

**JMBC course : Particle Technology**  
**April 29 – May 03, 2019 U-Parkhotel,**  
**UTwente, NL**

**Gas-Solid Filtration**



**JMBC course 2019**  
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## Outline

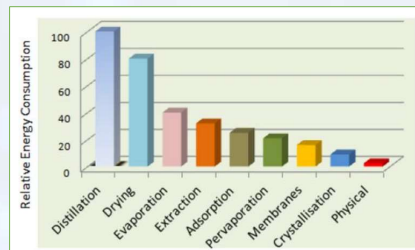
- Solid-gas separation
  - Purposes
  - Stokes law, Terminal velocity, Drag coefficient, Kozeny and Carman equation
  - Dust collectors, Baghouse filter systems
  - Electrostatic precipitators
  - Cyclones

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## Solid-gas separation



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## Solid-gas separation

- **Sedimentation**, in which the solids are allowed to settle by gravity through the fluid
- **Filtration**, in which the solids are collected on a medium, such as a porous material or a layer of fine particles, through which the fluid is pumped.
- **Centrifugal separation**, in which the solids are forced on to the walls of a vessel which is rotated to provide the centrifugal force.

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## Solid-gas separation: purposes

The need to remove suspended dust and mist from a gas arises not only in the treatment of effluent gas from a plant before it is discharged into the atmosphere but also in processes where solids are carried over in the vapour or gas stream.

In a plant involving a fluidised solid the removal of fine particles is necessary, first to prevent loss of material, and secondly to prevent contamination of the gaseous product.

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## Solid-gas separation: purposes

- Air-pollution control, as in fly-ash removal from power-plant flue gases.
- Equipment-maintenance reduction, as in filtration of engine intake air or pyrites furnace-gas treatment prior to its entry to a contact sulfuric acid plant.
- Safety- or health-hazard elimination, as in collection of siliceous and metallic dusts around grinding and drilling equipment and in some metallurgical operations and flour dusts from milling or bagging operations.
- Product-quality improvement, as in air cleaning in the production of pharmaceutical products and photographic film.
- Recovery of a valuable product, as in collection of dusts from dryers and smelters.
- In all pneumatic conveying plants, some form of separator must be provided at the downstream end.
- In spray drying; and the manufacture of high purity chemical products in granular form.

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## Solid-gas separation

- Whereas relatively large particles with **settling velocities** greater than about 0.3 m/s readily disengage themselves from a gas stream, fine particles tend to follow the same path as the gas and separation is therefore difficult.
- In practice, **dust particles** may have an average diameter of about 0.01 mm (10  $\mu\text{m}$ ) and a settling velocity of about 0.003 m/s, so that a simple gravity settling vessel would be impracticable because of the long time required for settling and the large size of separator which would be required for a given throughput of gas.

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## Solid-gas separation

Gases are separated from dispersed particles by passing it through a fabric or ceramic **filter** "**medium**" with a large surface area.

Particles that are not able to penetrate the medium will be retained on its surface, forming the so-called "**filter cake**".

As the particles on the cloth build up, they form a cake that acts as a filter, and often is a more effective filter than the fabric or screen.

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## Parameters

- Terminal velocity**
- Porosity of the cake**
- Pressure drop**
- Allowable gas velocity**

Typically the face velocity (= gas flow/filter surface, unit: m/s)  
also referred to as “air-to-cloth” (A/C) ratio is in the range 0.5 - 5 cm/s.

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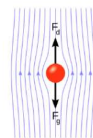
## Parameters

### Fluid Mechanics

- When fluid flows over an immersed body, forces are exerted on that body. The resultant force parallel to the fluid motion is referred to as the **drag**.

We will want to find:

- Terminal velocity** (maximum settling velocity)
- Settling time.**
- Drag Coefficient for spherical particle**



Laminar flow past a sphere: streamlines, **drag force  $F_d$**  and force by **gravity  $F_g$** .

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# Parameters

## Stokes Law

- Drag ( $F_d$ ) consists of both friction and pressure drag, and it is often expressed in terms of a drag coefficient ( $C_D$ ) as:

$$F_d = \frac{C_D \rho A v^2}{2}$$

A is projected area of particle  
 $\rho$  is density of fluid  
 $v$  is the approach velocity of fluid  
 Now define the ratio of drag force and area (R)

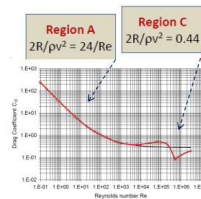
$$\frac{F_d}{A} = \varphi = \frac{C_D \rho v^2}{2} \text{ i.e. } C_D \text{ is a function of } \frac{2R}{\rho v^2}$$

At very small Reynolds numbers (<0.2)  
 Stokes has shown that the drag coefficient is a linear function of the Reynolds number.

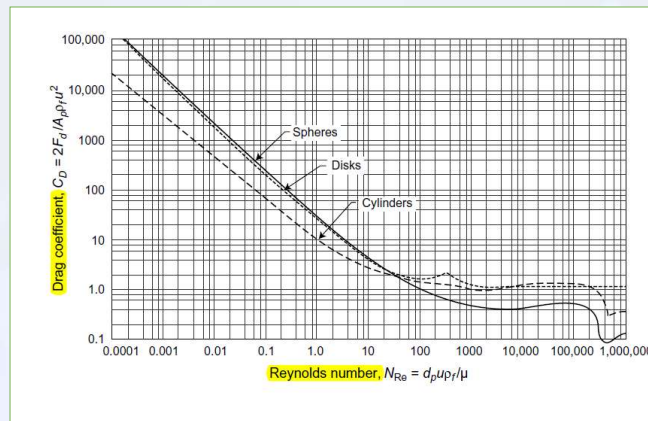
$$C_D = \frac{24}{Re}$$

$$\text{so } \varphi = \frac{12}{Re} \rho v^2$$

$$(Re = \rho v L / \mu)$$



# Parameters



## Parameters

- Drag coefficients may also be a function of variables not displayed in the plot, which leads to additional correlations and equations. These include:
  - particle velocity history
  - particle shape
  - the effect of walls and collisions with other particles
  - Random Brownian movement, if the particles are very small.

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## Parameters

- **Terminal velocity** of the particle,  $u_t$ , which is defined as the fluid velocity that renders a particle, subject to gravitational force, motionless when suspended unhindered in an upward-flowing fluid stream.
- At that condition, the drag force on the particle plus the buoyant force balance the force of gravity.

$$u_t = \sqrt{\frac{4d_p g (\rho_p - \rho_f)}{3C_D \rho_f}}$$

where:  $d_p$  is particle diameter;  $\rho_p$  is particle density;  $\rho_f$  is fluid density;  $u_t$  is terminal velocity (or settling velocity in a quiescent fluid);  $g$  is acceleration due to gravity; and  $C_D$  is the dimensionless drag coefficient.

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## Parameters

- The **drag coefficient**  $C_D$  is related to the **drag force**  $F_d$  on the projected area,  $A_p$ , of a spherical particle by

$$F_D = C_D \left( \frac{\pi d_p^2}{4} \right) \left( \frac{u_t^2}{2} \right) \rho_f$$

where:  $d_p$  is particle diameter;  $\rho_f$  is fluid density;  $u_t$  is terminal velocity (or settling velocity in a quiescent fluid) and  $C_D$  is the dimensionless drag coefficient.

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## Parameters

- Stokes' law,  $F_d = 3\pi\mu u d_p$ , which applies at  $Re < 2$ , gives  $C_D = 24/Re$ . Substitution gives the settling velocity for a spherical particle of diameter  $d_p$  as

$$u_t = \frac{g d_p^2 (\rho_p - \rho_f)}{18\mu}$$

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## Parameters

- **Porosity**

$$\varepsilon = 1 - \frac{W}{\rho_p L}$$

where W is the mass of powder deposited on the filtering medium per unit of area.

$\rho_p$  is the particle density and L represents the thickness of the dust cake.

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## Parameters

- **Kozeny and Carman** derived a semi-empirical equation that represents the dust cake as a series of parallel capillaries or channels whose total volume equals the void volume of the cake and whose surface area equals the surface area of the particles constituting the cake.
- The specific dust cake resistance coefficient is defined as a function of the dust cake porosity  $\varepsilon$ .

$$K = \frac{18\mu}{\rho_p D_{vs}^2 C} \frac{2k(1 - \varepsilon)}{\varepsilon^3}$$

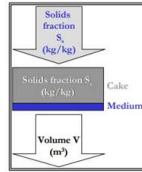
- Where the empirical constant k is equal to 4.8 for spherical particles and 5 for irregular particles and  $D_{vs}$  is the volume-surface mean diameter (or Sauter diameter).

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## Parameters



Fluid flow influenced by pressure differential across the filter

$$\text{Rate of filtration} = \frac{\text{Driving force}}{\text{Resistance}}$$

For a filter cake with porosity  $\epsilon$ , specific cake resistance  $\alpha$  (m/kg) can be defined as:

$$\alpha = \frac{1}{K(1-\epsilon)\rho_p}$$

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## Parameters

- When the deposited cake has a mass  $w$  (kg/m<sup>2</sup>) per unit filter surface, Ruth's equation gives (for filtration along  $x$  axis), with medium resistance  $R$  (1/m).

$$dw = (1 - \epsilon)\rho_{solid} dx$$

$$u = \frac{1}{\alpha(1-\epsilon)\rho_p} \frac{\Delta P}{L\mu_f} = \frac{\Delta P}{(\alpha w + R)\mu_f}$$

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## Parameters

- The cake mass,  $w$ , in  $\text{kg/m}^2$  filter surface, depends on the volume  $V$  ( $\text{m}^3$ ) of fluid that has been filtered per unit area, the density of fluid ( $\text{kg/m}^3$ ) of the fluid, and the fractions  $S_s$  and  $S_c$  ( $\text{kg/kg}$ ) of solids in the incoming fluid and the cake, respectively. A mass balance gives

$$w = \left( \rho_f V + \frac{w}{S_c} (1 - S_c) \right) \left( \frac{S_s}{(1 - S_s)} \right)$$

$$w = Vf(\rho_f, S_c, S_s)$$

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## Parameters

With the function  $f$  defined as:

$$f(\rho_{fluid}, S_c, S_s) = \left( \frac{\rho_{fluid}}{\left( \frac{1 - S_s}{S_s} \right) - \left( \frac{1 - S_c}{S_c} \right)} \right)$$

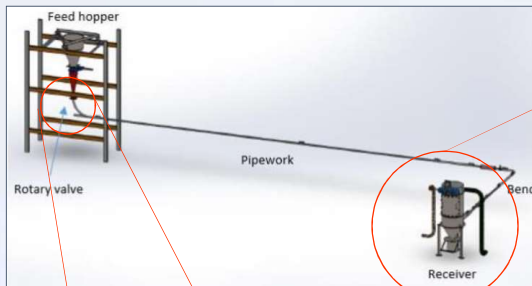
Note :  $u$  and  $V$  per  $\text{m}^2$  surface,  $A$  ! Throughput  $Q$  ( $\text{m}^3/\text{s}$ ) =  $uA$

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## An experiment



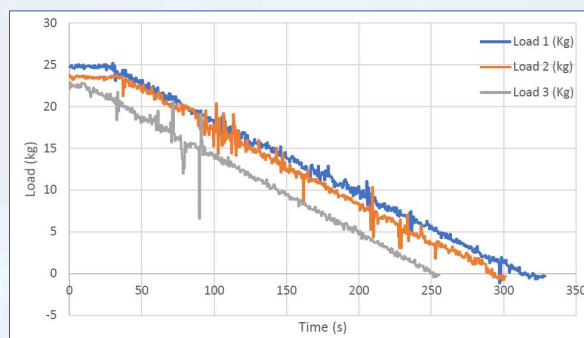
<https://youtu.be/SR6yVTqGRTw>

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## Rotary valve

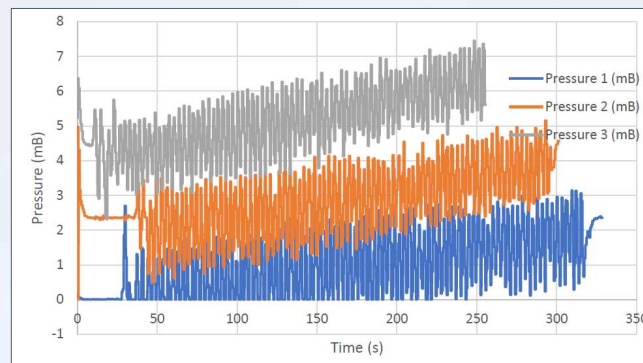


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## Pressure on the filtering system



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## Industrial applications

- A very common industrial filtration device is a fabric dust collector.
- In industry, multiple collectors are housed in enclosures called baghouses.
- Capable of capturing particles down to  $0.05 \mu\text{m}$ .
- Particles are collected on the outside of a fabric-encased, porous, cylindrical candle.
- The device has a vibratory or compressed-air blowback system to remove the particles trapped on the outside of the filter element.

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## Gas filters

Medium properties: chemical and physical stability  
Filter clean-up and capacity for regeneration

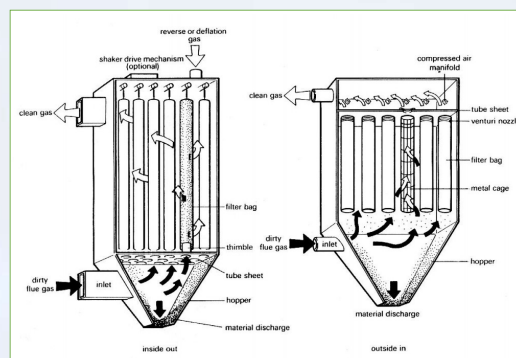
Major type of filters	Factors determining process quality
<b>Bag filters</b> made of fabric fibre materials textile, plastics, ceramic	Removal efficiency
<b>Rigid barrier filters</b> made of metal or of sintered ceramic, powder or fibres	Pressure drop, pressure drop increase
<b>Granular bed filters</b> based on a layer of granular solids	Filtration velocity = flow / filter area

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## Baghouse filter systems



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## Electrostatic precipitators

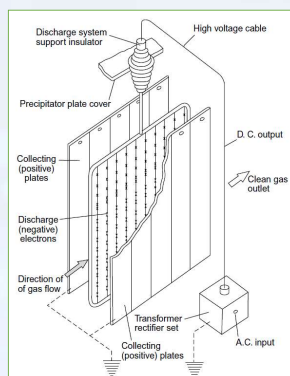
- Electrostatic precipitators are best suited for the collection of fine mists and submicron particles.
- The first practical application was fashioned by Cottrell in 1907 for abating sulfuric acid mists.
- Particle suspended in an ionized gas stream within an electrostatic field will become charged and migrate to a collecting surface.
- To obtain ionization, the voltage must be high enough to initiate a corona discharge, but not so high as to cause sparking.

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## Electrostatic precipitators



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## (Some) references

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