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## MULTI-SCALE SIMULATION APPROACH FOR THE FLUIDISED BED SPRAY GRANULATION PROCESS

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### FLUIDIZED BED SPRAY GRANULATION motivation

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free flowing



dust-free



redispersible



compact

**product formulation**

**tailor-made properties**



instant milk



culinary powders

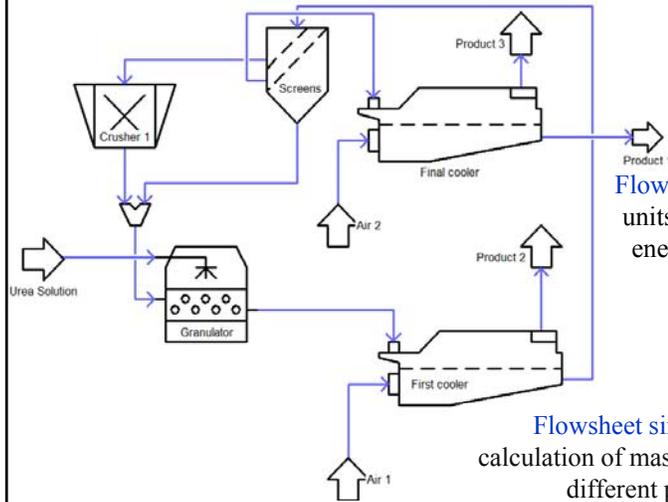


soluble coffee

## MULTISCALE SIMULATION APPROACH

### industrial production process

Most industrial processes consists of complex interconnection of different apparatuses and production steps

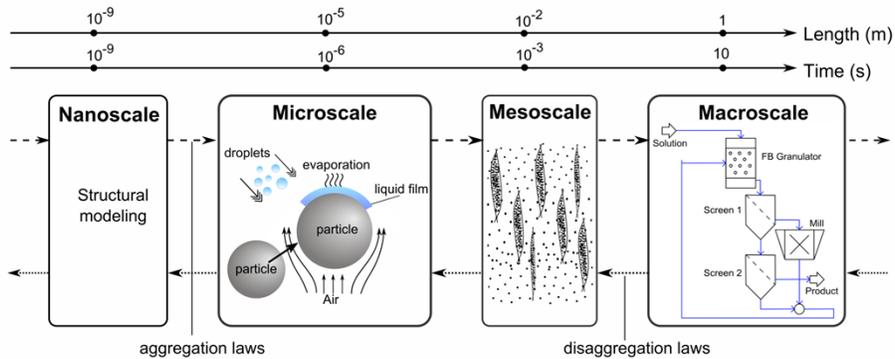


**Flowsheet:** Network of process units, which are connected by energy and material streams

**Flowsheet simulation:** Numerical calculation of mass and energy balances for different process structures

## MULTISCALE SIMULATION APPROACH

### process treatment on different scales

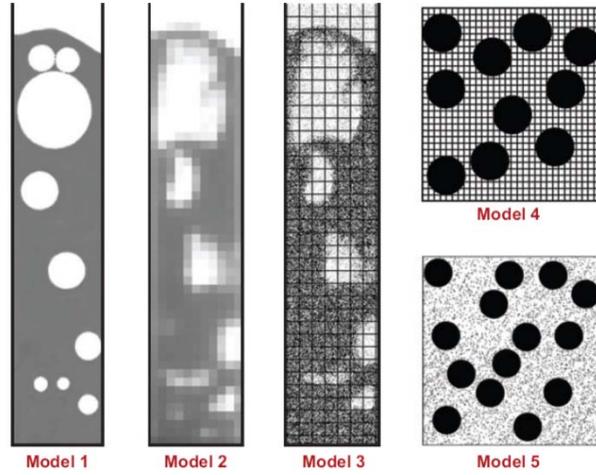


On the macroscale **empirical** or **semi-empirical** models are used, material properties are **poorly** considered

Description of the process on lower scales leads to exponential **increase** of computational volume

J. Werther, S. Heinrich, M. Dosta, E.-U. Hartge, *Particuology*, Vol. 9, 320-329<sup>4</sup>, 2011

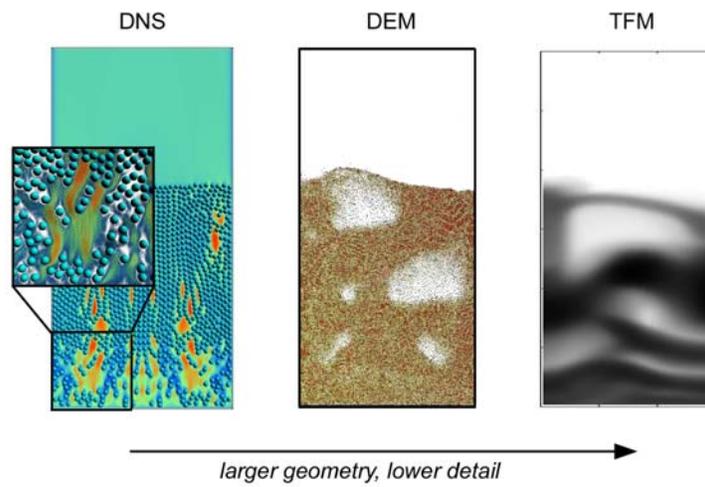
MULTI-SCALE MODELLING



Van der Hoef et al., Annu. Rev. Fluid M., 2008

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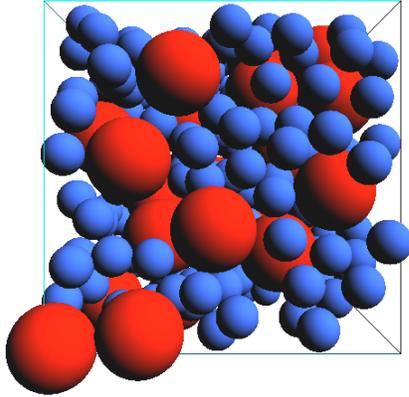
MULTI-SCALE MODELLING



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RESULTS OF LATTICE BOLTZMANN MODEL  
static array of bi-disperse particles at low  $Re_p$

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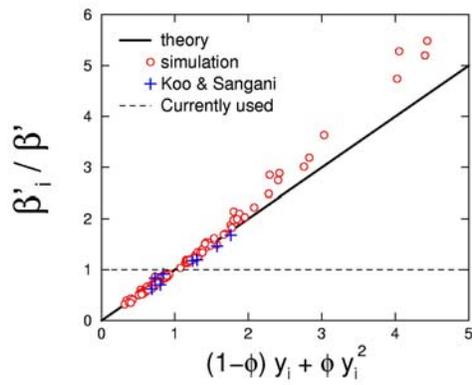


example of initial particle configuration for a bi-disperse system generated with a Monte Carlo procedure

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RESULTS OF LATTICE BOLTZMANN MODEL  
static array of bi-disperse particles at low  $Re_p$

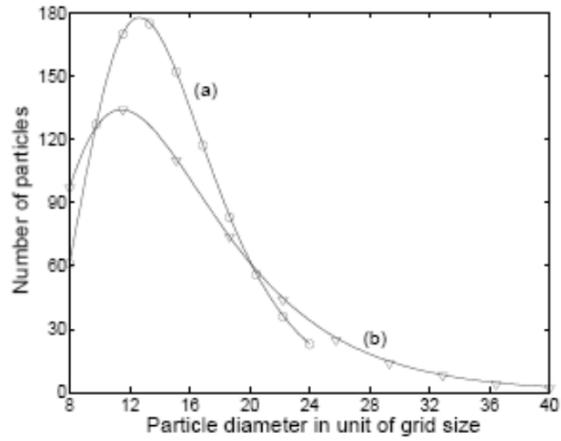
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$$\beta'_i = \left[ (1-\phi) y_i + \phi y_i^2 \right] \beta' \quad y_i = \frac{d_i}{\langle d \rangle}$$

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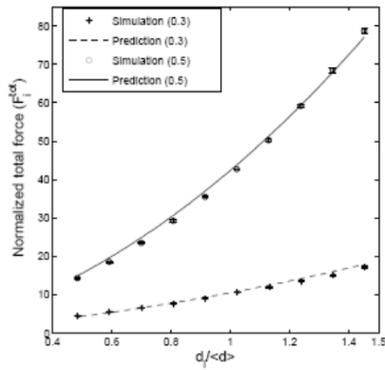
RESULTS OF LATTICE BOLTZMANN MODEL  
static array of particles with log-normal PSD



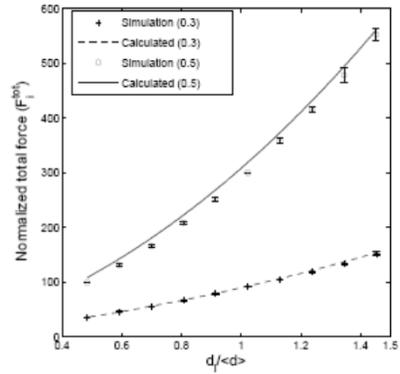
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RESULTS OF LATTICE BOLTZMANN MODEL  
static array of particles with log-normal PSD

Re=0.1



Re=500



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RESULTS OF LATTICE BOLTZMANN MODEL  
 final drag closure for mono-disperse and poly-disperse particles

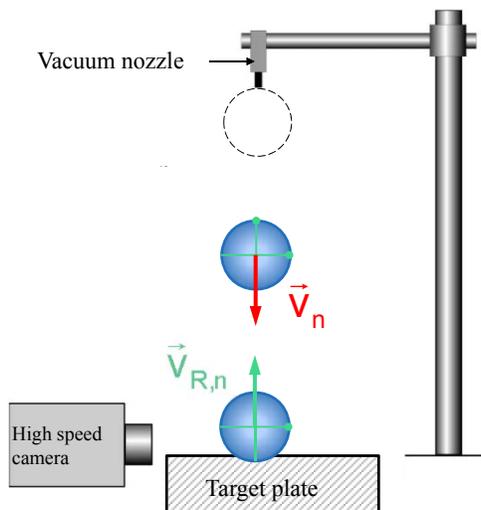
$$\frac{\bar{\mathbf{F}}_{g \rightarrow i}}{3\pi\mu d_i \varepsilon_g (\mathbf{u}_g - \mathbf{v}_i)} = \left[ \varepsilon_g \frac{d_i}{\langle d \rangle} + \varepsilon_s \frac{d_i^2}{\langle d \rangle^2} + 0.064 \varepsilon_g \frac{d_i^3}{\langle d \rangle^3} \right] \times \left[ \frac{10 \varepsilon_s}{\varepsilon_g^3} + \varepsilon_g + 1.5 \varepsilon_g \varepsilon_s^{1/2} + \frac{0.413 \text{Re}}{24 \varepsilon_g^3} \left( \frac{\varepsilon_g^{-1} + 3 \varepsilon_s \varepsilon_g + 8.4 \text{Re}^{-0.343}}{1 + 10^{3 \varepsilon_s} \text{Re}^{-(1+4 \varepsilon_s)/2}} \right) \right]$$

good fit (deviation less than 8%) of basic LB simulation data  
 generated over wide range of  $\varepsilon_g$  and Re

strictly valid for homogeneous arrays of particles

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MECHANICAL PARTICLE PROPERTIES  
 measurement of restitution coefficient



$$e_n = \left| \frac{\vec{v}_{R,n}}{\vec{v}_n} \right|$$

$e_n$  normal restitution coefficient  
 $v_n$  normal impact velocity  
 $v_{R,n}$  normal rebound velocity

van Buijtenen, M.S., Deen, N.G., Heinrich, S., Antonyuk, S. and J.A.M. Kuipers: A discrete element study of wet particle-particle interaction during granulation in a spout fluidized bed, *Canadian Journal of Chemical Engineering* (2009), Vol. 9999, 1-10.<sup>12</sup>

## MECHANICAL PARTICLE PROPERTIES

### measurement of restitution coefficient

Restitution coefficient:

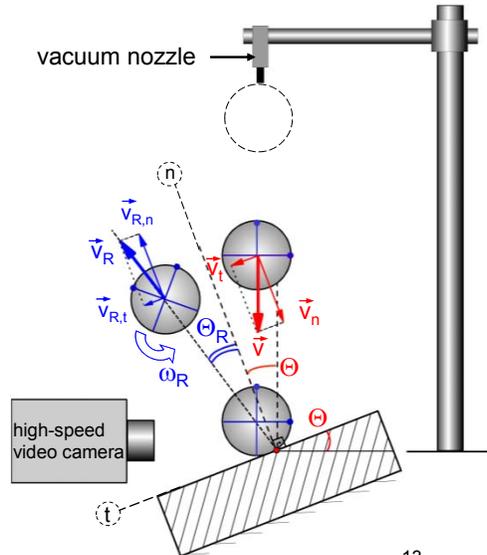
$$e = \sqrt{\frac{E_{kin,R}}{E_{kin}}} = \sqrt{1 - \frac{E_{diss}}{E_{kin}}} = \frac{|\vec{v}_R|}{|\vec{v}|}$$

$v_R/v$  relative rebound/impact velocity

$n/t$  normal and tangential component

$$e_n = \frac{|\vec{v}_{R,n}|}{|\vec{v}_n|} \quad \text{normal}$$

$$e_t = \frac{|\vec{v}_{R,t}|}{|\vec{v}_t|} \quad \text{tangential}$$

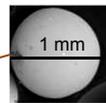
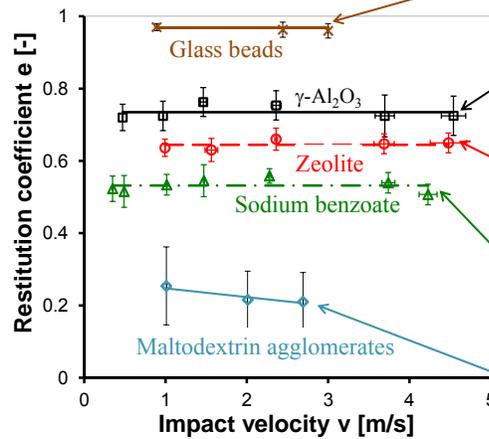


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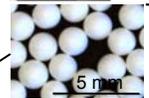
## MECHANICAL PARTICLE PROPERTIES

### measurement of "dry" restitution coefficient

Normal impact on a dry glass plate



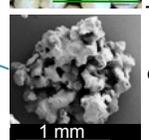
1 mm dominantly elastic



5 mm elastic-plastic



5 mm elastic-plastic

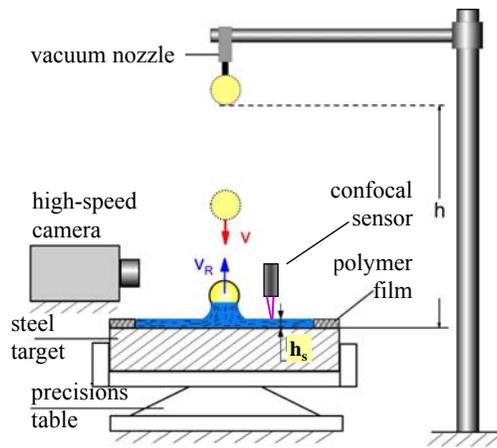


1 mm dominantly plastic

Antonyuk, S., Heinrich, S., Tomas, J., Deen, N.G., van Buijtenen, M.S. and J.A.M. Kuipers: Energy absorption during compression and impact of dry elastic-plastic spherical granules, Granular Matter (2010) 1, 12.

## MECHANICAL PARTICLE PROPERTIES

measurement of “wet” restitution coefficient



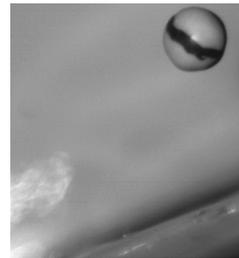
$$e = \sqrt{\frac{E_{kin,R}}{E_{kin}}} = \frac{v_R}{v}$$

$v_R/v$  relative rebound/impact velocity

$E_{kin,R}$  elastic rebound energy

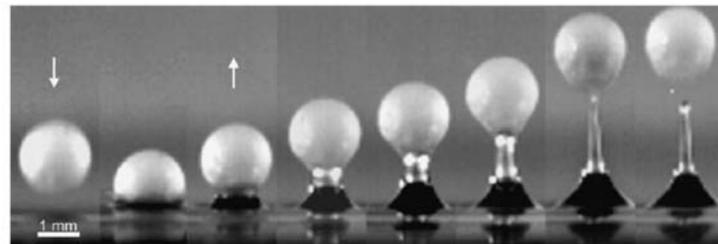
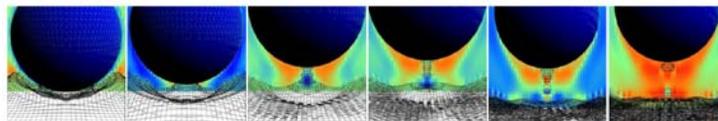
$E_{kin}$  impact energy

$E_{diss}$  irreversible absorbed energy



Objectives of the study:  $e = f(\text{impact velocity, liquid film thickness and viscosity})$

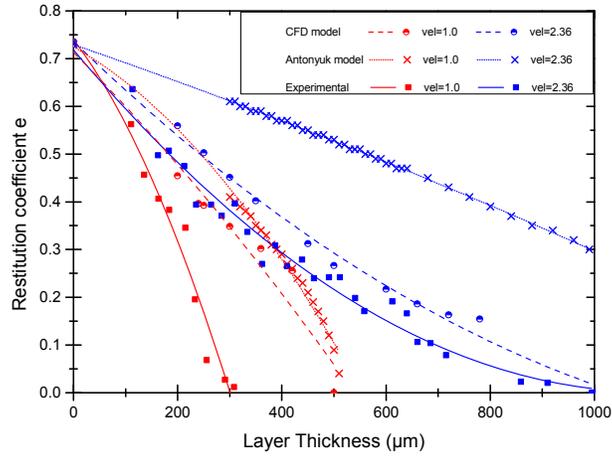
## PARTICLE COLLISION IN WET SYSTEMS



(above) Formation, thinning & eventual breakup of the liquid bridge (simulation results)

(below) Images from high-speed recording of  $\alpha\text{-Al}_2\text{O}_3$  granule impacting with velocity of 2.36 m/s on wall with a water layer (thickness 0.4 mm) (Antonyuk et al. (2009)).

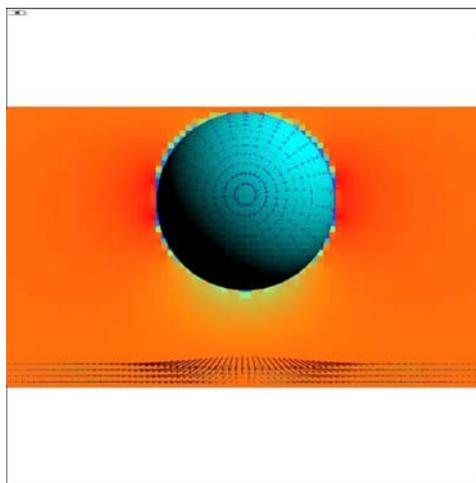
## PARTICLE COLLISION IN WET SYSTEMS



Influence of impact velocity on restitution coefficient of the  $\text{Al}_2\text{O}_3$  granules impacting on water layers with varying thickness.

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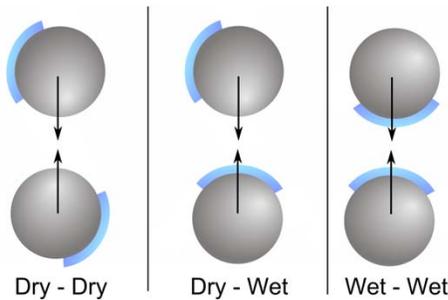
## PARTICLE COLLISION IN WET SYSTEMS



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PARTICLE COLLISION IN WET SYSTEMS  
collision types for different moisture contents

- During fluidized bed granulation the particles are covered by a liquid film
- Different types of collisions can occur:



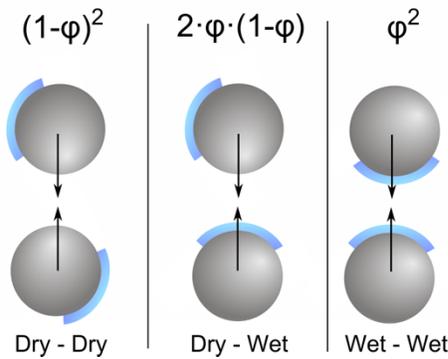
$$e = \sqrt{\frac{E_{\text{kin,R}}}{E_{\text{kin}}}} = \frac{v_R}{v}$$

How can the influence of the liquid film be predicted?

PARTICLE COLLISION IN WET SYSTEMS  
collision types for different moisture contents

- For the description of the liquid film, the wetted surface fraction  $\phi$  is used
- $\phi$  obtained from the calculations of the model on the macroscale

Collision probabilities



$$\phi = \frac{A_{\text{wet}}}{A_{\text{tot}}}$$

$A_{\text{wet}}$  wetted surface  
 $A_{\text{tot}}$  total particle surface

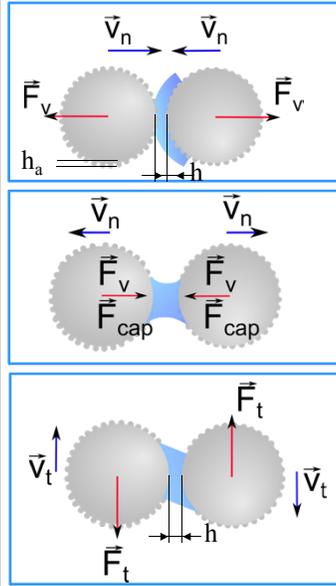
$$e = \sqrt{\frac{E_{\text{kin,R}}}{E_{\text{kin}}}} = \frac{v_R}{v}$$

$$e = e_1 \cdot (1 - \phi)^2 + e_2 \cdot 2 \cdot \phi \cdot (1 - \phi) + e_3 \cdot \phi^2$$

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PARTICLE COLLISION IN WET SYSTEMS

contact model for wet collisions



Viscous forces

Normal impact<sup>1</sup>

$$F_{v,n} = \frac{6 \pi \eta R^{*2} v_{n,rel}}{h}$$

Tangential impact<sup>2</sup>

$$F_{v,t} = 2 \pi \eta R^* v_{t,rel} \ln \left( 1 + \frac{R^*}{2h} \right)$$

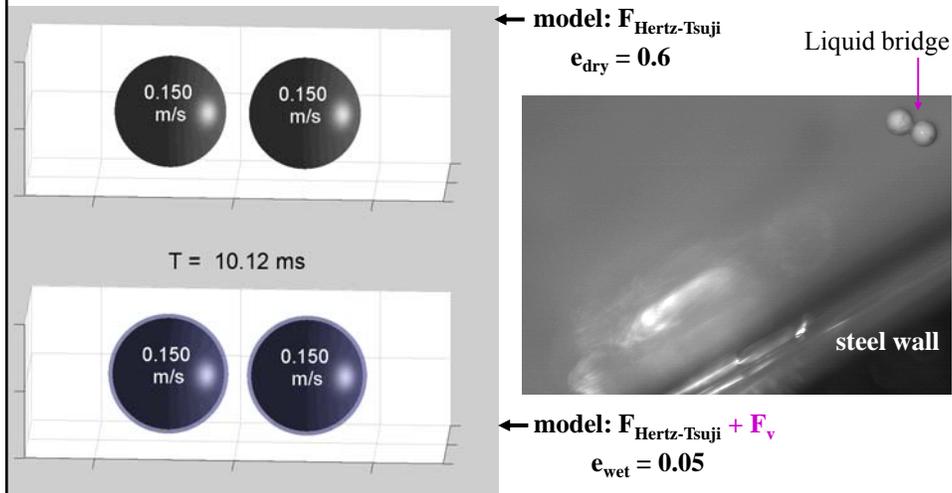
$$h \geq 2 h_a$$

- $v_{n,rel}$  normal relative velocity
- $v_{t,rel}$  tangential relative velocity
- $h$  minimum separation distance
- $h_a$  roughness
- $\eta$  viscosity
- $R^*$  average curvature radius in contact
- $F_{cap}$  capillary force

<sup>1</sup>Adams, M.J., Edmondson, B. (1987). Tribology in particulate technology.  
<sup>2</sup>Popov, V. (2009) Kontaktmechanik und Reibung, Springer. 21

PARTICLE COLLISION IN WET SYSTEMS

application of viscous contact model

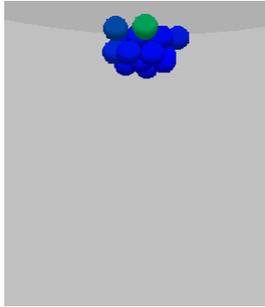


Particles:  $R = 0.4 \text{ mm}$ ,  $\rho = 190 \text{ kg/m}^3$ ,  $e_{dry} = 0.6$ ,  $G = 6.3 \text{ MPa}$

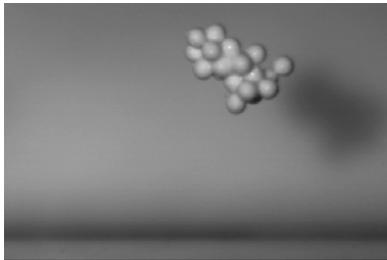
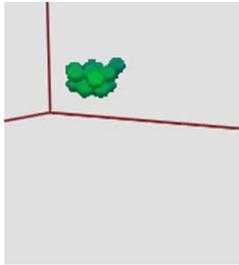
Liquid layer:  $\eta = 1 \text{ mPa}\cdot\text{s}$ ,  $h = 60 \text{ }\mu\text{m}$ ,  $h_a = 2.5 \text{ }\mu\text{m}$

## PARTICLE COLLISION IN WET SYSTEMS

application of viscous contact model



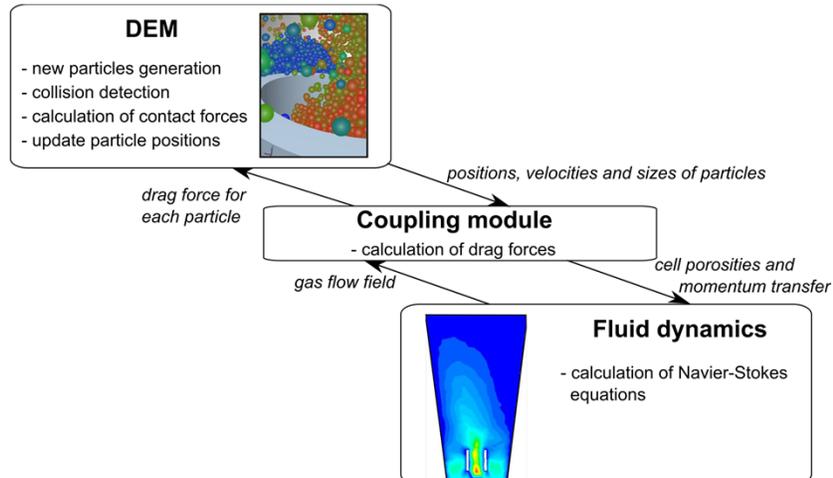
$d_p = 0.8 \text{ mm}$   
 $v_{imp} = 1.2 \text{ m/s}$   
 liquid layer:  
 $\eta = 8 \text{ mPa}\cdot\text{s}, h_m \approx 60 \text{ }\mu\text{m}$



$d_p = 0.8 \text{ mm}$   
 $v_{imp} = 1.2 \text{ m/s}$   
 liquid layer:  
 $\eta = 4 \text{ mPa}\cdot\text{s}, h_m \approx 230 \text{ }\mu\text{m}$

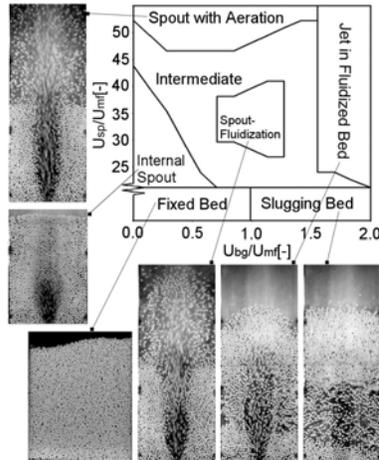
## COUPLING BETWEEN DEM AND CFD

- For the description of particle motion in the fluid field the **Computational Fluid Dynamics (CFD)** model is coupled



RESULTS DISCRETE PARTICLE MODEL

spouted bed



“CAPABILITIES” OF DPM  
(COLLISION PARAMETERS!!!)

(Link et al., CES, 2005)

REGIME PREDICTION

GAS BUBBLES BEHAVIOUR

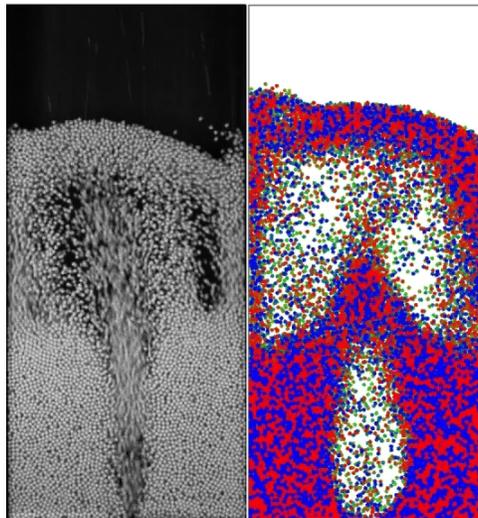
PRESSURE FLUCTUATIONS

SOLIDS MOTION

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RESULTS DISCRETE PARTICLE MODEL

spouted bed (dry system)



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## DISCRETE PARTICLE MODEL

### nozzle region

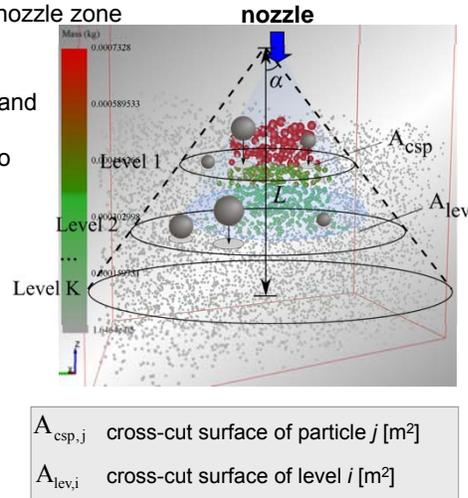
- For the description of particle wetting the nozzle zone model has been developed
- The nozzle zone is described by the suspension mass stream, spraying angle and the height of cone area
- The suspension mass flow which comes to the particle  $j$  in the level  $i$  is defined as:

$$\dot{M}_{susp,j} = \dot{M}_{susp}^i \cdot \frac{A_{csp,j}}{A_{lev,i}}$$

- Mass stream on the level  $i+1$ :

$$\dot{M}_{susp}^{i+1} = \dot{M}_{susp}^i \cdot \left( 1 - \frac{\sum A_{csp,j}}{A_{lev,i}} \right)$$

- In apparatus the different nozzles can be defined simultaneously

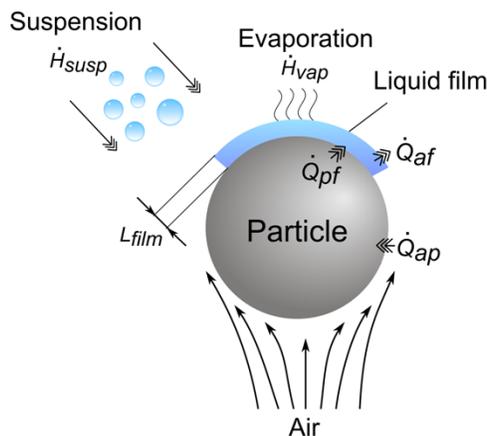


L. Fries, M. Dosta, S. Antonyuk, S. Heinrich, S. Palzer, *Chemical Engineering Technology*, 34, 2011

## DISCRETE PARTICLE MODEL

### heat and mass transfer

- For the calculation of liquid film drying the equations of energy and mass balance are used
- The heat and mass transfer coefficients  $\alpha$  and  $\beta$  are calculated for each particle



$$\dot{Q}_{af} = \alpha_{af} \cdot A_{film} \cdot (\vartheta_{air} - \vartheta_{film})$$

$$\dot{Q}_{ap} = \alpha_{ap} \cdot (A_p - A_{film}) \cdot (\vartheta_{air} - \vartheta_p)$$

$$\dot{Q}_{pf} = \alpha_{pf} \cdot A_{film} \cdot (\vartheta_p - \vartheta_{film})$$

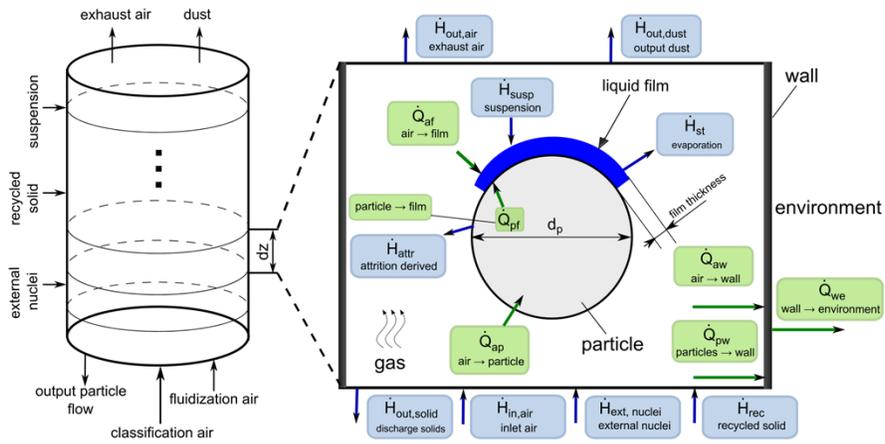
$$\frac{dH_{film}}{dt} = \dot{H}_{susp} + \dot{Q}_{pf} - \dot{H}_{vap} + \dot{Q}_{af}$$

$A_{film}$	Surface of liquid film [m <sup>2</sup> ]
$A_p$	Particle surface [m <sup>2</sup> ]
$\vartheta_p$	Particle temperature [°C]
$\vartheta_{film}$	Temperature of liquid film [°C]

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## DISCRETE PARTICLE MODEL

### heat and mass transfer and particle growth



- growth rate for each particle:

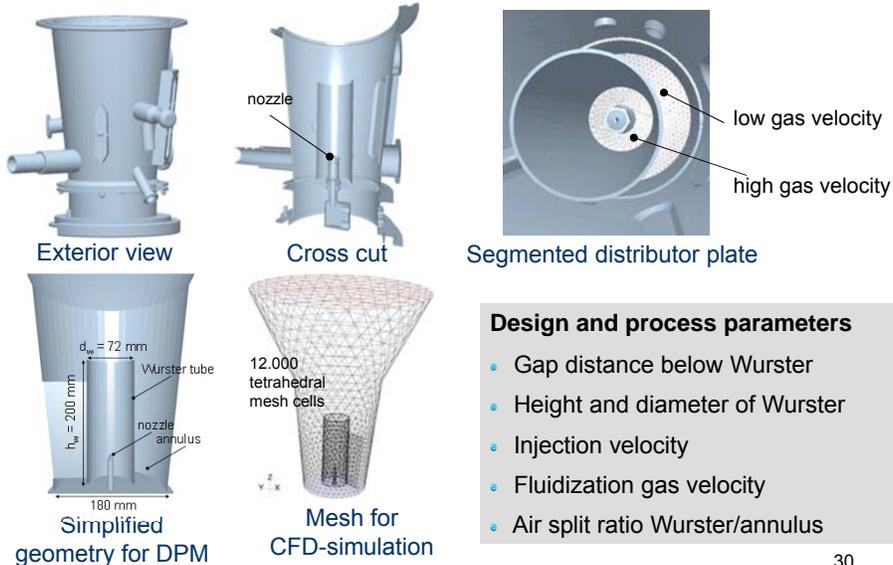
$$\frac{dR_p}{dt} = \frac{\dot{M}_{vap} \cdot (1 - x_w)}{4 \cdot \pi \cdot R_p^2 \cdot x_w \cdot \rho_s}$$

$R_p$	Particle radius [m]
$\dot{M}_{vap}$	Vapor mass stream [kg/s]
$\rho_s$	Solid density [kg/m <sup>3</sup> ]

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## RESULTS DISCRETE PARTICLE MODEL / CFD

### real granulators – Wurster coater

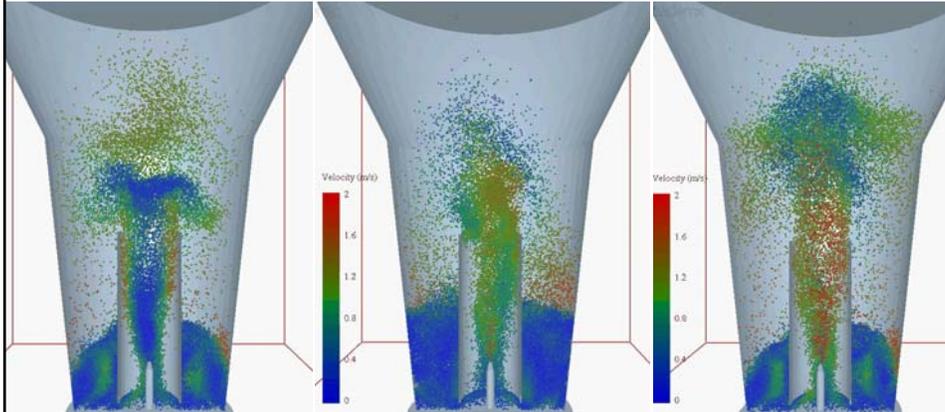


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RESULTS DISCRETE PARTICLE MODEL / CFD

real granulators – Wurster coater

150.000 particles,  $d_p = 2 \text{ mm}$ ,  $\rho_p = 1500 \text{ kg/m}^3$ , total mass = 0.94 kg,  $e = 0.8$ , simulation time  $t = 2.5 \text{ s}$ , fluidization velocity: Wurster:  $u_w = 8 \text{ m/s} = 10.1 \cdot u_{mf}$ , annulus:  $u_{ann} = 3 \text{ m/s} = 3.8 \cdot u_{mf}$



$v_{\text{nozzle}} = 20 \text{ m/s}$

$v_{\text{nozzle}} = 100 \text{ m/s}$

$v_{\text{nozzle}} = 160 \text{ m/s}$

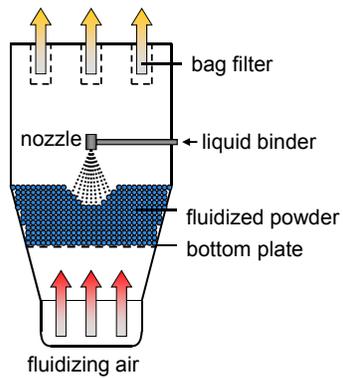
- High spout velocity provides stable circulation regime
- Backmixing is prevented

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RESULTS DISCRETE PARTICLE MODEL / CFD

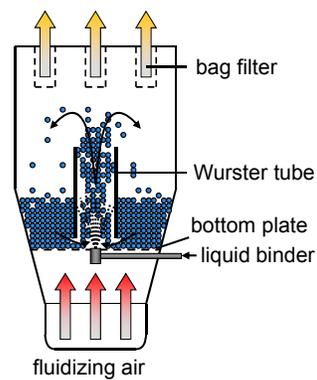
comparison of granulator configurations

Top spray



**Application:**  
Granulation and agglomeration  
of food and fertilizers.

Wurster-coater

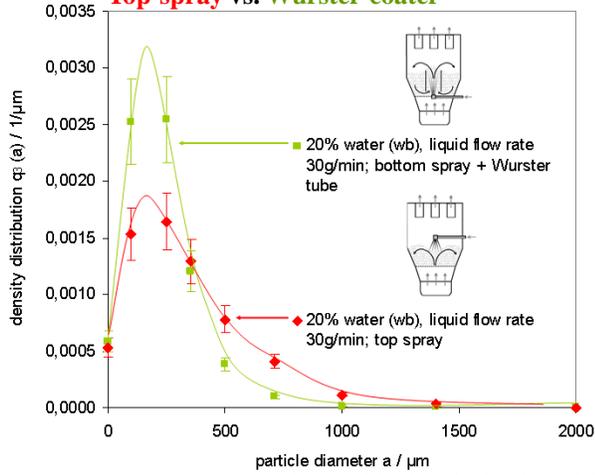


**Application:**  
tablet coating,  
encapsulation of flavors.

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RESULTS DISCRETE PARTICLE MODEL / CFD  
 comparison of granulator configurations

**Top-spray vs. Wurster-coater**



**Process conditions**

Glatt GCPG 3.1  
 Dextrose syrup (DE21)  
 Fluidization air: 250 m<sup>3</sup>/h

Injection: water,  
 20% of bed mass  
 at constant spray rate

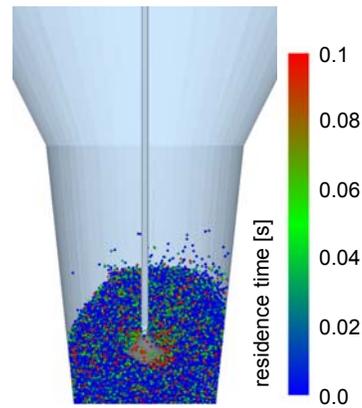
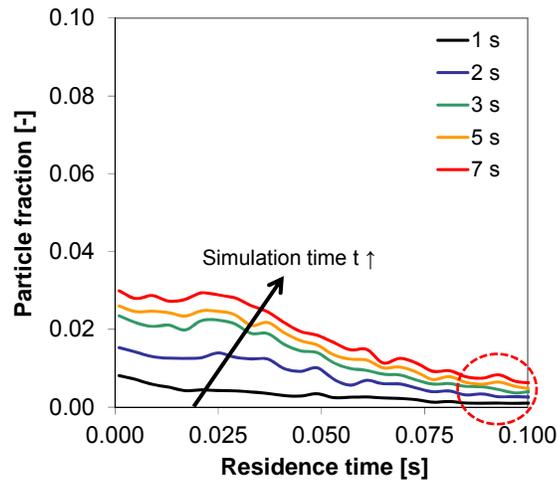
- Top-spray-configuration produces wide size distribution of the product
- Circulating regime allows more homogeneous wetting at equal process conditions

L. Fries, S. Antonyuk, S. Heinrich, S. Palzer, Chemical Engineering Science, 2011 33

RESULTS DISCRETE PARTICLE MODEL / CFD  
 comparison of granulator configurations

**Top spray granulator**

Broad residence time distribution



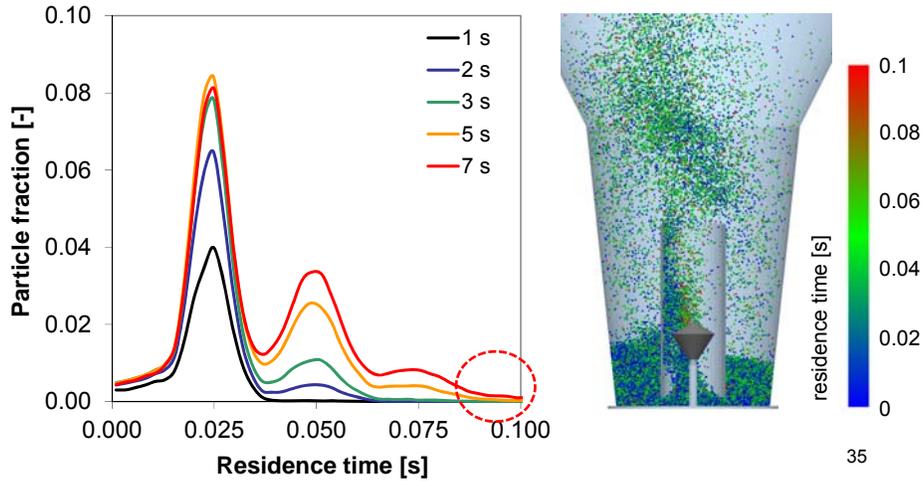
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RESULTS DISCRETE PARTICLE MODEL / CFD  
 comparison of granulator configurations

**Wurster-coater**

Cyclic wetting

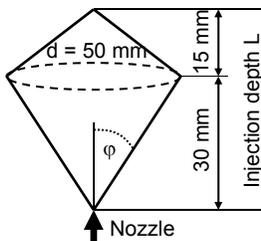
Defined residence time per cycle



RESULTS DISCRETE PARTICLE MODEL / CFD  
 particle collision dynamics

**Collisions between surface-wet particles**

Parameter	Wurster-coater	Top Spray
Particle fraction inside spray zone	0.53 %	0.36 %
Average angular velocity inside spray zone	43 rad/s	54 rad/s
Average collision frequency (inside spray zone)	88 s <sup>-1</sup>	864 s <sup>-1</sup>
Average relative collision velocity inside spray zone	0.39 m/s	0.15 m/s

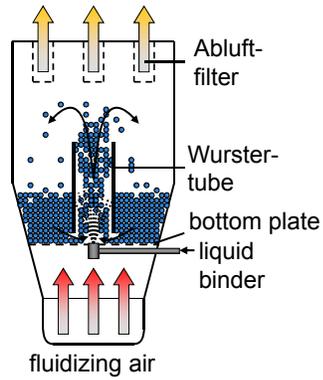


**Wurster-coater:**

- Lower collision frequency
  - Higher kinetic energy
- Reduced agglomeration probability

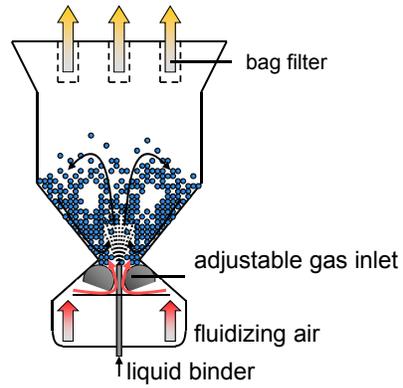
RESULTS DISCRETE PARTICLE MODEL / CFD  
 comparison of granulator configurations

**Wurster-Coater**



**Application:**  
 tablet coating,  
 encapsulation of flavors.

**Spouted bed**



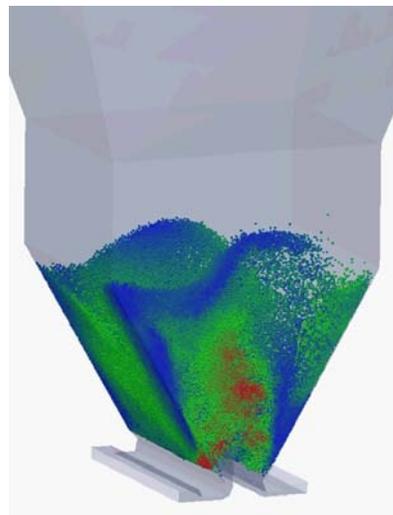
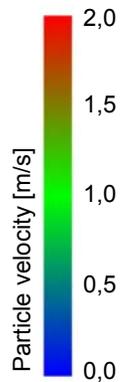
**Application:**  
 very fine, cohesive and non-spherical  
 particles

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RESULTS DISCRETE PARTICLE MODEL / CFD  
 comparison of granulator configurations

**Spouted bed**

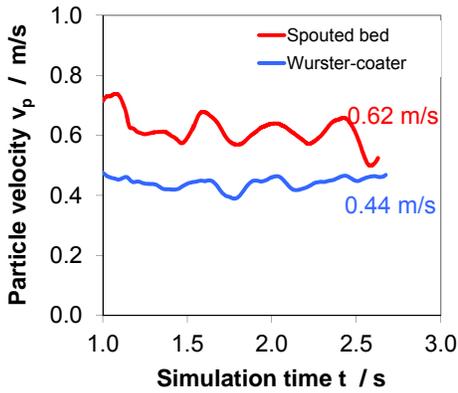
Joint STW/DFG project



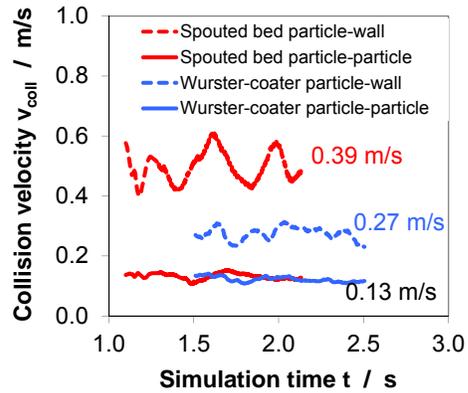
150.000 Particle,  $d_p = 2$  mm, Density  $\rho_p = 1500$  kg/m<sup>3</sup>, Bed mass = 0.94 kg,  $e = 0.8$ , Simulation time 30 s

RESULTS DISCRETE PARTICLE MODEL / CFD  
comparison of granulator configurations

Translation: mean particle velocity



Collision dynamics

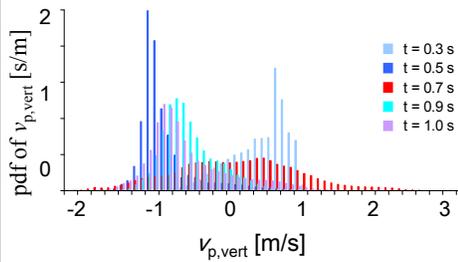


**Spouted bed:** Higher impact energy for particle-wall collisions  
→ Increased agglomerate strength

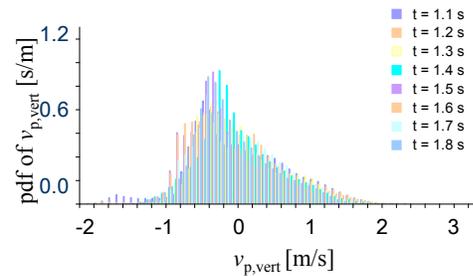
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RESULTS DISCRETE PARTICLE MODEL / CFD  
spouted bed behaviour

start-up process from fixed bed  
(transient), simulation time  $t = 0 \rightarrow 1$  s



steady-state spouting,  $t > 1$  s

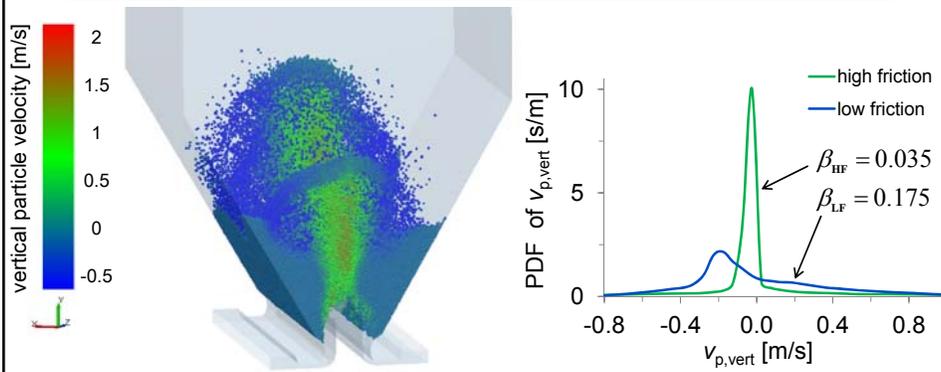


- Typical distribution of vertical particle velocities for spouted bed was found
- This kind of parameters can't be measured up-to-day by available methods. They can be obtained only from a simulation.

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## RESULTS DISCRETE PARTICLE MODEL / CFD

### stable spouted bed behaviour

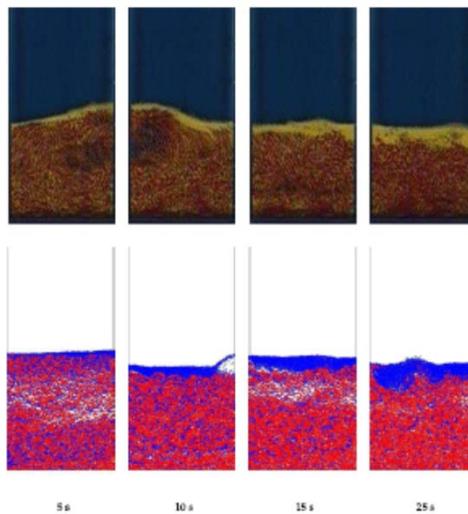


- High friction influences the particle mobility  $\beta$
- The spread of the function strongly decreases
- The shape of velocity distribution changes from Gumbel Max to Gumbel Min (skewed to the left)

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## RESULTS DPM MODEL

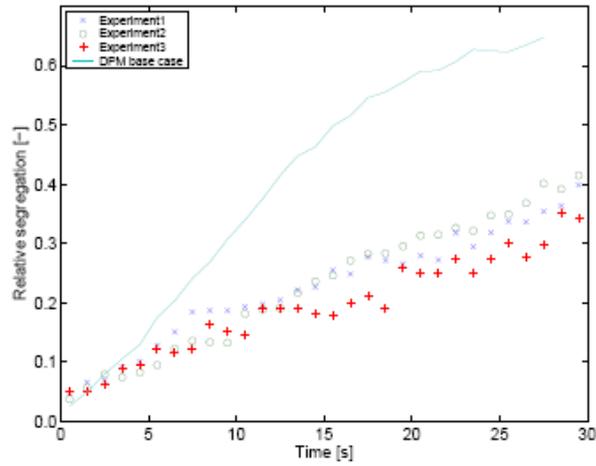
### segregation in bidisperse systems



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RESULTS DPM MODEL  
segregation in bidisperse systems

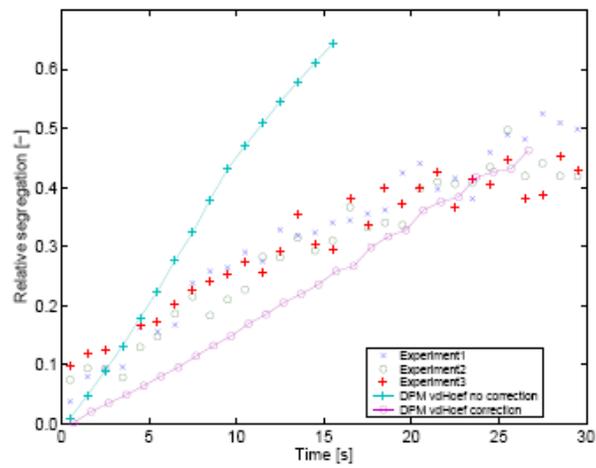
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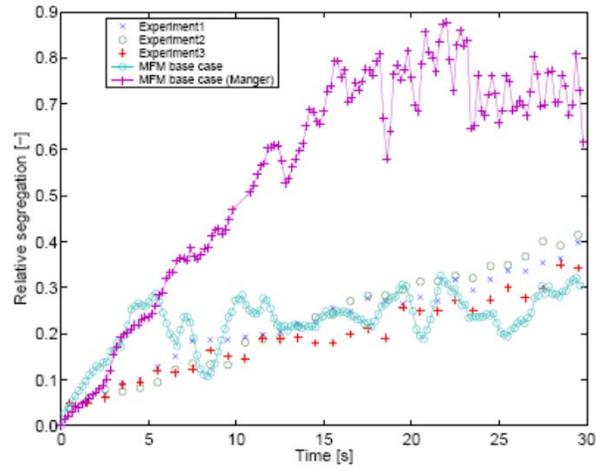
RESULTS DPM MODEL  
segregation in bidisperse systems

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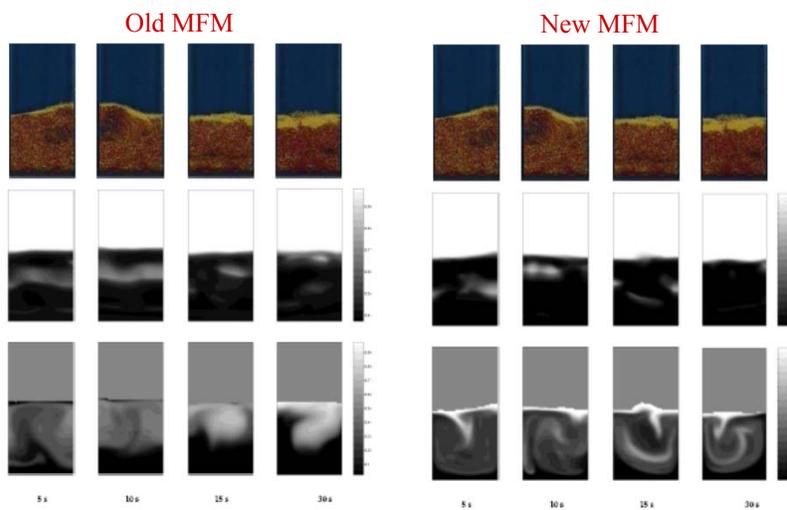
44

RESULTS MFM MODEL  
segregation in bidisperse systems

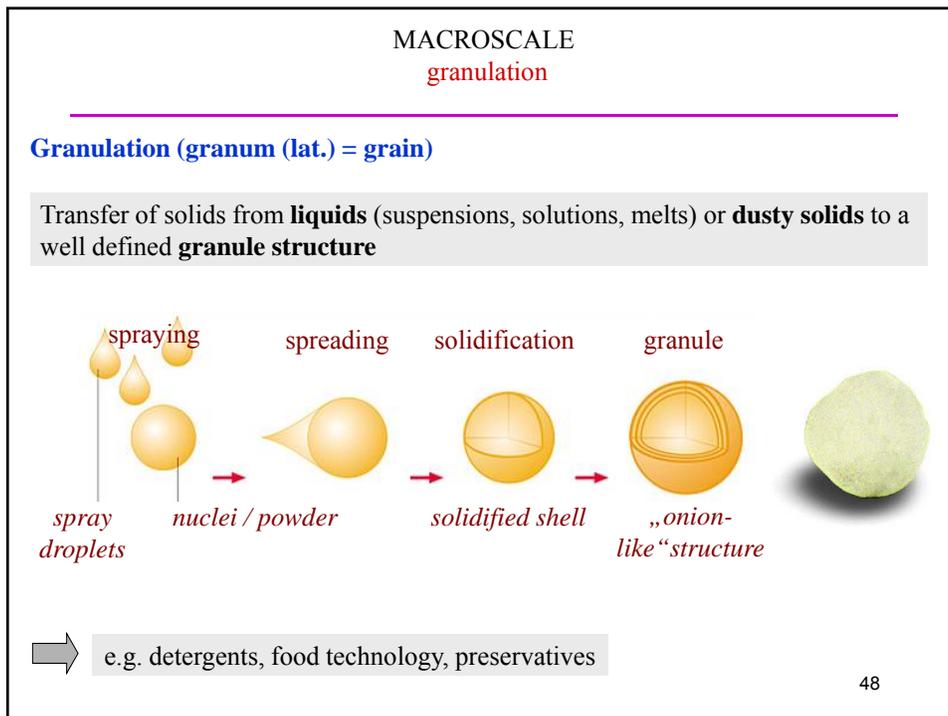
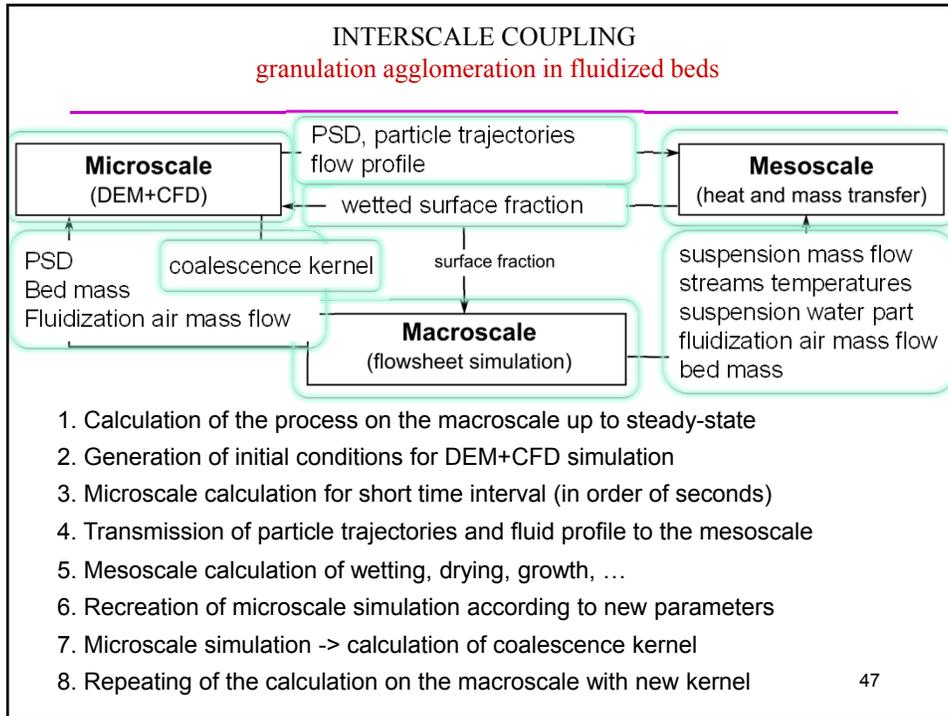


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RESULTS MFM MODEL  
segregation in bidisperse systems



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MACROSCALE  
population balance model for granulation

For the description of the change of particle size distribution, a one-dimensional  
Population Balance Model (PBM) has been used

$$\frac{\partial n_{\text{tot}} q_{0,b}}{\partial t} = - \underbrace{\frac{\partial G_e n_{\text{tot}} q_{0,b}}{\partial d_p}}_{\text{Growth rate}} + \underbrace{\dot{n}_{\text{in}} q_{0,\text{in}} - \dot{n}_{\text{out}} q_{0,\text{out}}}_{\text{Input and output streams}}$$

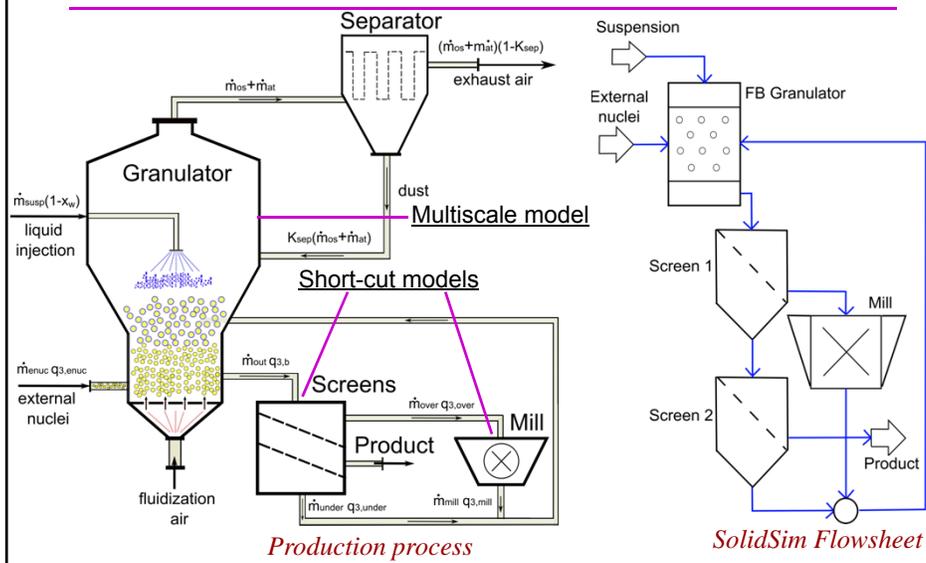
Empirical model:

$$G_e = \frac{2 \cdot \dot{M}_e}{\rho \cdot A_{\text{tot}}}$$

$$\dot{M}_e = \dot{M}_{\text{susp}} \cdot (1 - x_w)$$

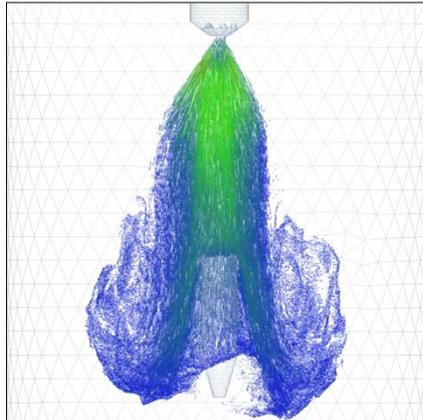
$G_e$	Growth rate [m/s]
$A_{\text{tot}}$	Total particle surface [m <sup>2</sup> ]
$\dot{M}_e$	Effective mass stream [kg/s]
$\rho$	Particle density [kg/m <sup>3</sup> ]
$\dot{M}_{\text{susp}}$	Suspension mass stream [kg/s]
$x_w$	Water part in suspension [%]

MACROSCALE  
flowsheet of granulation process



M. Dosta, S. Heinrich, J. Werther, Powder Technology, 204, 71-82, 2010<sup>50</sup>

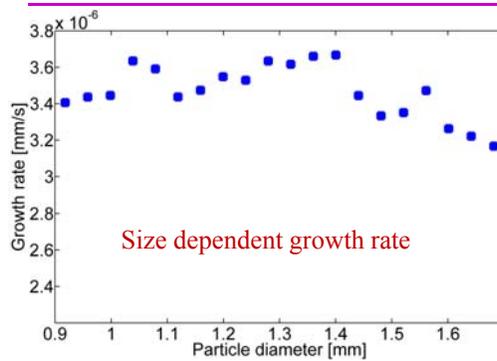
MICROSCALE  
DEM simulation of the nozzle zone



 ECCE\_Heine\_2.avi

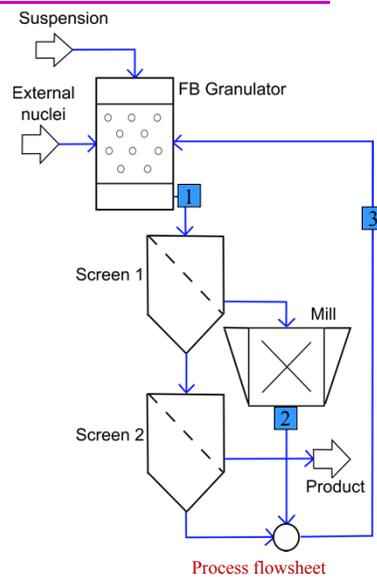
 ECCE\_Heine.avi

MACROSCALE  
simulation results



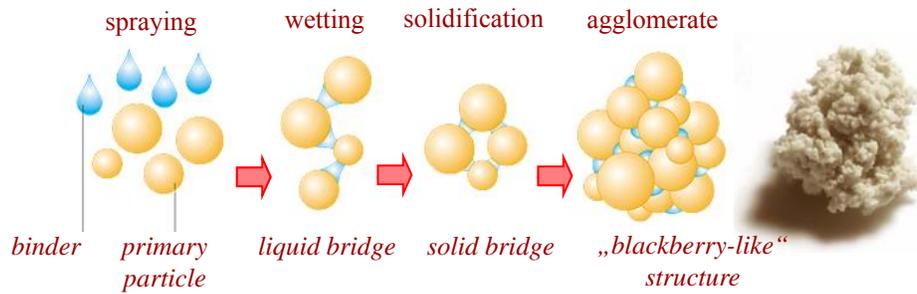
Empirical model / Growth rate from multiscale model

Stream	Median [mm]	Mass stream [g/s]
1	1.03 / 0.954	2.25 / 2.32
2	0.9 / 0.9	0.305 / 0.219
3	0.941 / 0.868	1.6 / 2.45



MACROSCALE  
agglomeration

Agglomeration (agglomerare (lat.) = to agglomerate)  
of primary particles (powder)

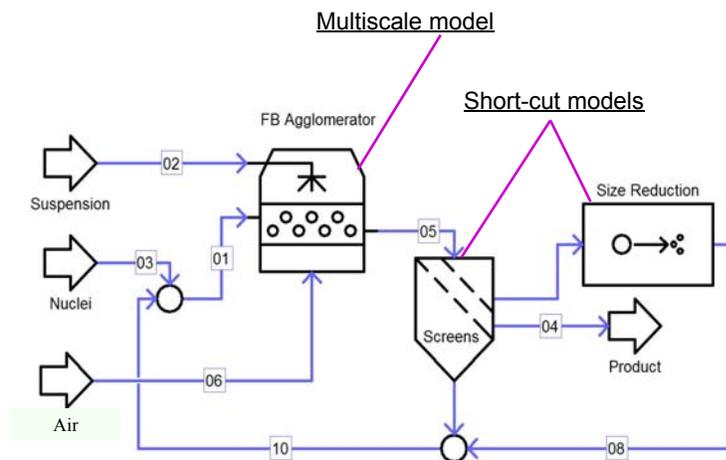


→ e.g. pharmaceutical technology, combination of active agents and excipients, instant coffee

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MACROSCALE  
flowsheet of agglomeration process

- As an simulation example the continuous agglomeration process has been used



**MACROSCALE**  
**population balance model for agglomeration**

- The agglomeration process on the macroscale has been described by population balance model
- PBM of pure agglomeration (no growth, breakage or attrition)

$$\frac{\partial n(t, v)}{\partial v} = B_{\text{agg}}(t, v) - D_{\text{agg}}(t, v) + \dot{n}_{\text{in}}(t, v) - \dot{n}_{\text{out}}(t, v)$$

where

$$B_{\text{agg}}(t, v) = \frac{1}{2N_{\text{tot}}(t)} \int_0^v \beta(t, v-u, u) \cdot n(t, u) \cdot n(t, v-u) du \quad \text{birth rate}$$

$$D_{\text{agg}}(t, v) = \frac{1}{N_{\text{tot}}(t)} \int_0^\infty \beta(t, v, u) \cdot n(t, u) \cdot n(t, v) du \quad \text{death rate}$$

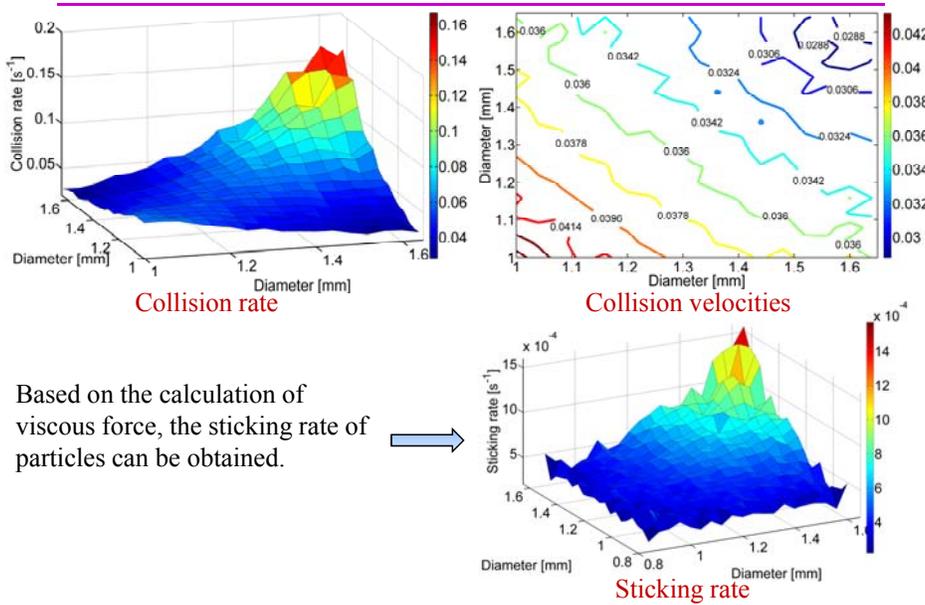
- One of the main process parameters – coalescence kernel  $\beta(t, v, u)$

$$\beta(t, v, u) = \beta_0(t) \cdot \beta^*(v, u)$$

where  $\beta_0(t)$  - time dependent part,  $\beta^*(v, u)$  - size dependent part

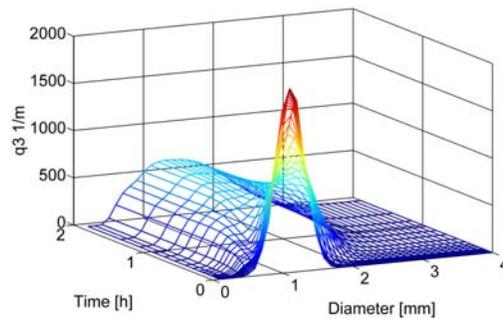
➡ *obtaining of physical based coalescence kernel*

**MICROSCALE**  
**simulation results for agglomeration**



## MACROSCALE simulation results for agglomeration

- The contact forces which arise from subsequent collisions with neighbour particles can cause the **rupture** of the formed liquid bridge
- A **force balance** including viscous adhesion forces in the liquid bridge and separating forces due to collisions is solved on the microscale
- The received results are used to calculate the **probability for the destruction of a liquid bridges** connecting two particles due to further collisions with other particles



Time progression of PSD of macro process

## CONCLUSIONS

- The multiscale simulation leads to more detailed process description, where material microproperties **can be considered**
- Accurate closures are required for fluid-particle and particle-particle interactions
- Complex solids processes with multiple process units can be described by **flowsheet simulation**
- In this contribution the general view of **simulation framework** has been proposed and applied for granulation/agglomeration processes