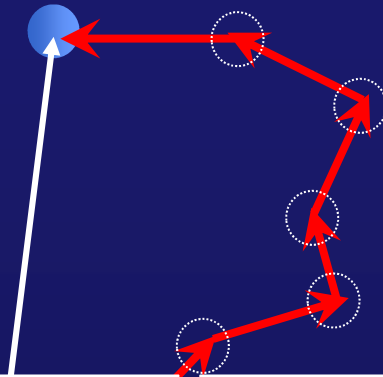
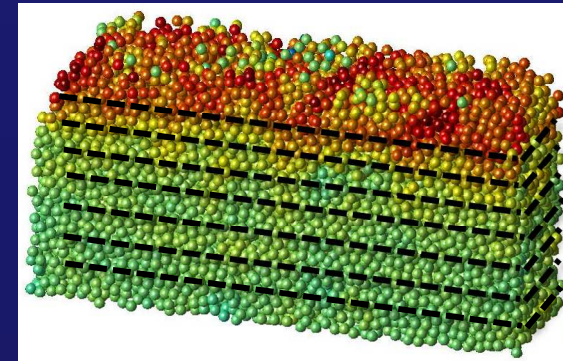
Gas – Liquid transition:

$\zeta \rightarrow$ Density ρ



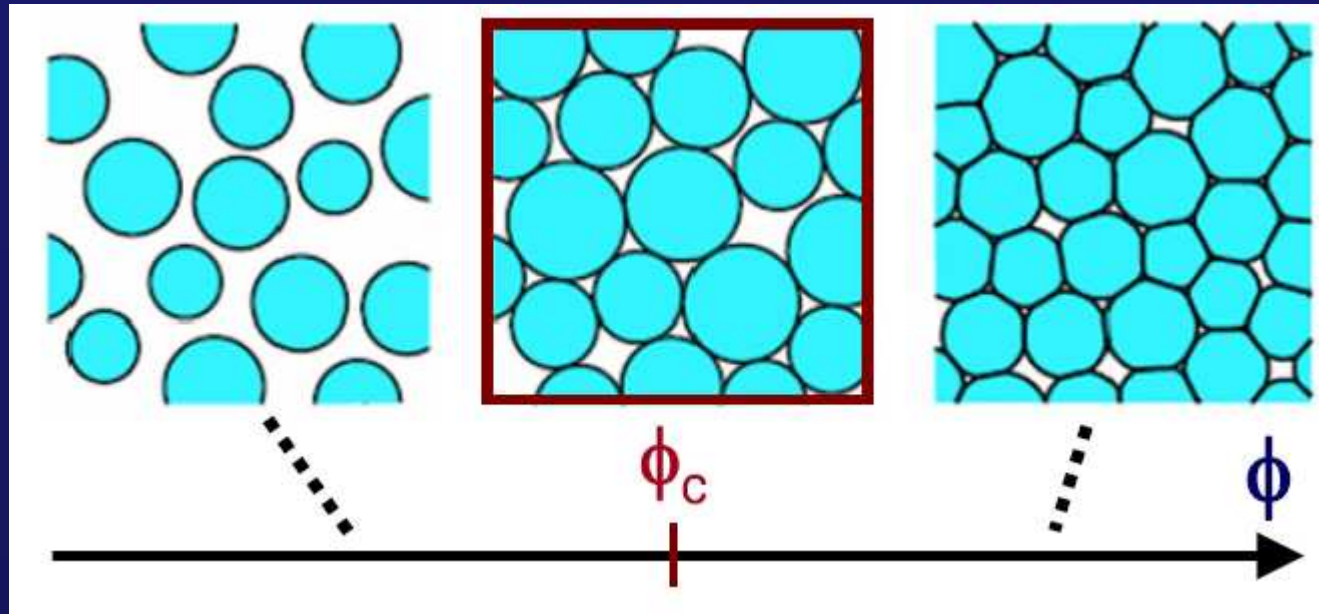
What is the right order parameter ?

First order transition ?



First order transition in 4D space-time

Soft Spheres: beyond the glass transition



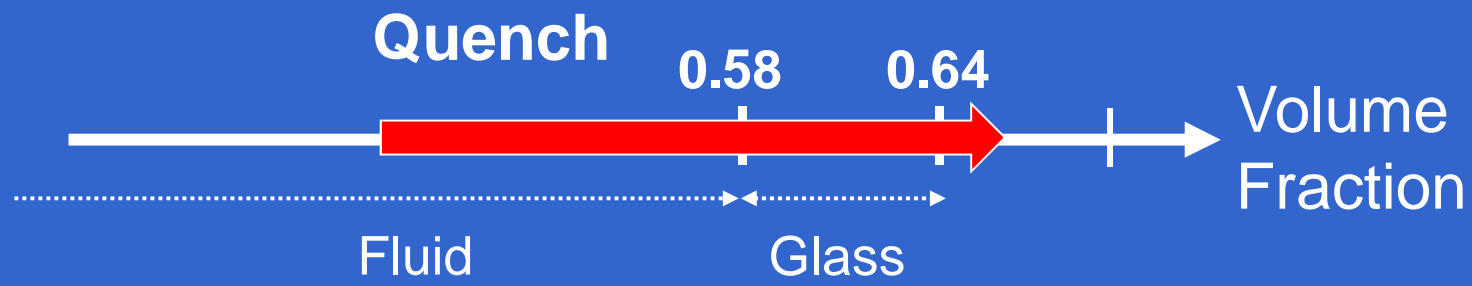
... compress beyond close packing

Soft Sphere Glasses

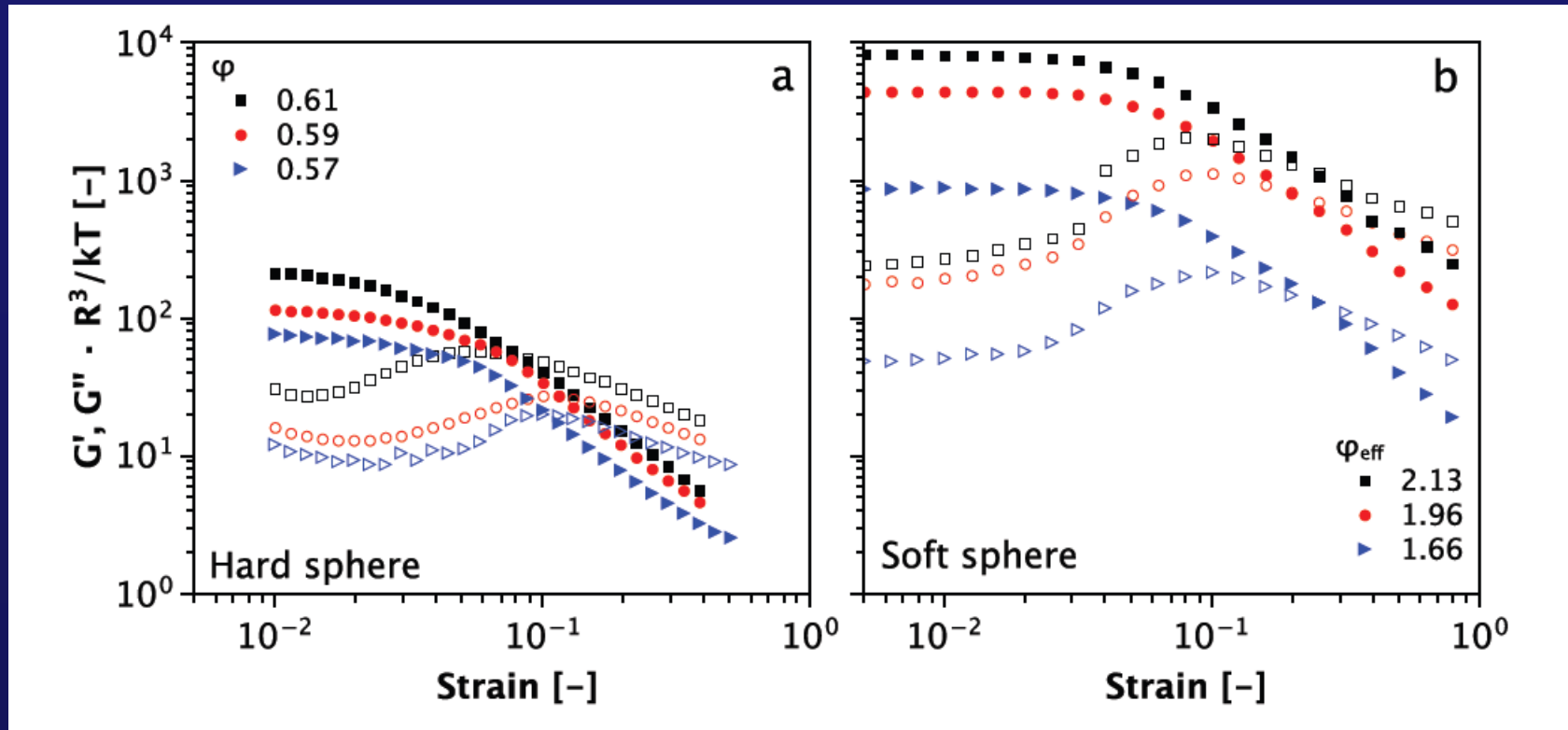
Temperature-sensitive colloids



Quench beyond glass transition

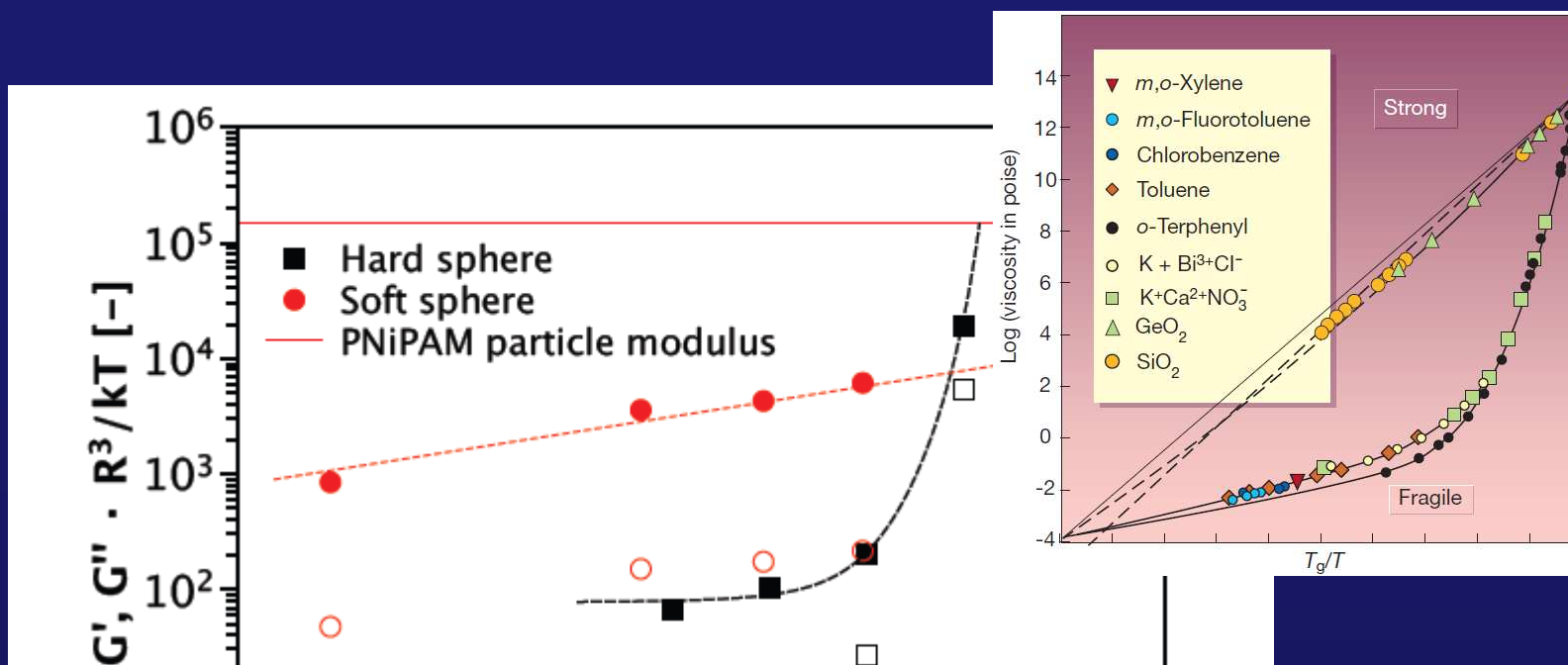


Rheology: Hard and Soft Sphere Glasses



Soft Spheres: High elastic component!

Rheology: Hard and Soft Sphere Glasses



Soft spheres \rightarrow Strong Glasses
Hard Spheres \rightarrow Fragile Glasses

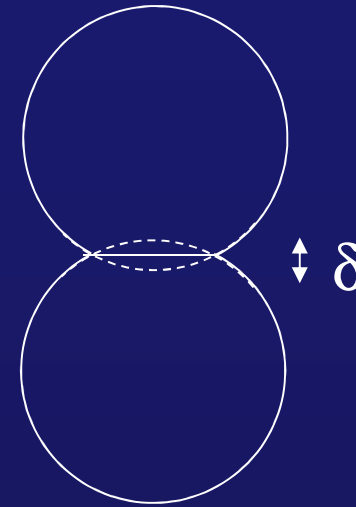
Mattsson, Weitz (*Nature* 2010)

Soft Spheres
Weaker volume fraction dependence

Soft Spheres : Hertzian Interaction

Hertzian Interaction

$$u = \frac{8}{15} \sqrt{\frac{R}{2}} E_p \delta^{2.5},$$



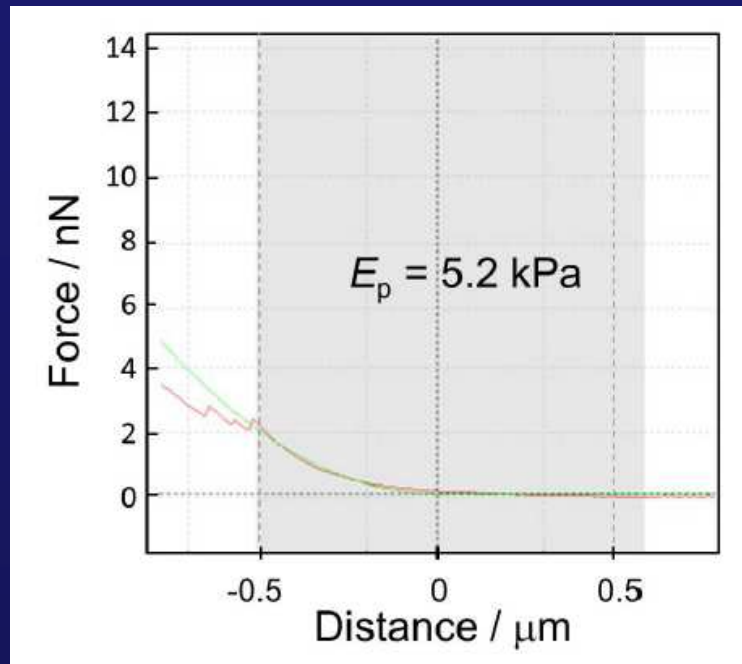
Suspension Modulus

$$G_{\infty} = \frac{2\pi}{15} n^2 \int_0^{2R} g(r) \frac{d}{dr} \left[r^4 \frac{du(r)}{dr} \right] dr,$$

Cloitre, Bonnecaze (*J. Rheol.* 2006)

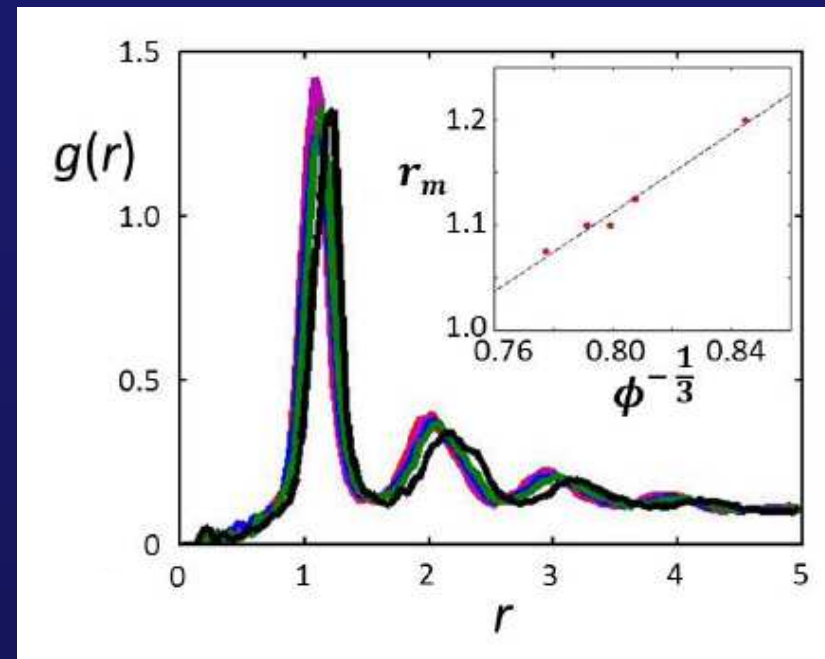
Soft Spheres : Hertzian Interaction

1. Particle Modulus



(Atomic Force Microscopy)

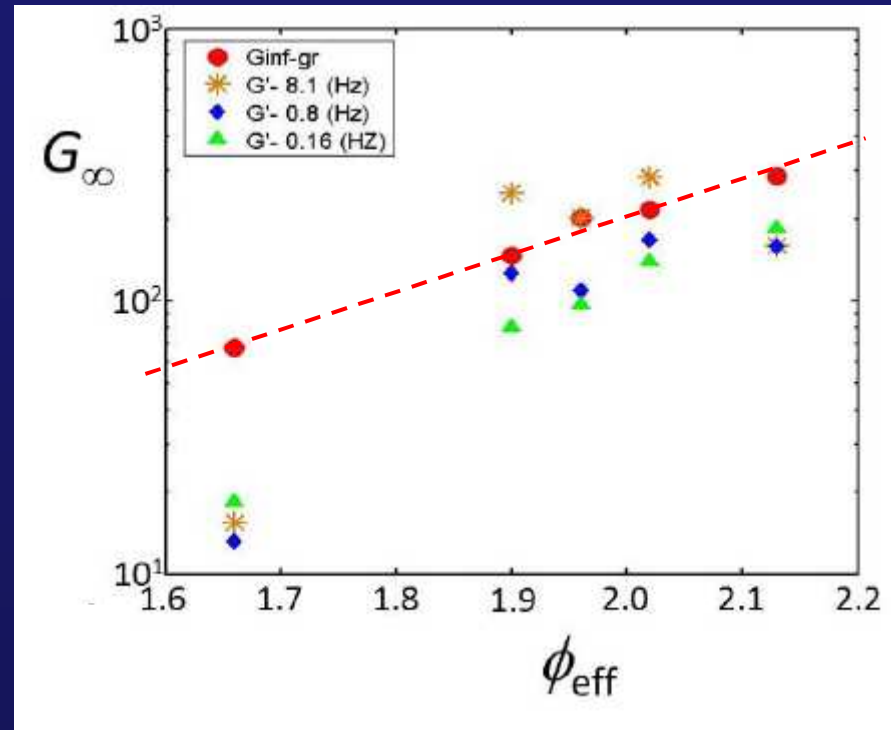
2. Pair Distribution Function



(Confocal Microscopy)

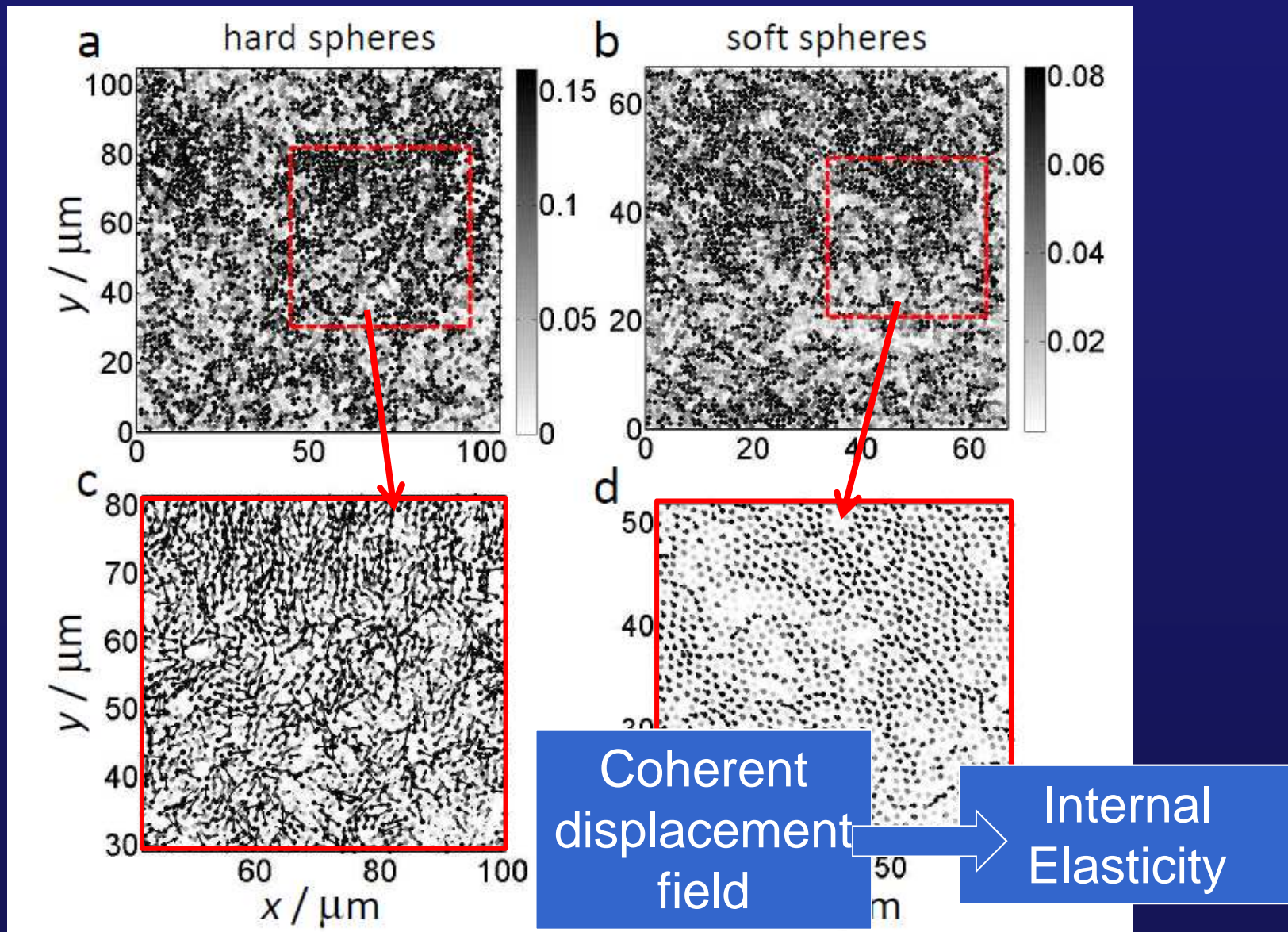
Soft Spheres : Hertzian Interaction

Shear Modulus: Model & Measurement



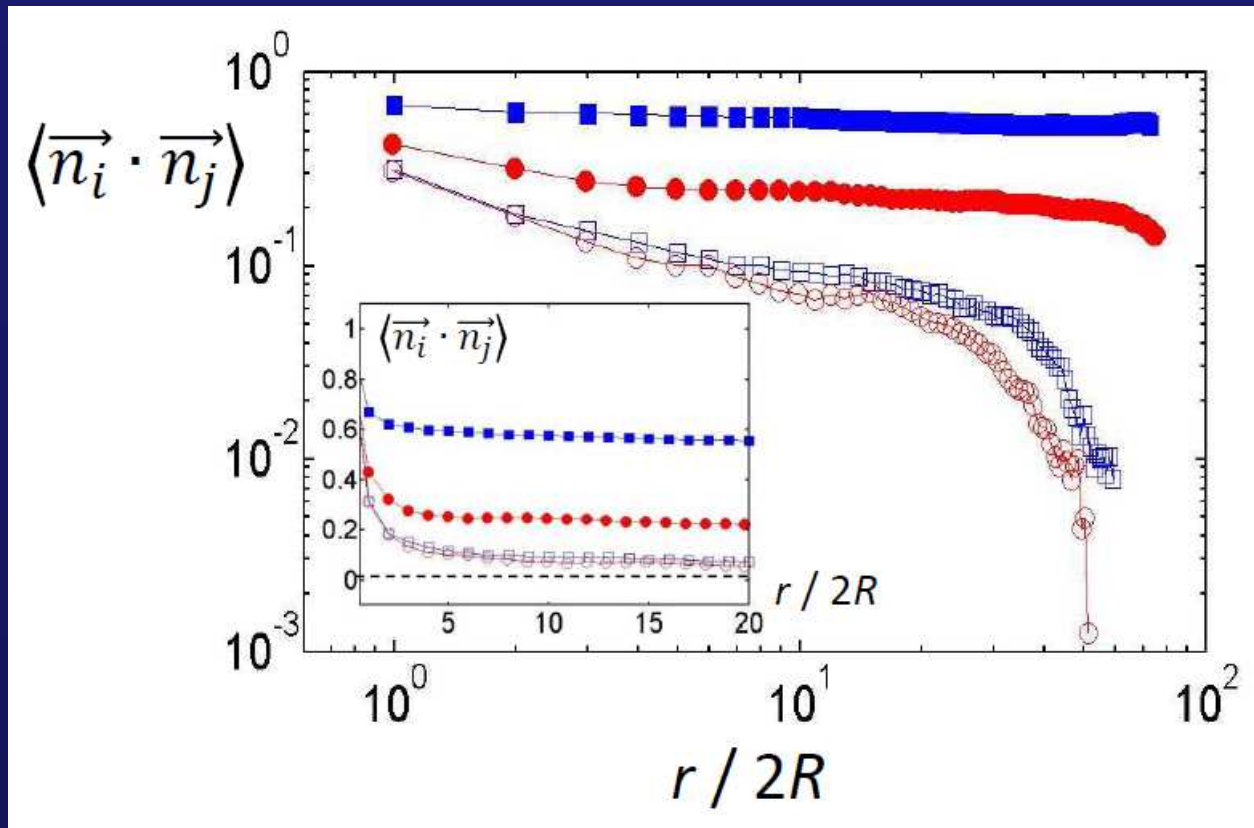
How does elasticity affect
microscopic relaxation?

Soft Sphere Glasses



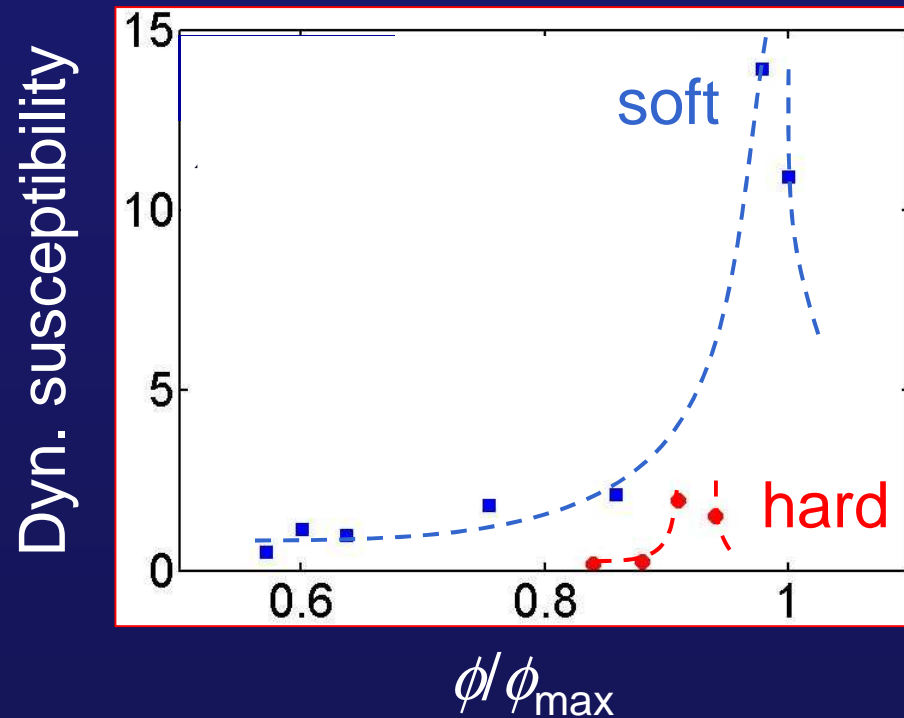
Soft Sphere Glasses

Correlations of Displacements



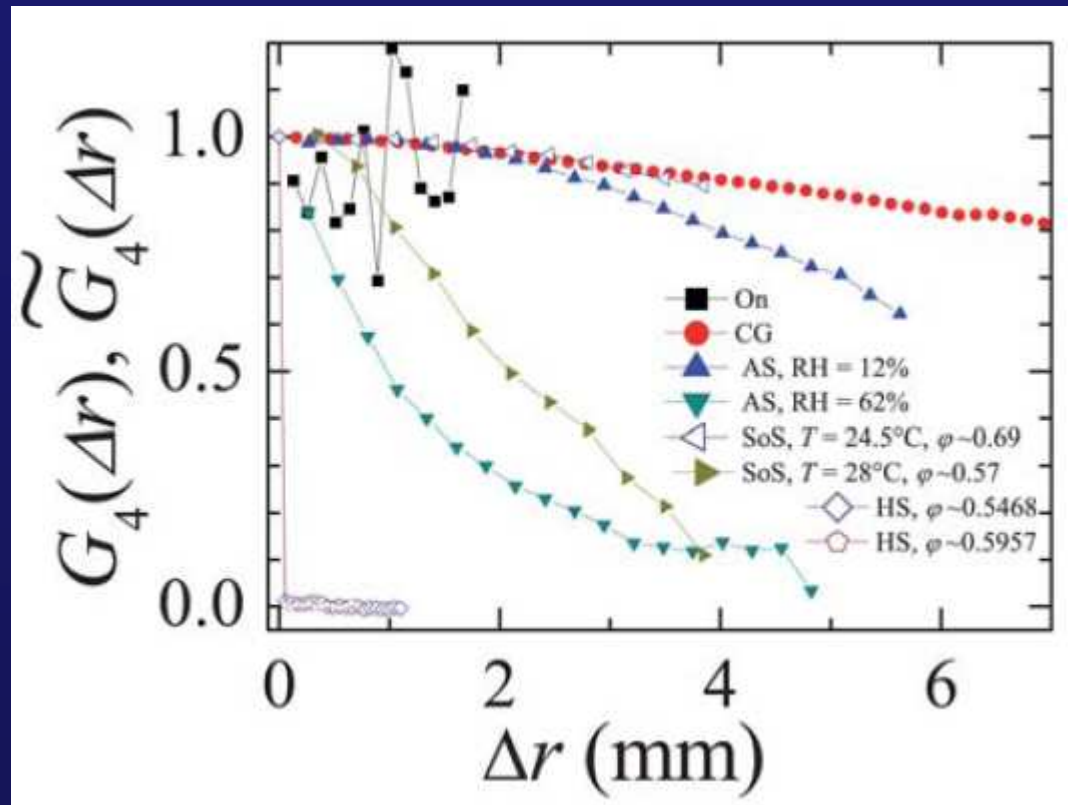
Soft Sphere Glasses

➔ Large Dynamic susceptibility!



Soft Sphere Glasses

Long-range correlations ...



... ubiquitous in Soft Matter!

Conclusions

- Colloidal Glasses
Insight into flow of amorphous materials
- Strain correlations :
central to material arrest, flow and failure
- **New anisotropic** correlations:
Stress-dependent anisotropic scaling → Strain localization
- → Dynamic first order transition in 4D space-time