



# JMBC Particle Technology 2019

## Fluidization

Ruud van Ommen\*

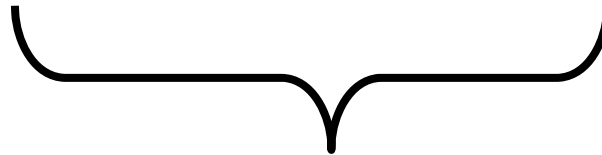
With material from Naoko Ellis\*\*

\*Delft University of Technology, the Netherlands

\*\*University of British Columbia, Canada

# Powder Flow versus Gas-Particle Flow

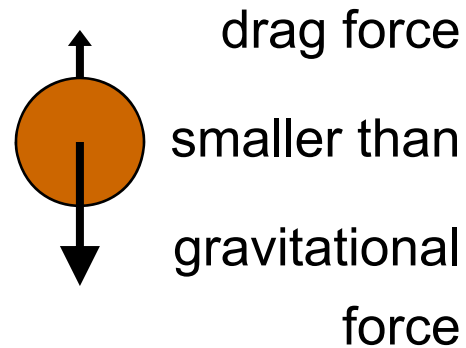
- First particle-particle interaction, then gas-particle interaction
  - Research area:  
granular matter
- First gas-particle interaction, then particle-particle interaction
  - Research area:  
fluid mechanics



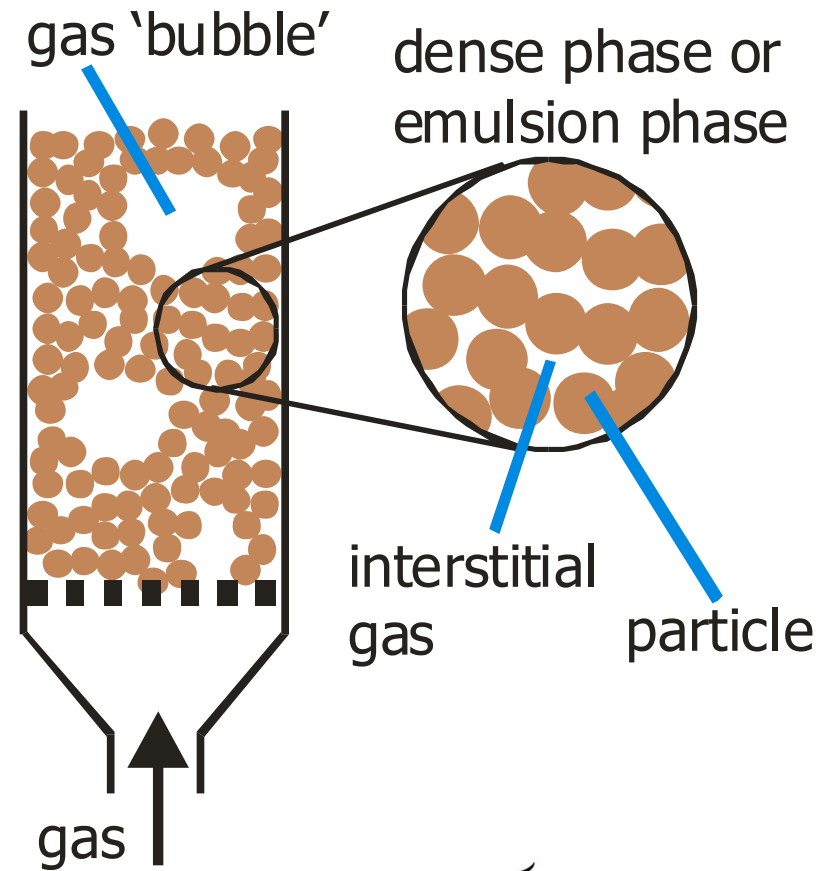
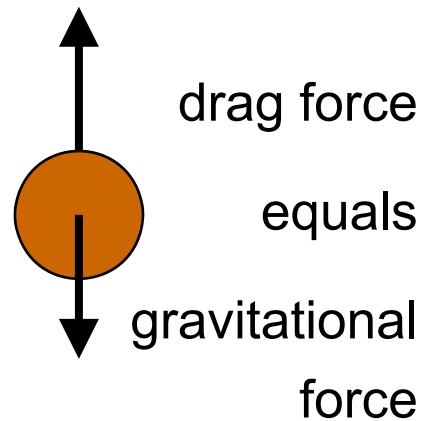
**Chemical Engineering / Particle Technology**

# Intro gas-solids fluidized bed

Packed bed:  
particles are  
stagnant



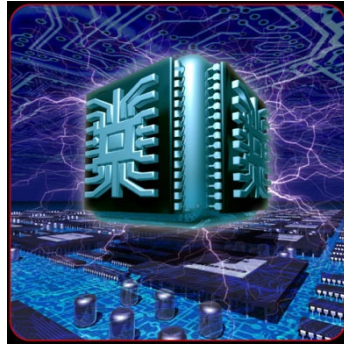
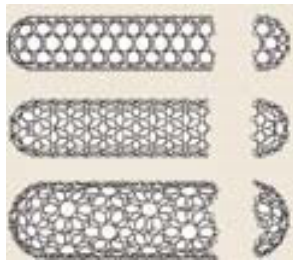
Fluidized bed:  
particles  
suspended in  
an upward  
gas stream;  
they move



# Significance of Fluidized beds

## Advanced materials

- Silicon production for semiconductor and solar industry
- Coated nanoparticles
- Nano carbon tubes



## Chemical and Petrochemical

- Cracking of hydrocarbons
- Gas phase polymeric reactions

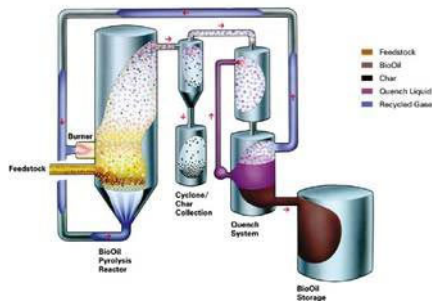


## Physical operations

- Coating of metal and glass objects
- Drying of solids
- Roasting of food
- Classify particles

## Combustion/pyrolysis

- Combustion/gasification of coal
- Pyrolysis of wood waste
- Chemical looping combustion

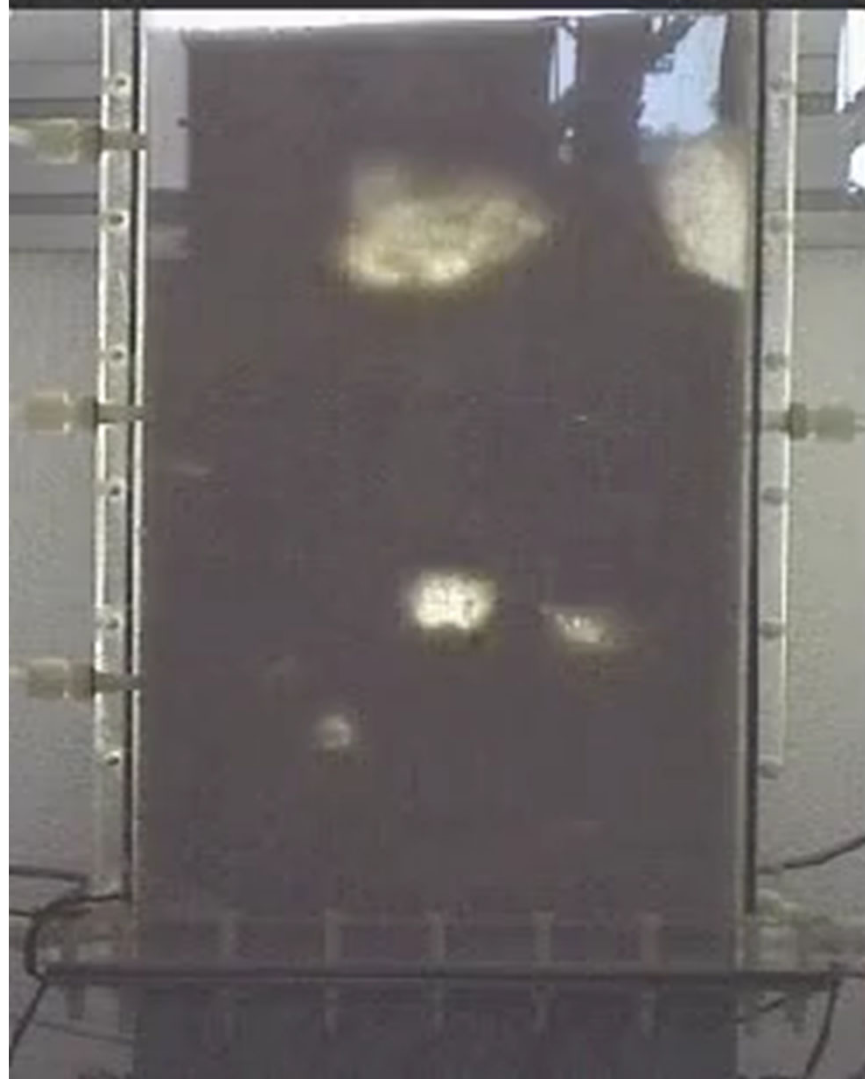


<http://www.chemsoc.org/timeline/pages/1961.html>  
<http://physicsweb.org/article/world/11/1/9>  
[www.unb.ca/che/che5134/fluidization.html](http://www.unb.ca/che/che5134/fluidization.html)  
<http://www.niroinc.com/html/drying/fdfliuidtype.html>  
<http://www.dynamotive.com/biooil/technology.html>

## Pharmaceutical

- Coating of pills
- Granulation
- Production of plant and animal cells

## Gas-Solid Fluidized Bed



# Characteristics of Gas Fluidized Beds

## Primary Characteristics:

- Bed behaves like liquid of the same bulk density – can add or remove particles
- Rapid particle motion – good solids mixing
- Very large surface area available

## Question

What is the surface area of 1 m<sup>3</sup> of 100 μm particles?

# Characteristics of Gas Fluidized Beds

## Secondary Characteristics:

- Good heat transfer from surface to bed, and gas to particles
- Isothermal conditions radially and axially
- Pressure drop depends only on bed depth and particle density – does not increase with gas velocity (ideal case)
- Particle motion usually streamlines → erosion and attrition



# (Dis)advantages of fluid beds

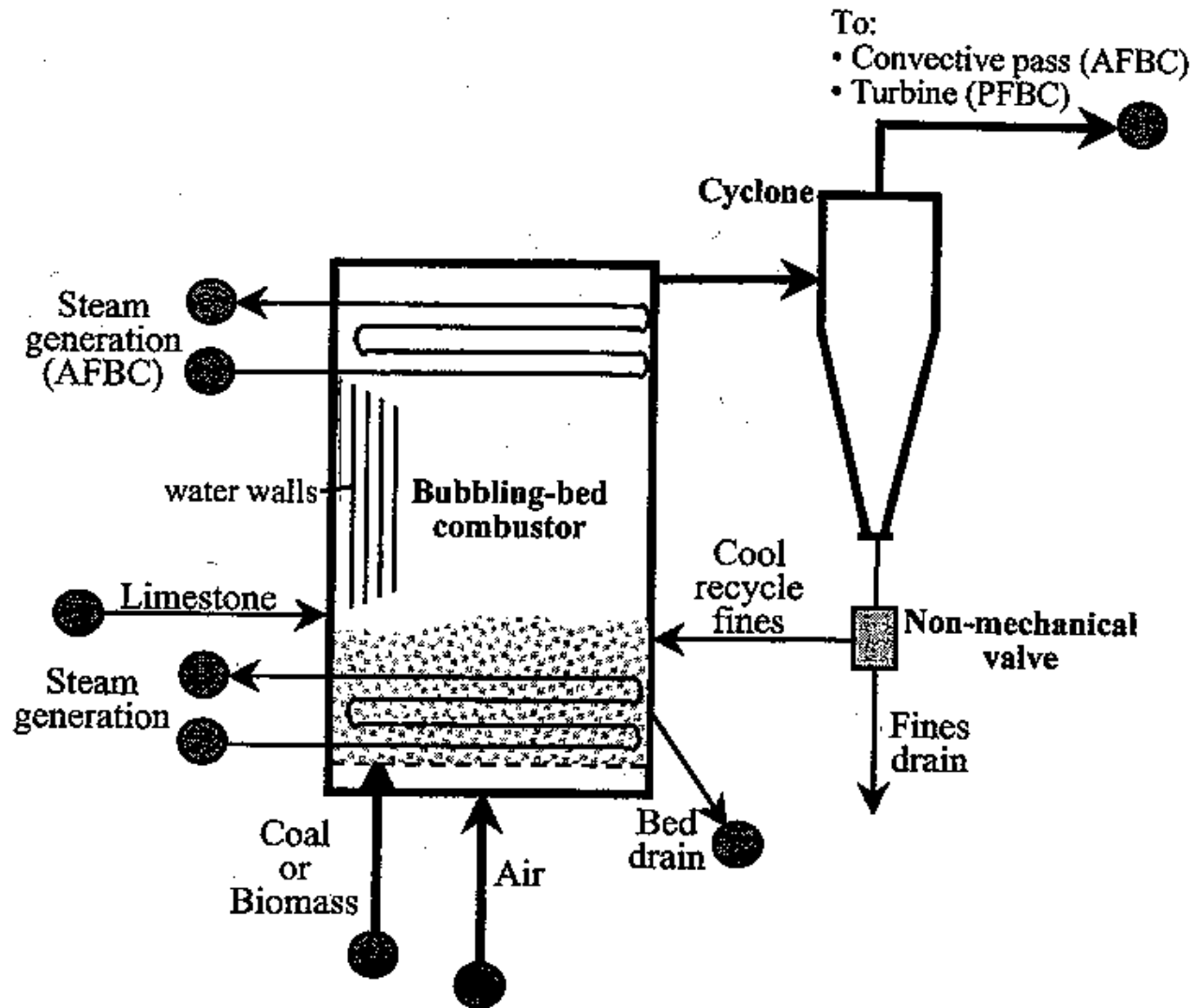
## **Advantages**

- good G-S mass transfer in dense phase
- good heat transfer
- easy solids handling
- low pressure drop

## **Disadvantages**

- ◆ bypass of gas in bubbles
- ◆ broad RTD gas and solids
- ◆ erosion of internals
- ◆ attrition of solids
- ◆ difficult scale-up

# Basic Components

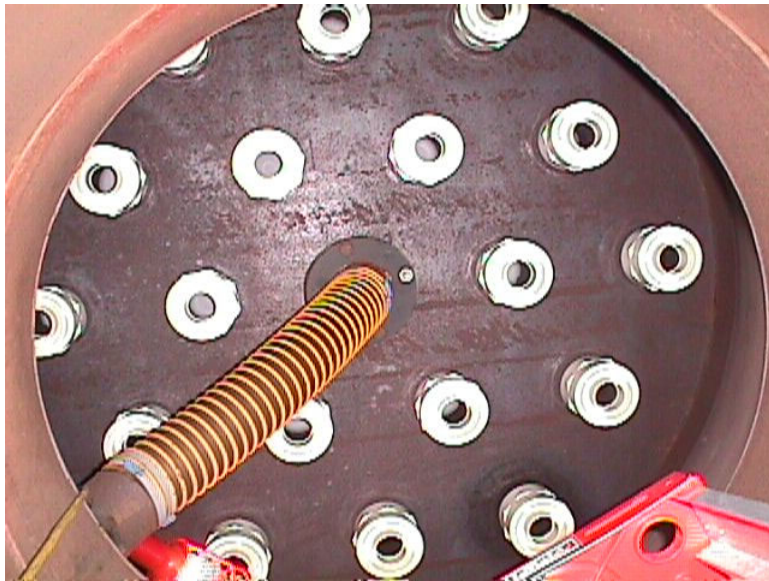


Yang W. Bubbling fluidized beds (Chapter 3). In: *Handbook of Fluidization and Fluid-Particle Systems*. Yang W (Ed.). Marcel Dekker, Inc., NY, NY, USA, 53–113 (2003).

# 1.56 m Diameter Column



# Industrial Scale



Solid offtake

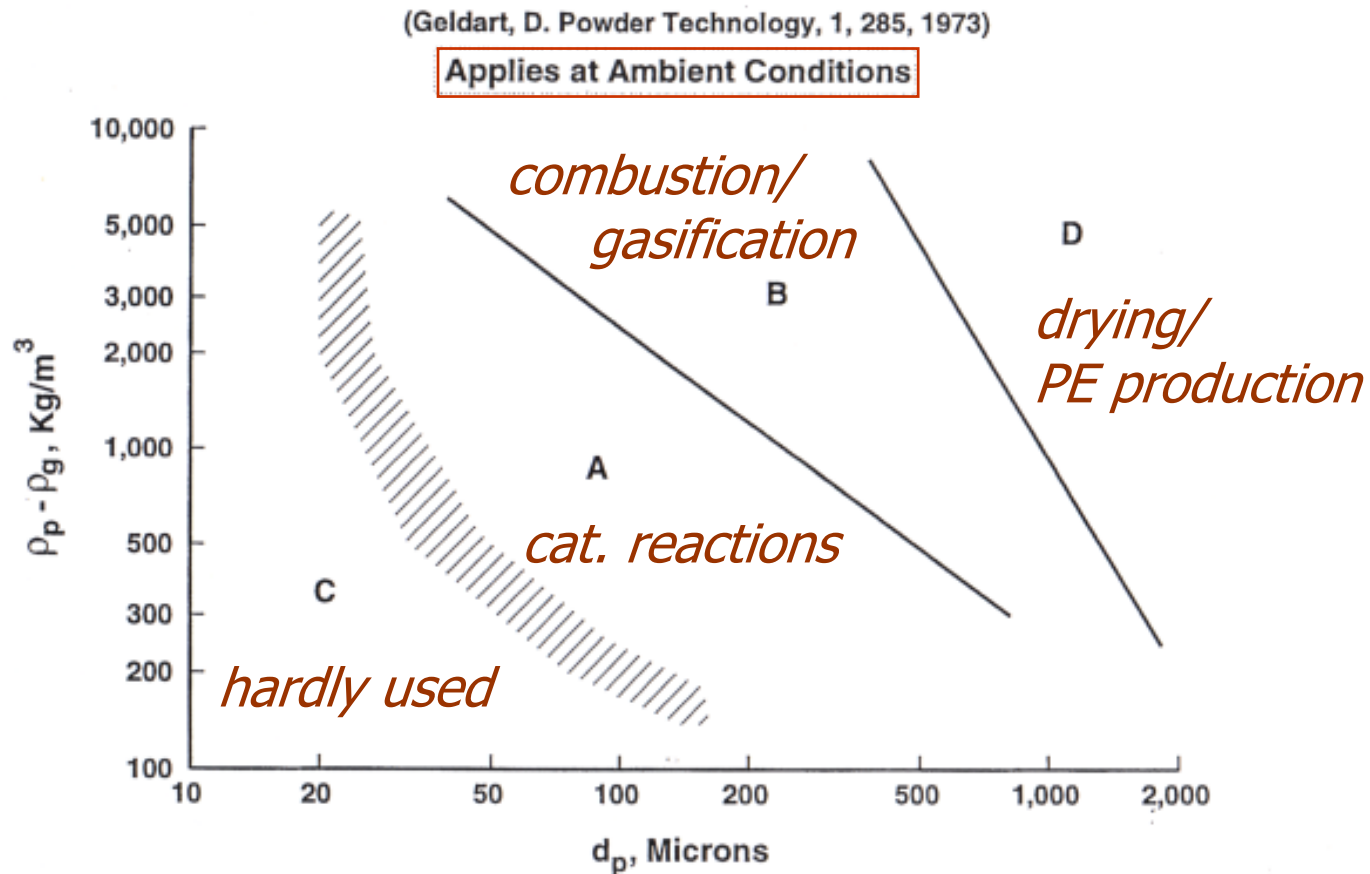


A Fluid Catalytic Cracking Unit. Photo courtesy of Grace Davison.

# Approaches to the Study of Particulate Systems

- Totally empirical (leading to dimensional correlations)
- Empirical guided by scientific principles (e.g. Buckingham Pi Theorem to obtain dimensionally consistent correlations)
- Semi-empirical, i.e. some mechanistic basis, but with one or more empirical constants
- Mechanistic physical model without any empiricism, numerical solutions of governing equations of motion and transport

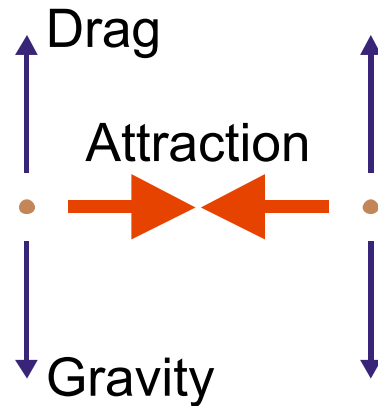
# Geldart's powder classification



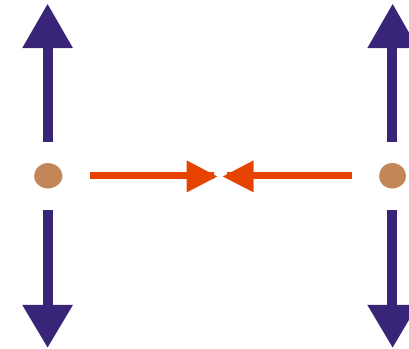
- A: Aeratable ( $U_{mb} > U_{mf}$ ) Material Has a Significant Deaeration Time (FCC Catalyst)
- B: Bubbles Above  $U_{mf}$  ( $U_{mb} = U_{mf}$ ) (500-micron Sand)
- C: Cohesive (Flour, Fly Ash)
- D: Spoutable (Wheat, 2000-micron Polyethylene Pellets)

# Geldart's powder classification

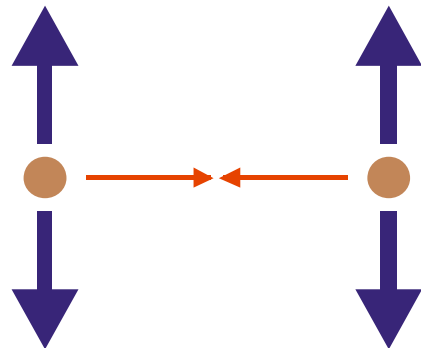
**C**  
Cohesive  
0-30  $\mu\text{m}$   
*flour*



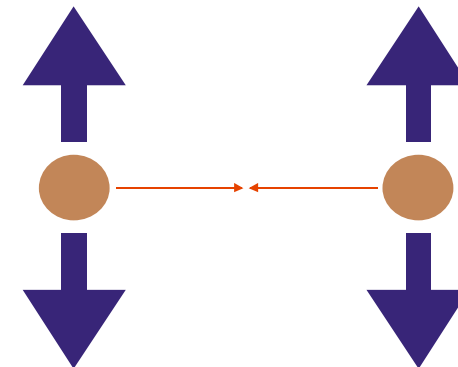
**A**  
Aeratable  
30-100  $\mu\text{m}$   
*milk powder*



**B**  
Bubbling  
100-1000  $\mu\text{m}$   
*sand*



**D**  
Spoutable  
>1000  $\mu\text{m}$   
*coffee beans*



## Group C

- Cohesive
- Difficult to fluidize, and channeling occurs
- Interparticle forces greatly affect the fluidization behaviour of these powders
- Mechanical powder compaction, prior to fluidization, greatly affected the fluidization behaviour of the powder, even after the powder had been fully fluidized for a while
- Saturating the fluidization air with humidity reduced the formation of agglomerates and greatly improved the fluidization quality. The water molecules adsorbed on the particle surface presumably reduced the van der Waals forces.
- $d_p \sim 0-30 \mu\text{m}$
- Example: flour, cement





## Group A

- Aeratable
- Characterized by a small  $d_p$  and small  $\rho_p$
- $U_{mb}$  is significantly larger than  $U_{mf}$
- Large bed expansion before bubbling starts
- Gross circulation of powder even if only a few bubbles are present
- Large gas backmixing in the emulsion phase
- Rate at which gas is exchanged between the bubbles and the emulsion is high
- Bubble size reduced by either using a wider particle size distribution or reducing the average particle diameter
- There is a maximum bubble size
- $d_p \sim 30-100 \mu\text{m}$
- Examples: FCC, milk flour



## Group B

- Bubbling
- $U_{mb}$  and  $U_{mf}$  are almost identical
- Solids recirculation rates are smaller
- Less gas backmixing in the emulsion phase
- Rate at which gas is exchanged between bubbles and emulsion is smaller
- Bubbles size is almost independent of the mean particle diameter and the width of the particle size distribution
- No observable maximum bubble size
- $d_p \sim 100-1000 \mu\text{m}$
- Example: sand

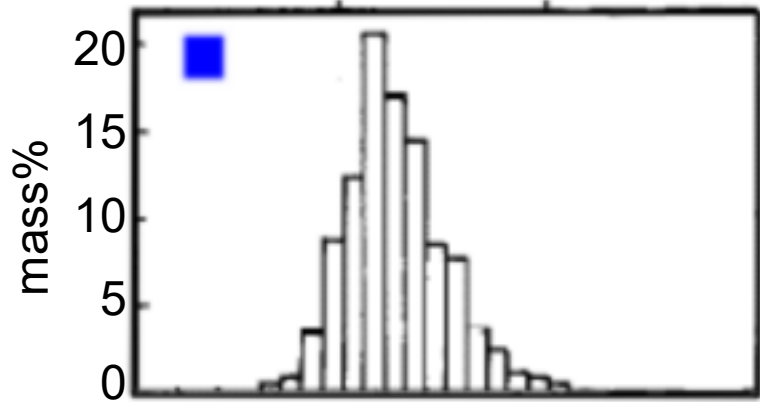
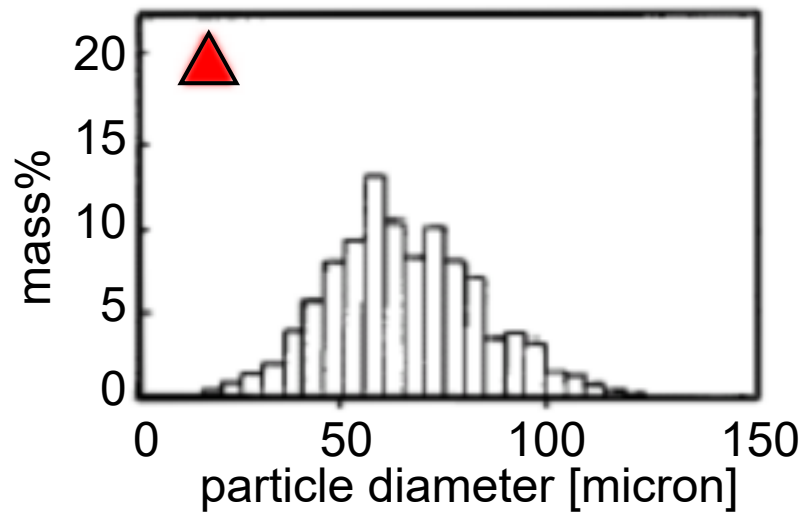


## Group D

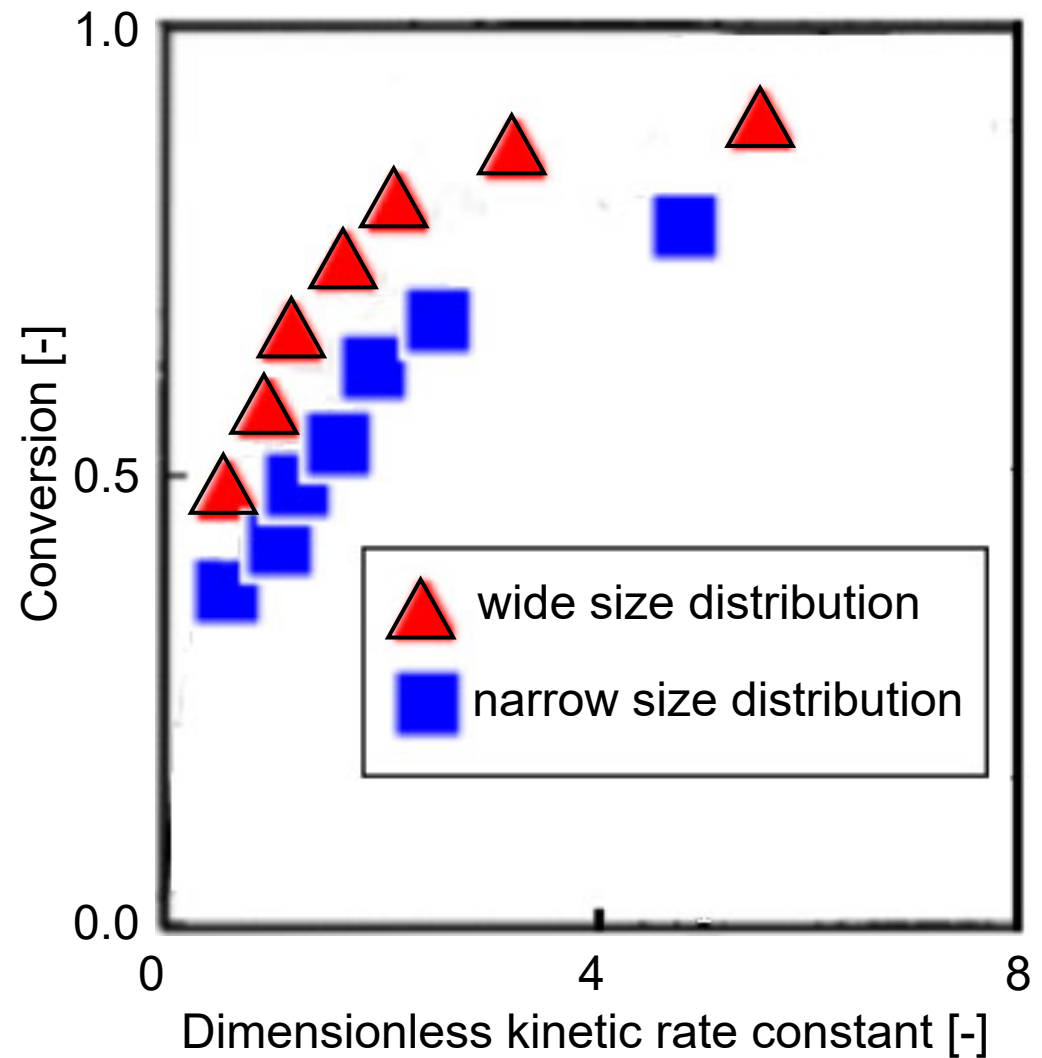
- Spoutable
- Either very large or very dense particles
- Bubbles coalesce rapidly and flow to large size
- Bubbles rise more slowly than the rest of the gas percolating through the emulsion
- Dense phase has a low voidage
- $d_p \sim > 1000 \text{ mm}$
- Examples: Coffee beans, wheat, lead shot



# Influence of particle size distribution

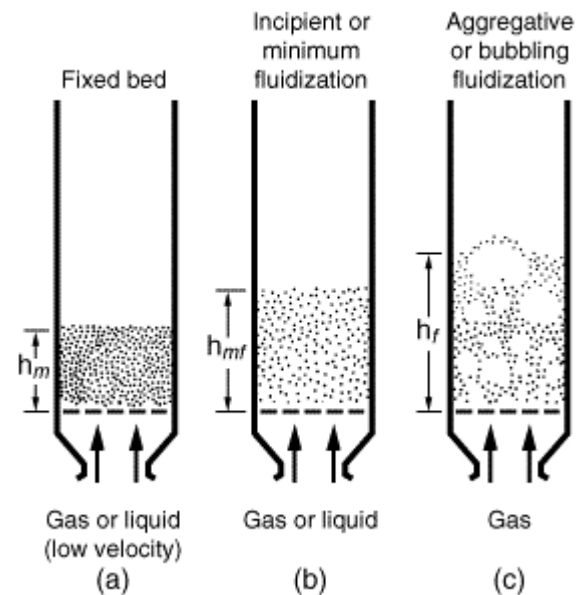


*Adapted from Sun & Grace (1990)*



## Implication of $U_{mb}/U_{mf}$

- $U_{mb}/U_{mf}$  could be used as an important index for the fluidization performance of fine particle fluidized beds on local hydrodynamics
- Geldart particle classification:
  - Group A powders  
with  $U_{mb}/U_{mf} > 1$
  - Group B powders  
with  $U_{mb}/U_{mf} = 1$



# Demarcation

## Demarcation between Group A and B powders

$$\frac{U_{mb}}{U_{mf}} \geq 1 \quad U_{mb} = K d_p$$

For air at room T and P,  $K = 100$  (Yang, W.-C., 2003)

$$\frac{8 \times 10^{-4} g d_p (\rho_p - \rho)}{K \mu} \leq 1$$

Pressure and temperature effect: (Grace, 1986)

$$(d_p^*)_{AB} = 101 \left( \frac{\rho_p - \rho}{\rho} \right)^{-0.425}$$

If :  $(d_p^*) < (d_p^*)_{AB} \rightarrow$  powder belongs to Group A or C  
If :  $(d_p^*) > (d_p^*)_{AB} \rightarrow$  powder belongs to Group B or D

## Demarcation between Group B and D powders

For Group D powders  $U_B \leq \frac{U_{mf}}{\varepsilon_{mf}}$

# Demarcation

Demarcation between Group C and A powders (Molerus, 1982)

$$10(\rho_p - \rho_f)d_p^3 g / F_H = 0.01$$

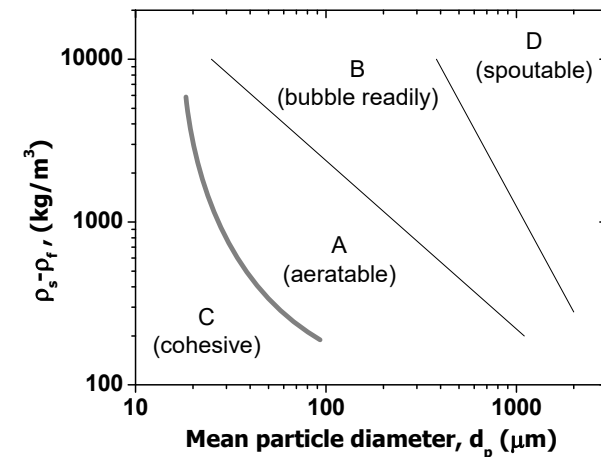
$F_H$  is the adhesion force determined experimentally.  
( $F_H=8.76 \times 10^{-8}$  N for glass beads and FCC catalysts)

Demarcation between Group A and B powders

$$\frac{U_{mb}}{U_{mf}} \geq 1$$

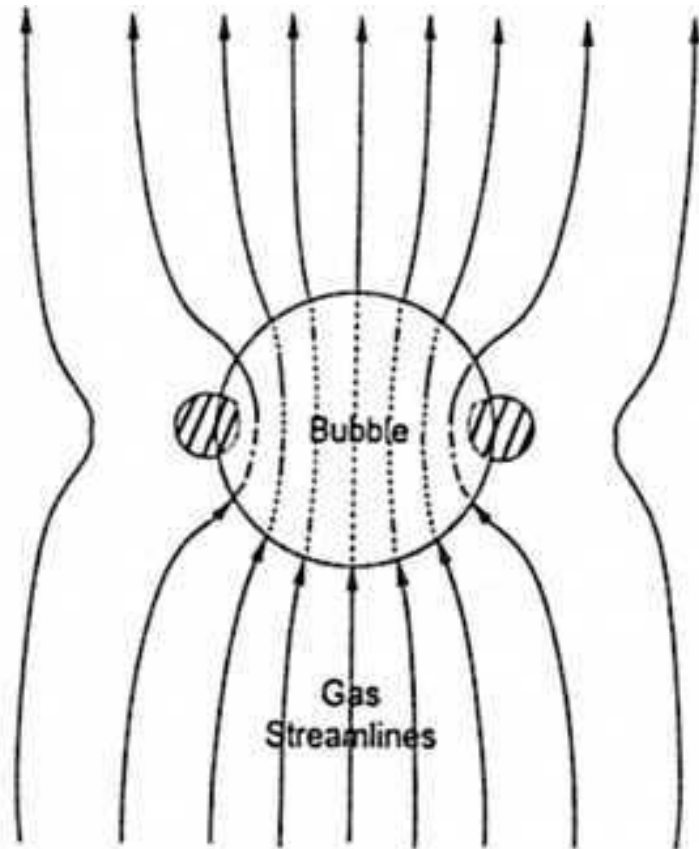
Demarcation between Group B and D powders

For Group D powders  $U_B \leq \frac{U_{mf}}{\epsilon_{mf}}$



# Characteristics of single bubble: Slow vs. fast bubbles (Davidson model)

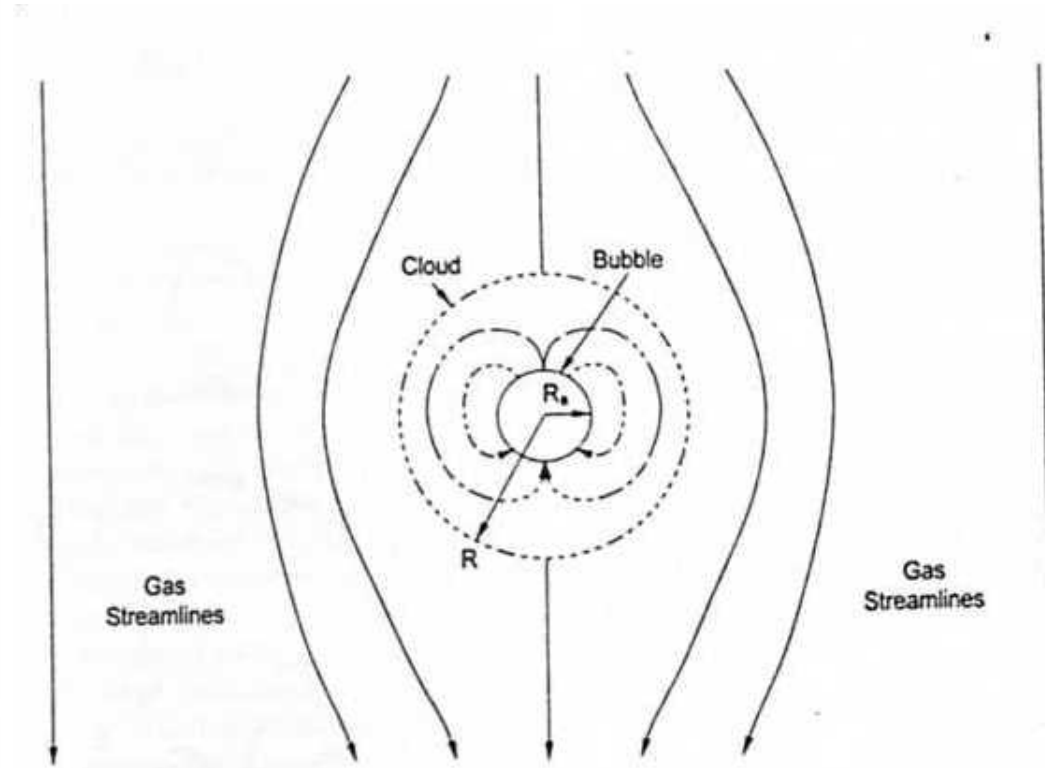
## slow bubble



Slow Bubbles  $U_B < U_{mf} / E_{mf}$

group D

## fast bubble



Fast Bubbles  $U_B > U_{mf} / E_{mf}$

group A & B



## Simple demarcation criteria accounting for T, P effects

Goosen's classification:

- C/A boundary:  $Ar=9.8$
- A/B boundary:  
 $Ar=88.5$
- B/D boundary:  
 $Ar=176,900$

Grace's classification:

- A/B boundary:  $Ar=125$
- B/D boundary:  
 $Ar=145,000$

$$Ar = \frac{g\rho_g(\rho_p - \rho_g)d_p^3}{\mu^2}$$

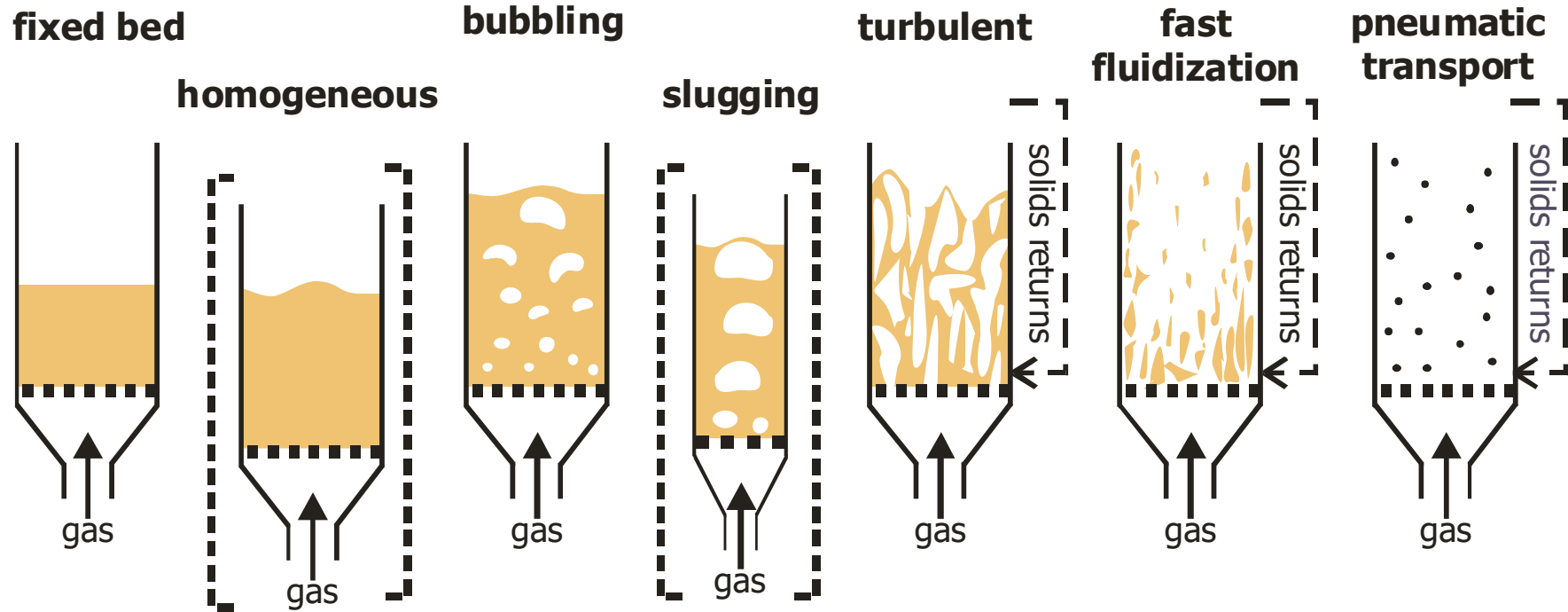
## Correlations for $U_{mb}$

Abrahamsen and Geldart (1980)

$$\frac{U_{mb}}{U_{mf}} = \frac{2300 \rho_g^{0.126} \mu_g^{0.523} \exp(0.716 F_{45})}{d_p^{0.8} g^{0.934} (\rho_p - \rho_g)^{0.934}}$$

Where  $F_{45}$  is the fraction of solids which are less than  $45\mu\text{m}$ .

# Flow Regimes



only A powders  
at low gas velocity

only narrow beds

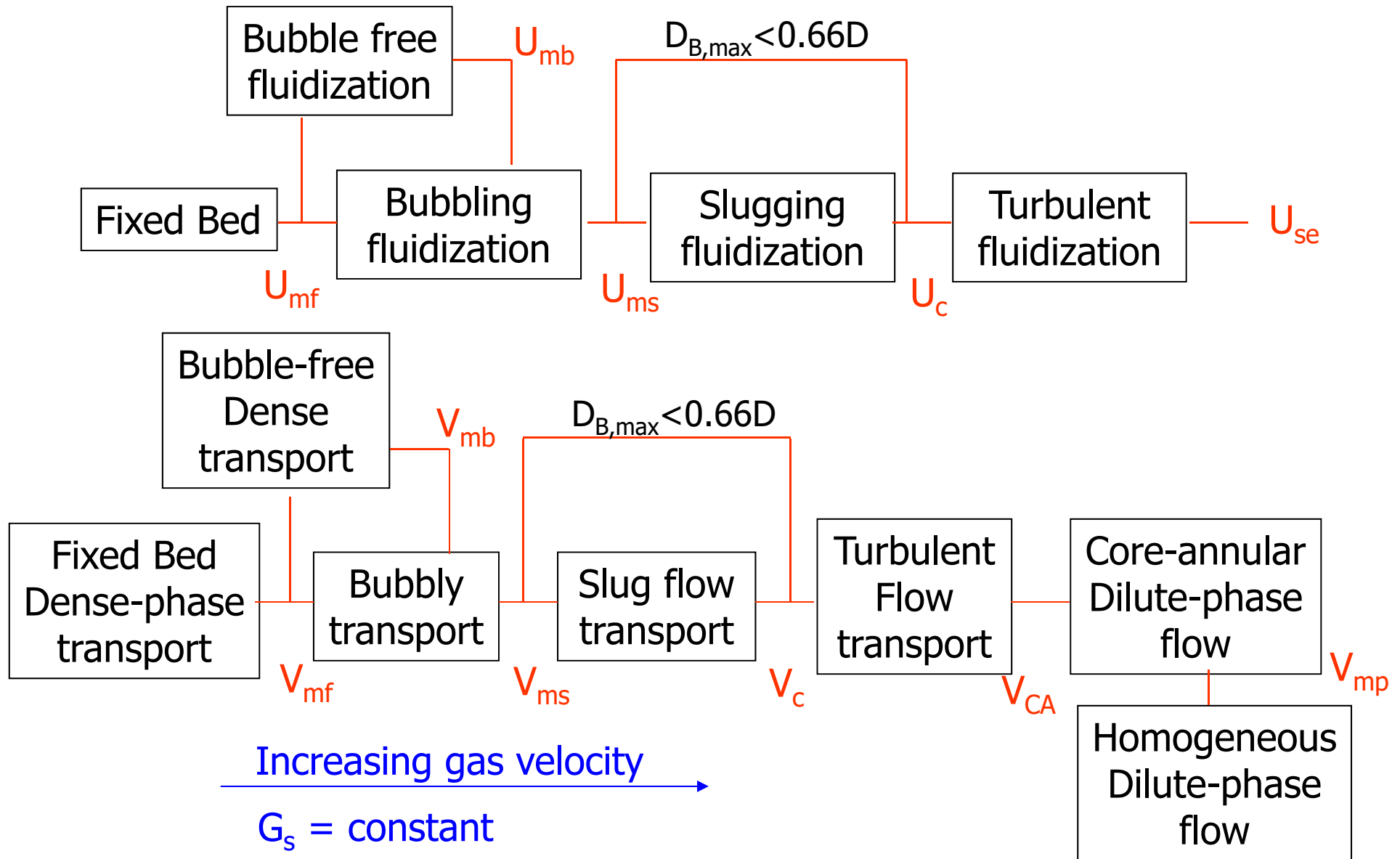


gas velocity

# Flow Regimes

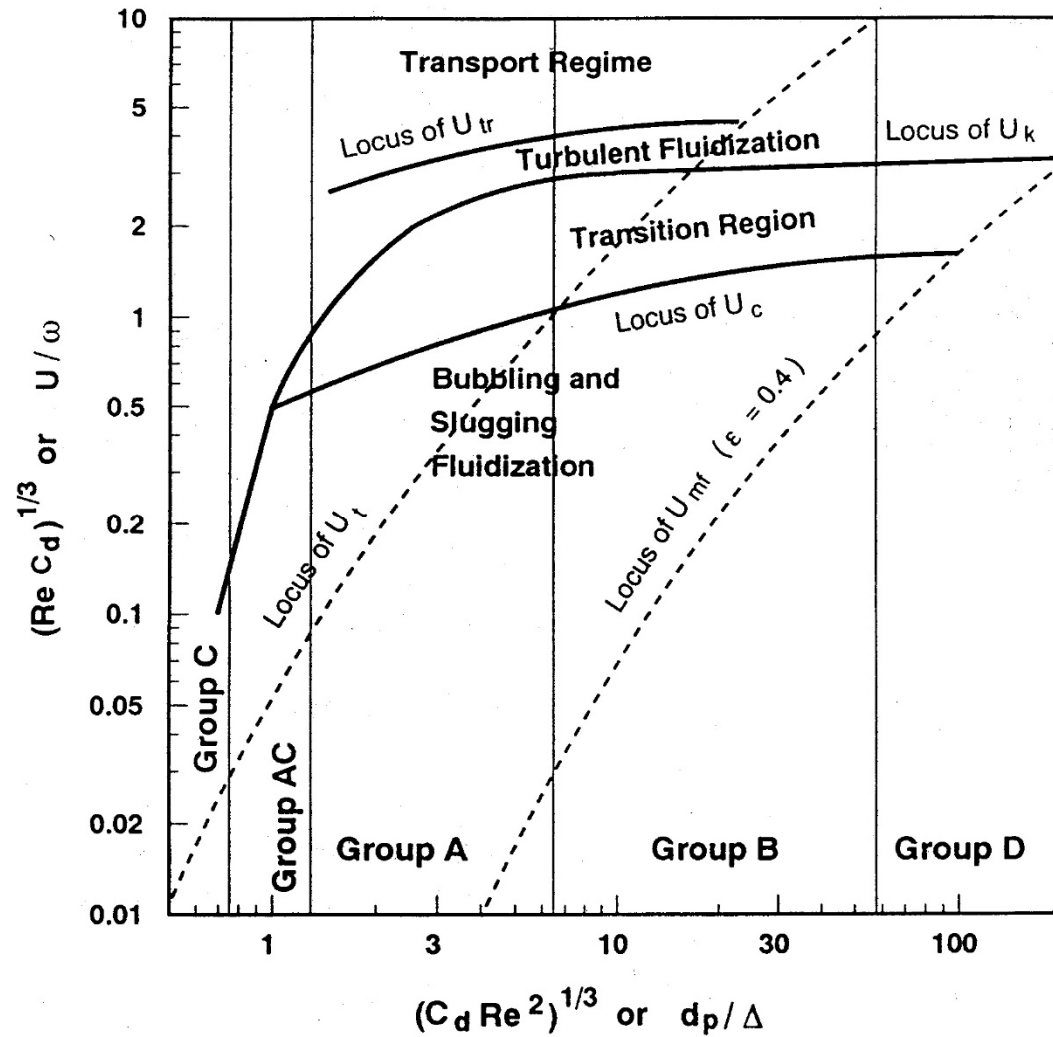
<b>U range</b>	<b>Regime</b>	<b>Appearance and Principal Features</b>
$0 \leq U < U_{mf}$	Fixed Bed	Particles are quiescent; gas flows through interstices
$U_{mf} \leq U < U_{mb}$	Particulate regime	Bed expands smoothly in a homogeneous manner; top surface well defined, small-scale particle motion
$U_{mb} \leq U < U_{ms}$	Bubbling regime	Gas voids form near distributor, coalesce and grow; rise to surface and break through
$U_{ms} \leq U < U_c$	Slug flow regime	Bubble size approaches column cross-section. Top surface rises and collapses with regular frequency.
$U_c \leq U < U_k$	Turbulent fluidization flow regime	Pressure fluctuations gradually decrease until turbulent fluidization flow regime is reached.
$U_k \leq U < U_{tr}$	(Turbulent Regime)	Small gas voids and particle clusters dart to and fro. Top surface is difficult to distinguish.
$U \geq U_{tr}$	Fast Fluidization	No upper surface to bed, particles transported out the top in clusters and must be replaced.
$U \gg U_{tr}$	Pneumatic conveying	No bed. All particles fed in are transported out the top as a lean phase.

# Regime Transition Flow Chart

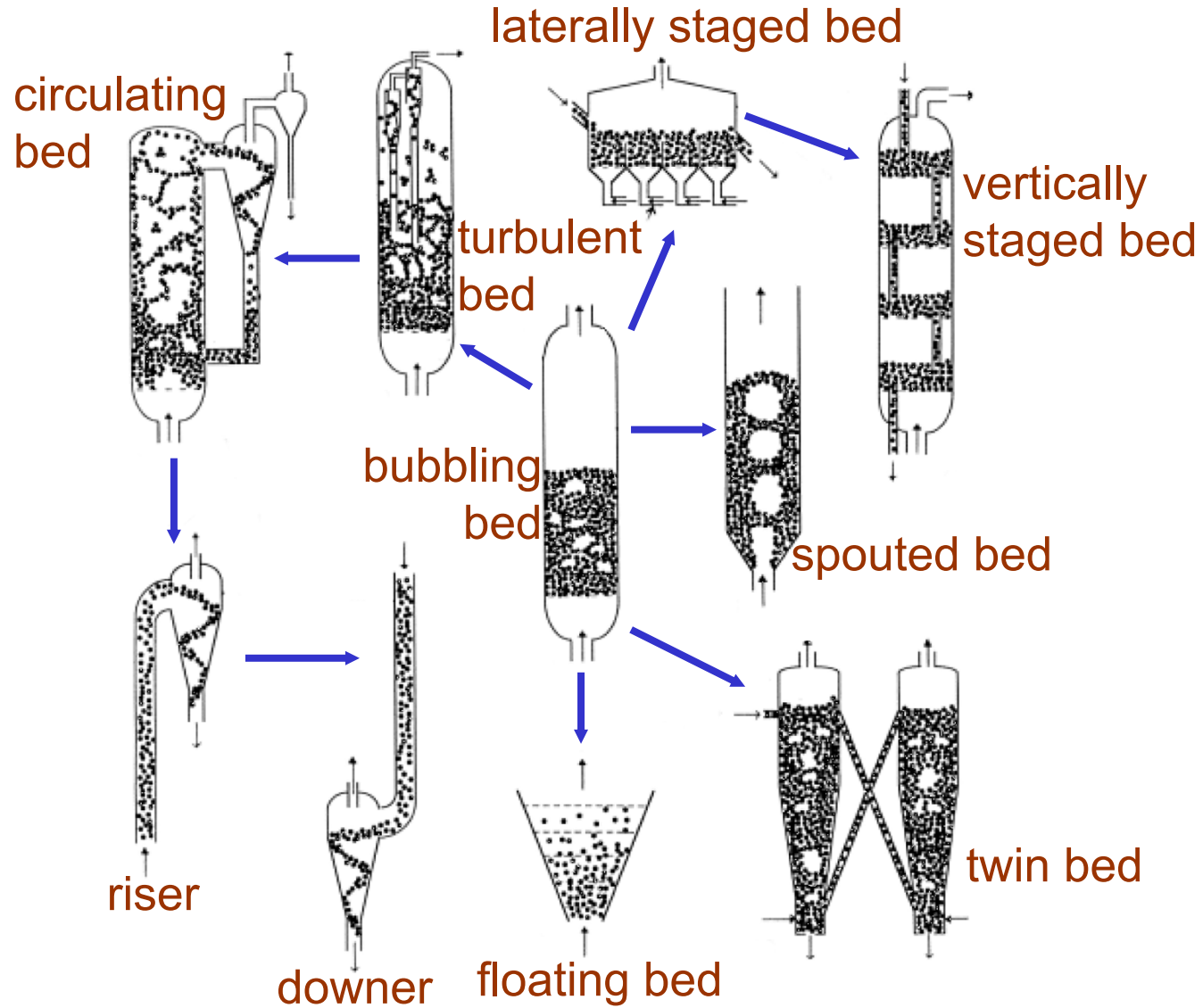


Bi & Grace, 1995

# Unifying Fluidization Regime Diagram

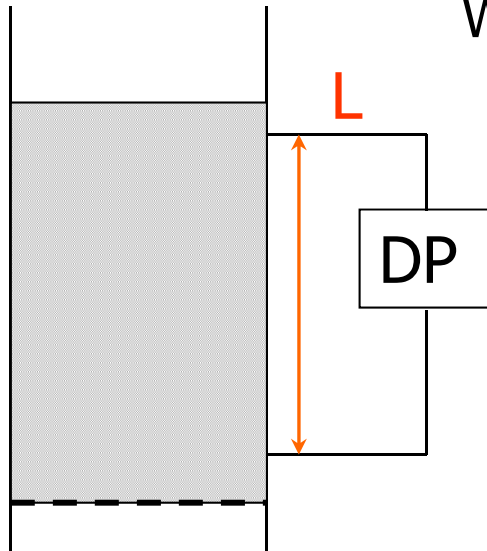


# Fluidized bed lay-out



# Static Head of Solids

When acceleration, friction and gas head are negligible



$$\Delta P = \frac{\text{weight of particles} - \text{upthrust on particles}}{\text{bed cross-sectional area}}$$

$$\frac{\Delta P}{L} = (1 - \varepsilon)(\rho_p - \rho)g$$

## Time-averaged pressure measurements

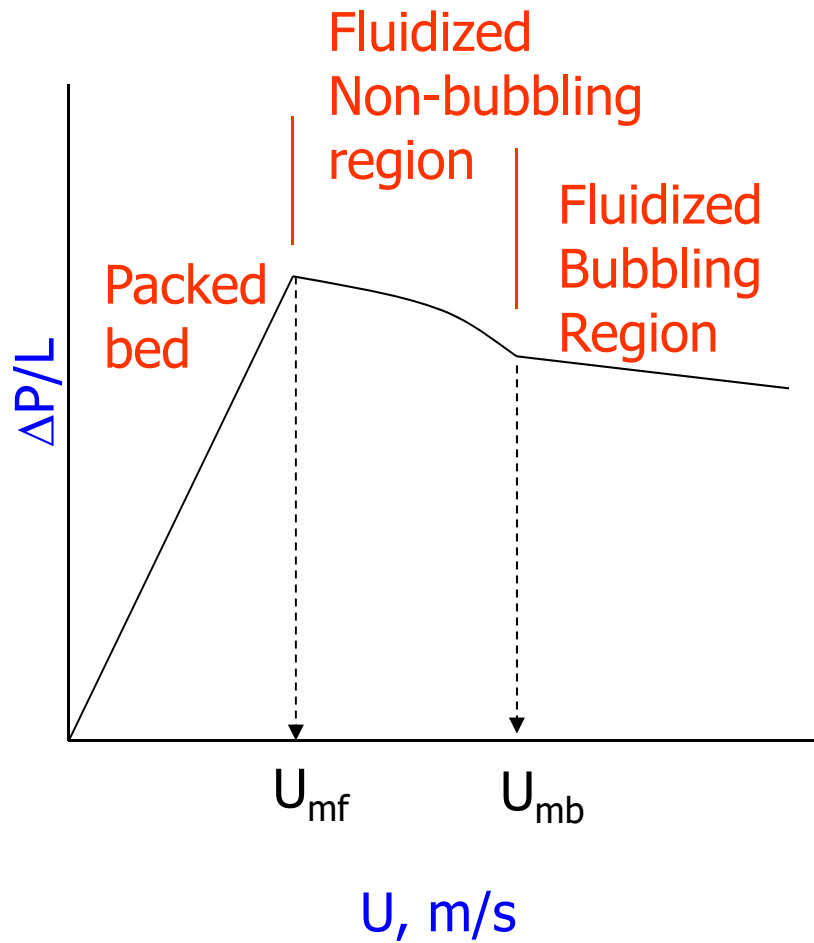
- Most industrial and pilot plant fluidized beds have pressure taps.
- There should be at least 2 or 3 taps within the fluidized bed.
- Pressure measurement from plenum chamber must be from where it will not be affected by either the gas expansion or the contraction
- For hot units, back flushed taps are often used.  
(gas flowrate must be regulated)

For other measurement techniques in fluidized beds:  
van Ommen & Mudde, Int J Chem Reactor Eng 6 (2008) R3

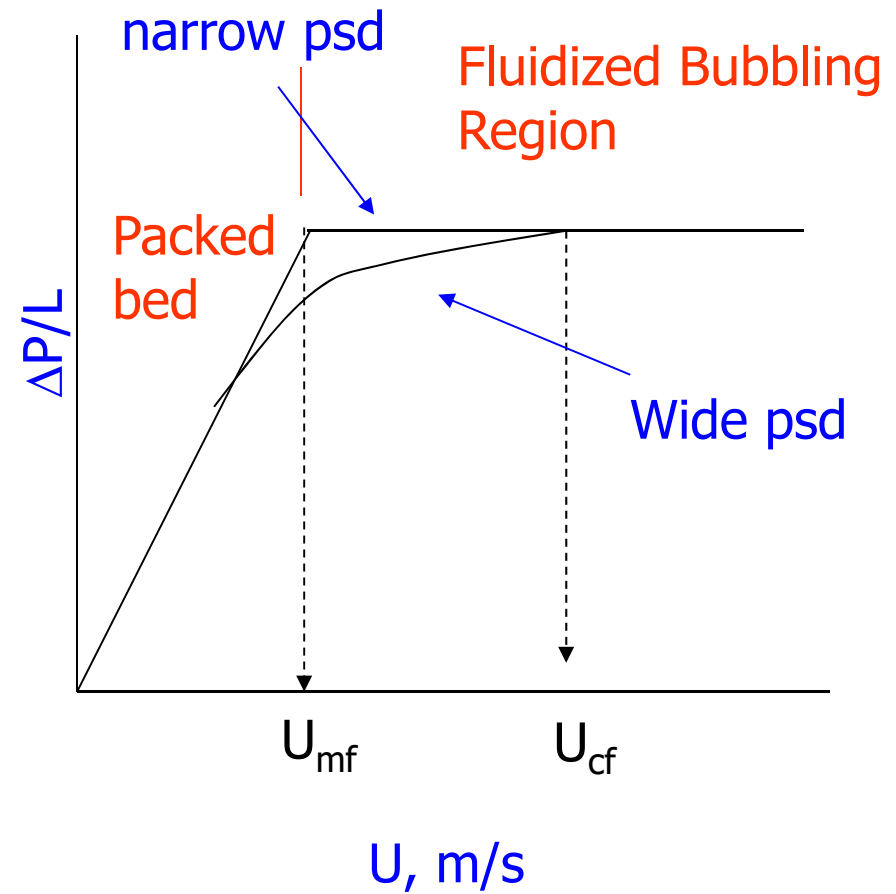


# Fluidization Curve

## Group A particles



## Group B particles



## Minimum Fluidization

The frictional pressure drop at the point of minimum fluidization equalizes the bed mass per unit of cross-sectional area.

$$\begin{aligned} -\Delta P_{\text{friction}} &= 150 \frac{U_{\text{mf}} \mu (1 - \varepsilon_{\text{mf}})^2 \Delta x_{\text{mf}}}{D_{\text{sv}}^2 \varepsilon_{\text{mf}}^3} + 1.75 \frac{U_{\text{mf}}^2 \rho (1 - \varepsilon_{\text{mf}}) \Delta x_{\text{mf}}}{D_{\text{sv}} \varepsilon_{\text{mf}}^3} \\ &= g \Delta x_{\text{mf}} (\rho_p - \rho) (1 - \varepsilon_{\text{mf}}) \end{aligned}$$

The frictional pressure drop at the point of minimum fluidization ( $U_{\text{mf}}, \varepsilon_{\text{mf}}, \Delta x_{\text{mf}}$ ), can be considered equal to the frictional pressure drop in a fixed bed (Ergun)

## Minimum Fluidization Velocity ( $U_{mf}$ )

Dimensionless relationship following from equation on previous slide

$$Re_{mf} = \sqrt{C_1^2 + C_2 Ar} - C_1$$

$$Re_{mf} = U_{mf} \rho D_{sv} / \mu$$

$$Ar = g \rho (\rho_p - \rho) D_{sv}^3 / \mu^2$$

$$C_1 = 300 (1 - \varepsilon_{mf}) / 7$$

$$C_2 = \varepsilon_{mf}^3 / 1.75$$

# Minimum Fluidization

## Estimation of $\varepsilon_{mf}$

$$0.4 < \varepsilon_{mf} < 0.55$$

- $\varepsilon_{mf} \approx \varepsilon_{\text{fixed bed}}$
- $\varepsilon_{mf} \approx (14 \phi)^{-1/3}$  where  $\phi$  is the particle sphericity

Authors	$C_1$	$C_2$
Wen and Yu (1966)	33.7	0.0408
Richardson (1971)	25.7	0.0365
Saxena and Vogel (1977)	25.28	0.0571
Babu et al. (1978)	25.25	0.0651
Grace (1982)	27.2	0.0408
Chitester et al. (1984)	28.7	0.0494

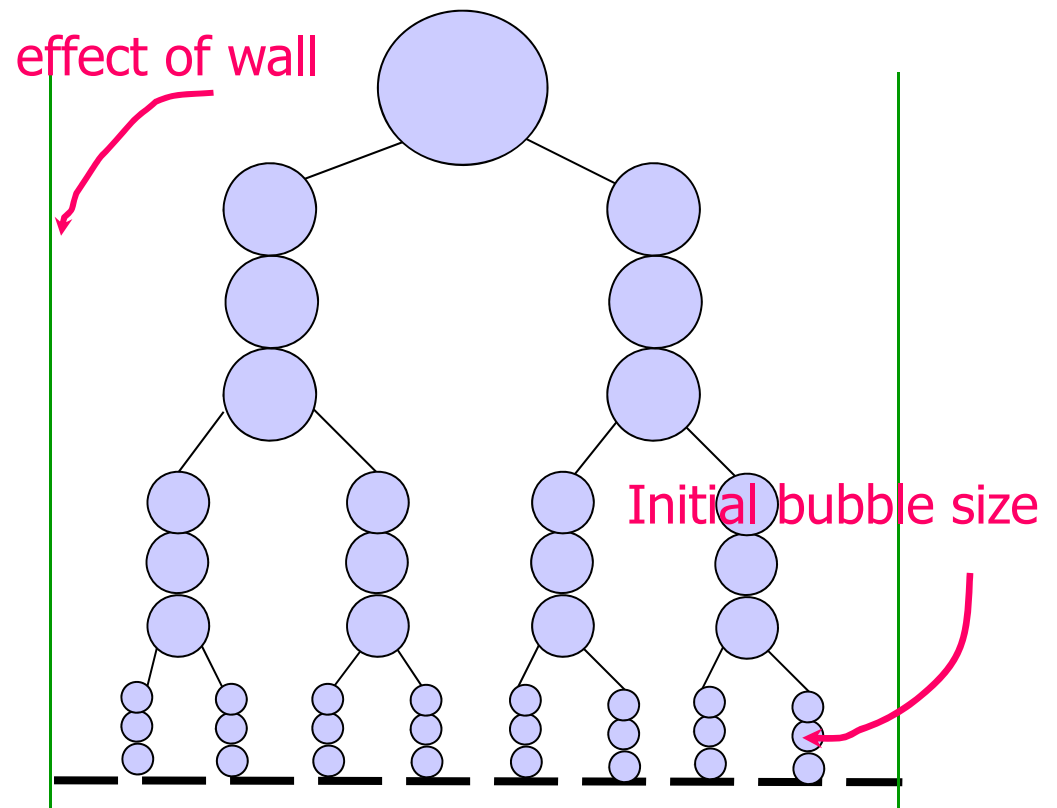
# Freely Bubbling Beds: Bubble Growth



## Why grow?

- 1) The hydrostatic pressure on the bubbles decreases as they rise up the bed;
- 2) Bubbles may coalesce by one bubble catching up with another;
- 3) Bubbles which are side by side may coalesce;
- 4) Bubbles may grow by depleting the continuous phase locally.

Mean bubble size =  
 $f(\text{type of distributor, distance above the distributor plate, excess gas velocity})$



# Freely Bubbling Beds: Bubble Size

Darton et al. (1977) 
$$D_b(z) = 0.54 g^{-0.2} (U - U_{mf})^{0.4} \left( z + 4 \sqrt{\frac{A}{N_{or}}} \right)^{0.8}$$

where  $A/N_{or}$  is the area of distributor plate per orifice

Mori & Wen (1975)

$$\frac{D_{be} - D_b}{D_{be} - D_{b0}} = \exp\left(-0.3 \frac{z}{D_T}\right)$$

Ranges of key variables:

$$5 \leq U_{mf} \leq 200 \text{ mm/s}$$

$$60 \leq d_p \leq 450 \mu\text{m}$$

$$U - U_{mf} \leq 0.48 \text{ m/s}$$

$$D_T \leq 1.3 \text{ m}$$

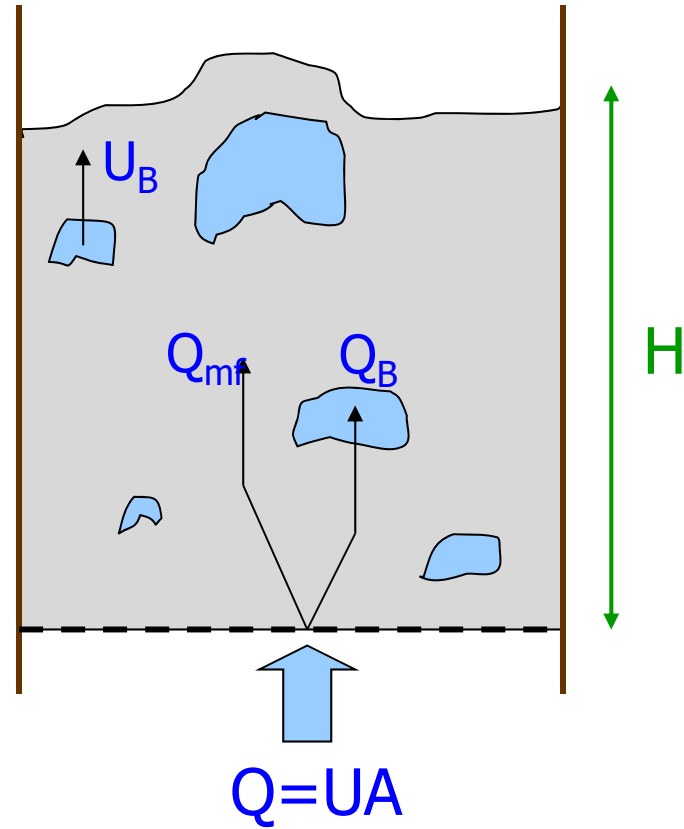
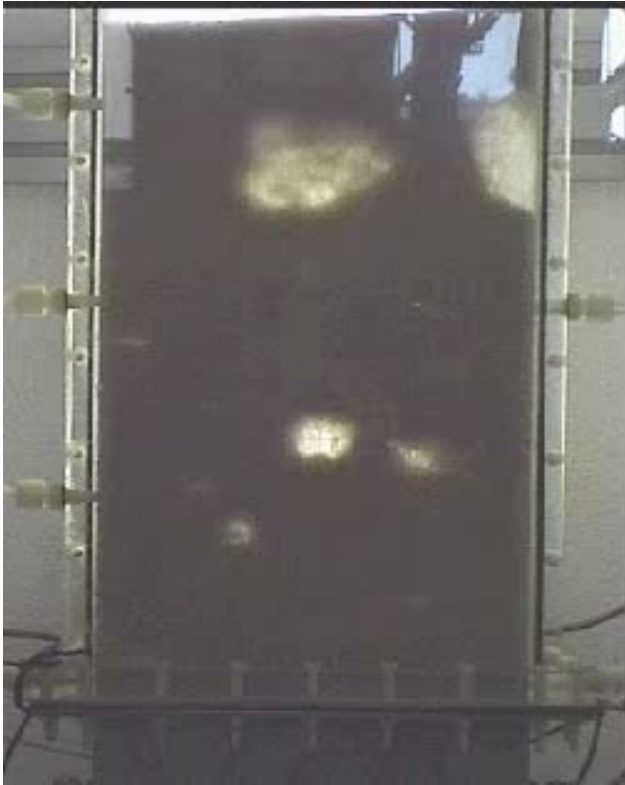
where:

$$D_{b0} = \frac{1.38}{g^{0.2}} \left[ \frac{A}{N_{or}} (U - U_{mf}) \right]^{0.4} \quad \text{for perforated plates}$$

$$D_{b0} = 0.376 (U - U_{mf})^2 \quad \text{for porous plates}$$

$$D_{be} = 1.64 \left[ A (U - U_{mf}) \right]^{0.4}$$

# Two-phase theory



# Two-phase theory

Total gas flow rate:  $Q = UA$

Flow rate in dense phase:  $Q_{mf} = U_{mf} A$

Gas passing through the bed as bubbles:  $Q - Q_{mf} = (U - U_{mf})A$

Fraction of the bed occupied by bubbles:  $\delta_b = \frac{H - H_{mf}}{H} = \frac{Q - Q_{mf}}{AU_B} = \frac{U - U_{mf}}{U_B}$

The distribution of the gas between the bubbles and dense phase is of interest because it influences the degree of chemical conversion.

In practice, the two-phase theory overestimates the volume of gas passing through the bed as bubbles

$$\frac{Q_B}{A} = Y(U - U_{mf})$$

Visible bubble flow rate:

where  $0.8 < Y < 1.0$  for Group A powders

where  $0.6 < Y < 0.8$  for Group B powders

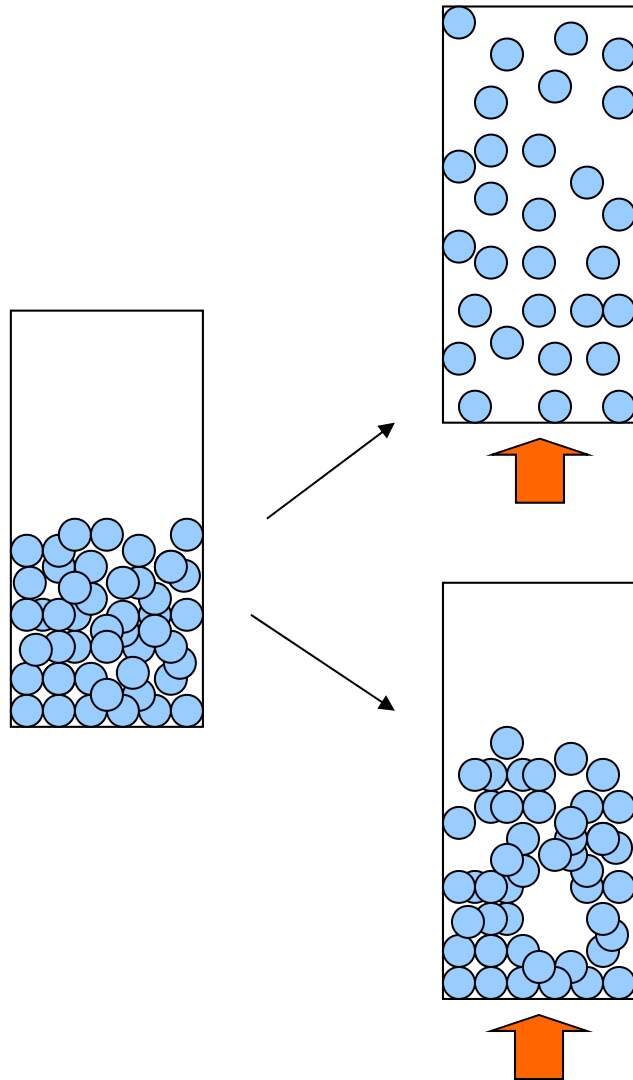
where  $0.25 < Y < 0.6$  for Group D powders

Baeyens and Geldart (1985)

$$Y = 2.27 Ar^{-0.21}$$



# Homogeneous fluidization



Non-bubbling fluidization  
Particulate or homogeneous fluidization

Mechanism???

Delay caused in the adjustment of the mean particle velocity to a change in the local concentration resulting from the larger particle to fluid phase inertia (Didwania, 2001)

Bubbling fluidization  
Aggregative or heterogeneous fluidization

# Steady-state expansion of fluidized beds

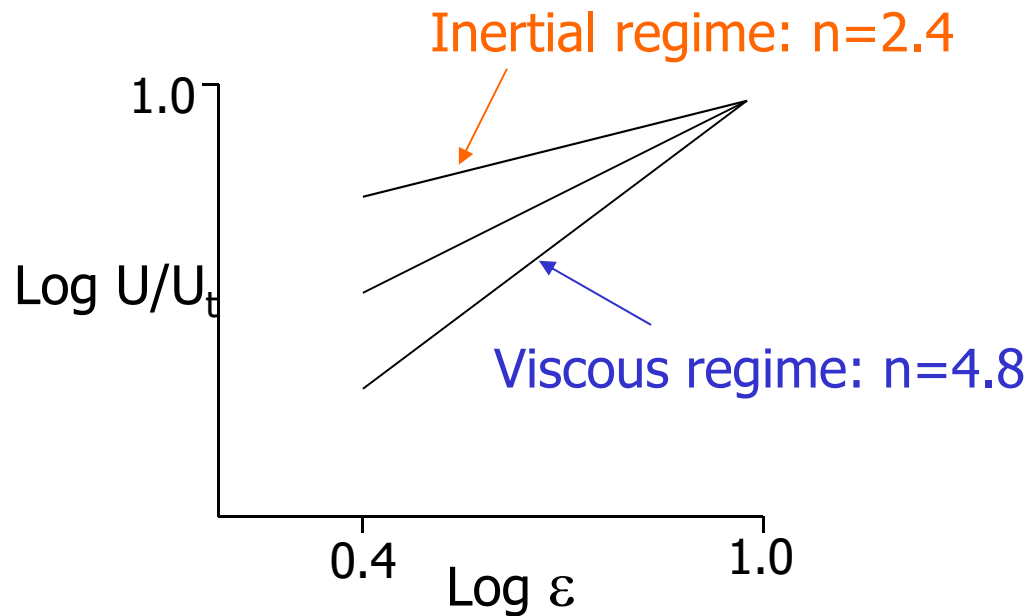
$$V_B = L_B (1 - \varepsilon) A$$

$$\Delta P_B = (\rho_p - \rho_g) V_B g = \text{constant}$$

$V_B$ : total volume of particles

Homogeneous bed expansion: Richardson-Zaki relation

$$\frac{U}{U_t} = \varepsilon^n$$



mass of particles in the bed :

$$M_B = (1 - \varepsilon) \rho_p A H$$

$$H_2 = \frac{(1 - \varepsilon_1)}{(1 - \varepsilon_2)} H_1$$

# Heat and mass transfer

Heat transfer: particle to wall or internal

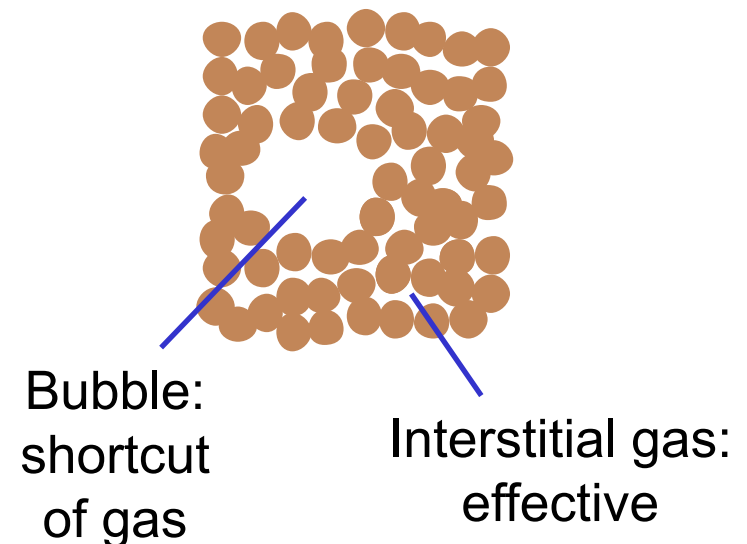
Mass transfer: gas to particle

Fluidized beds show an excellent heat transfer

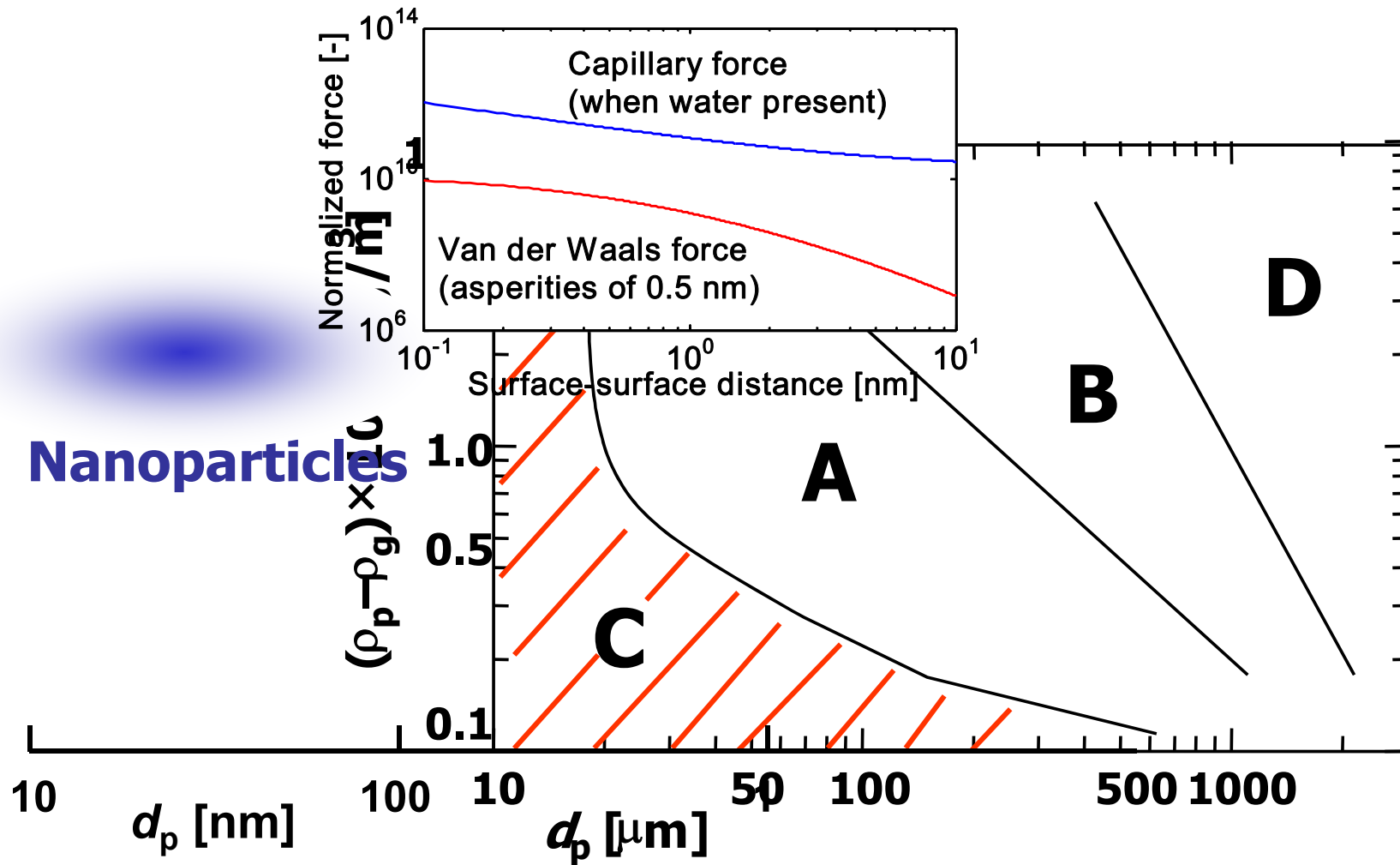
Mixing of solids by (large) bubbles →  
almost constant temperature throughout the reactor

However, large bubbles  
decrease the mass transfer

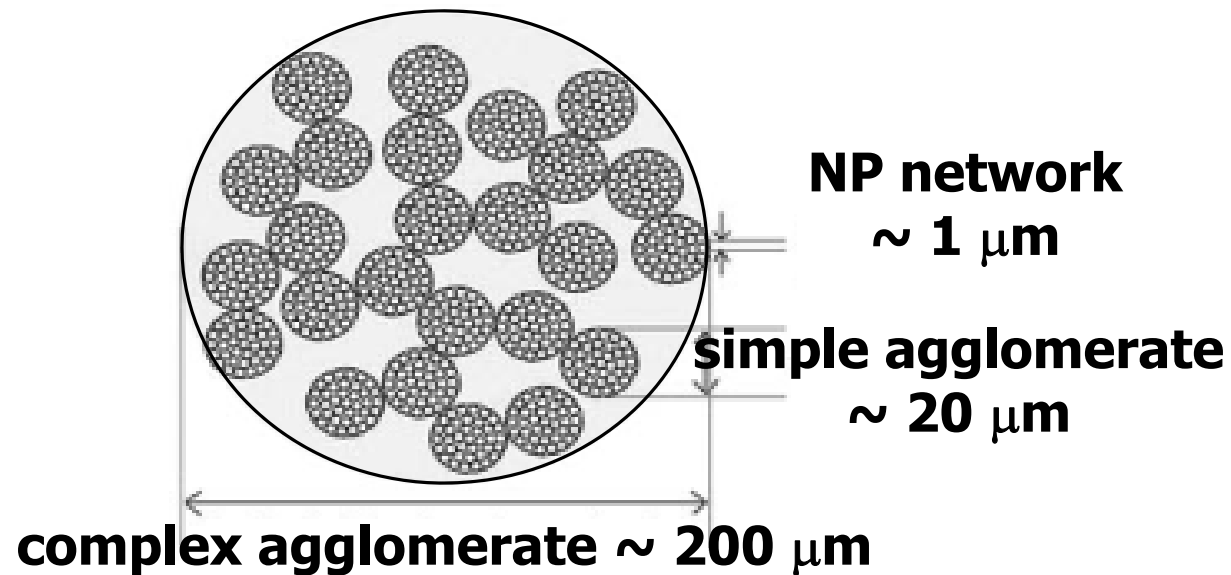
Research → decrease bubble size



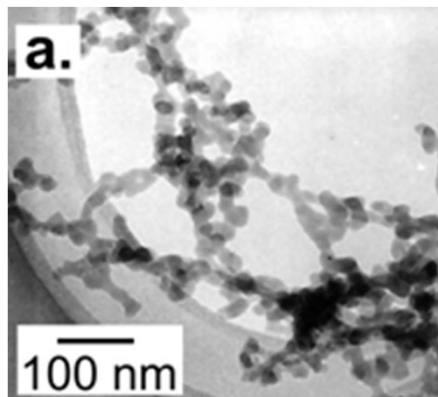
# Geldart's Fluidization Map still valid?



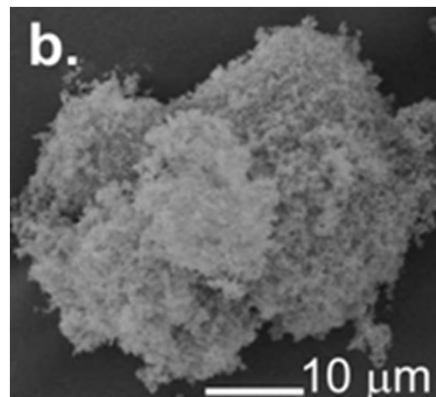
# Nanoparticles are fluidized as agglomerates!



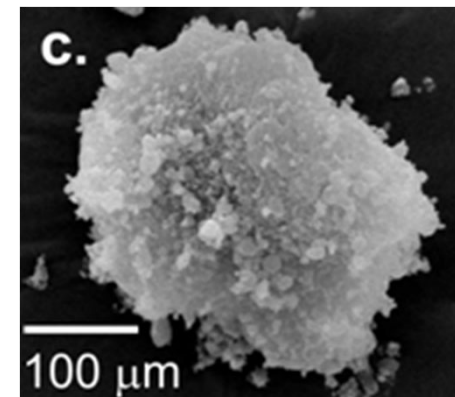
**Wang et al., Powder Technol. 124 (2002) 152:**



TEM NP network



SEM simple agglomerate

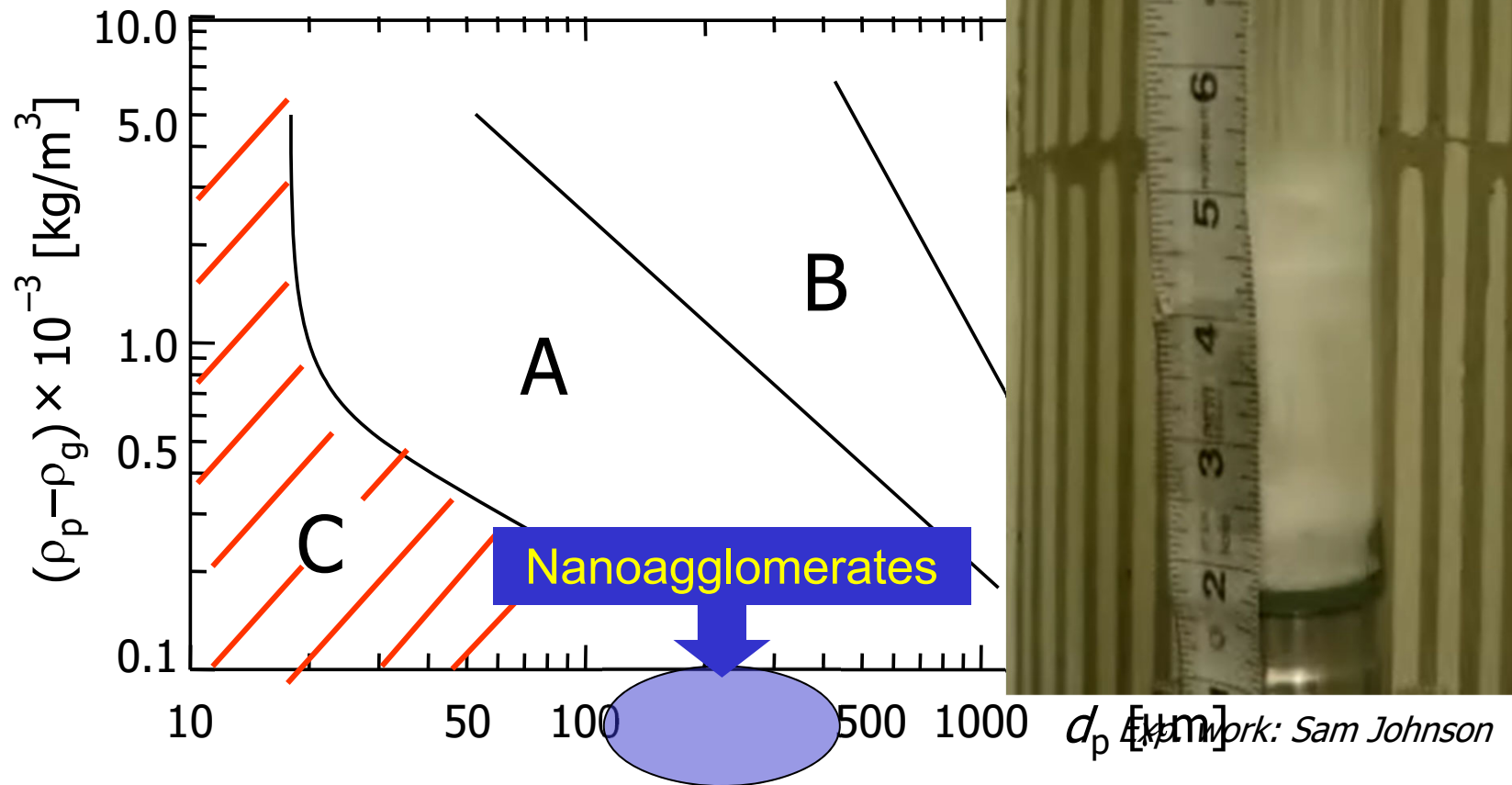


SEM complex agglomerate

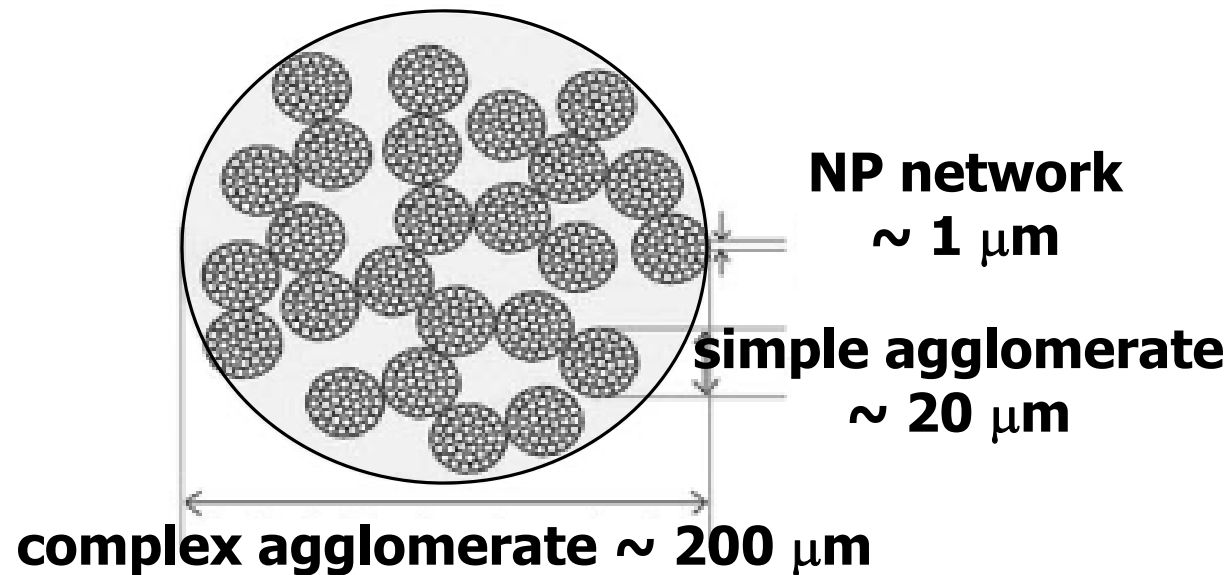
# Geldart's Fluidization Map still valid?

- Primary particle size – 10-100 nm
- Agglomerate size – 100-400  $\mu\text{m}$
- Agglomerate density – 20-120  $\text{kg}/\text{m}^3$

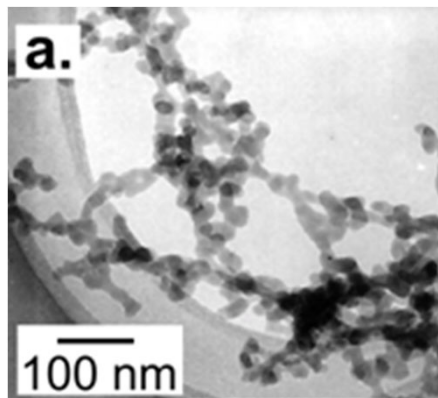
25 nm  $\text{TiO}_2$  particles



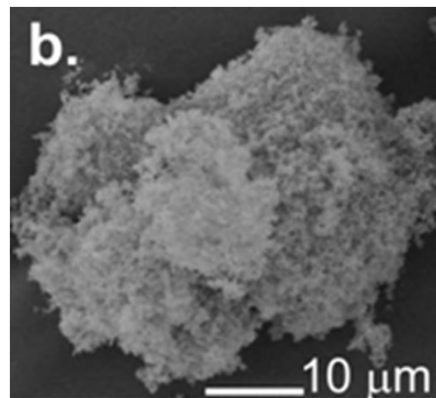
# Nanoparticles are fluidized as agglomerates



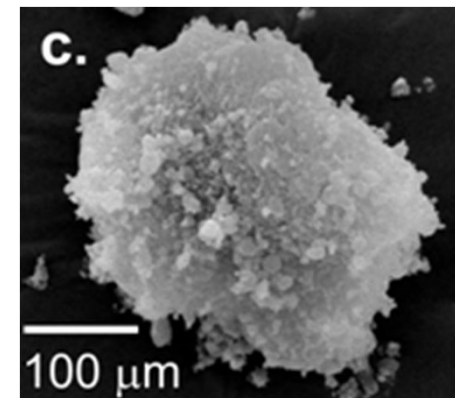
**Wang et al., Powder Technol. 124 (2002) 152:**



**TEM NP network**



**SEM simple agglomerate**



**SEM complex agglomerate**

# In-situ movies of nanoparticle agglomerates

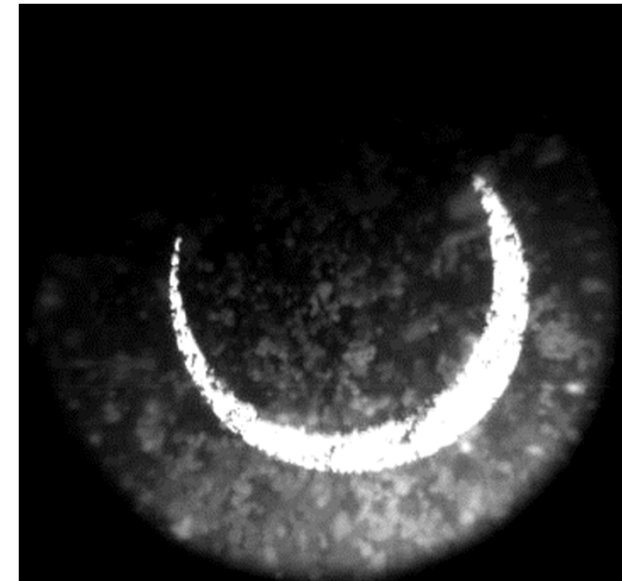
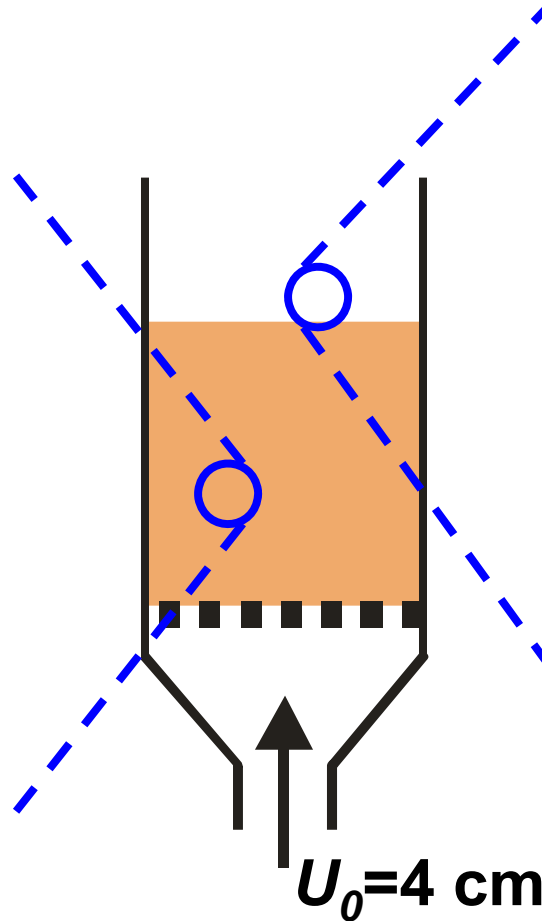
High-speed camera with boroscope, slowed down 70x

Primary particles:

$\text{SiO}_2$ , 10-20 nm diameter

splash zone

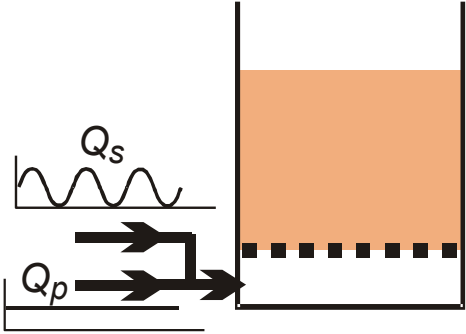
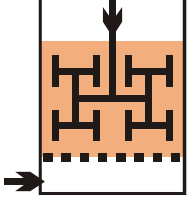
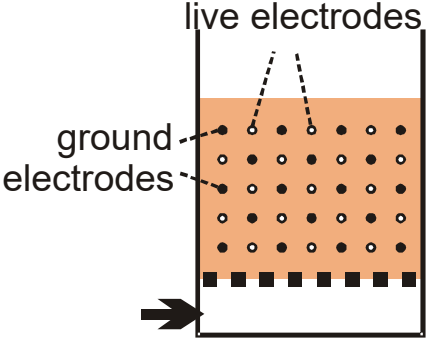
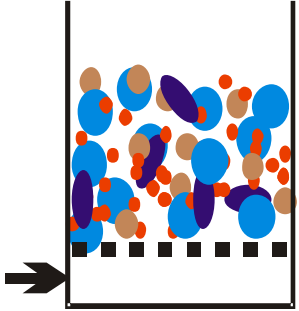
bed



4 mm

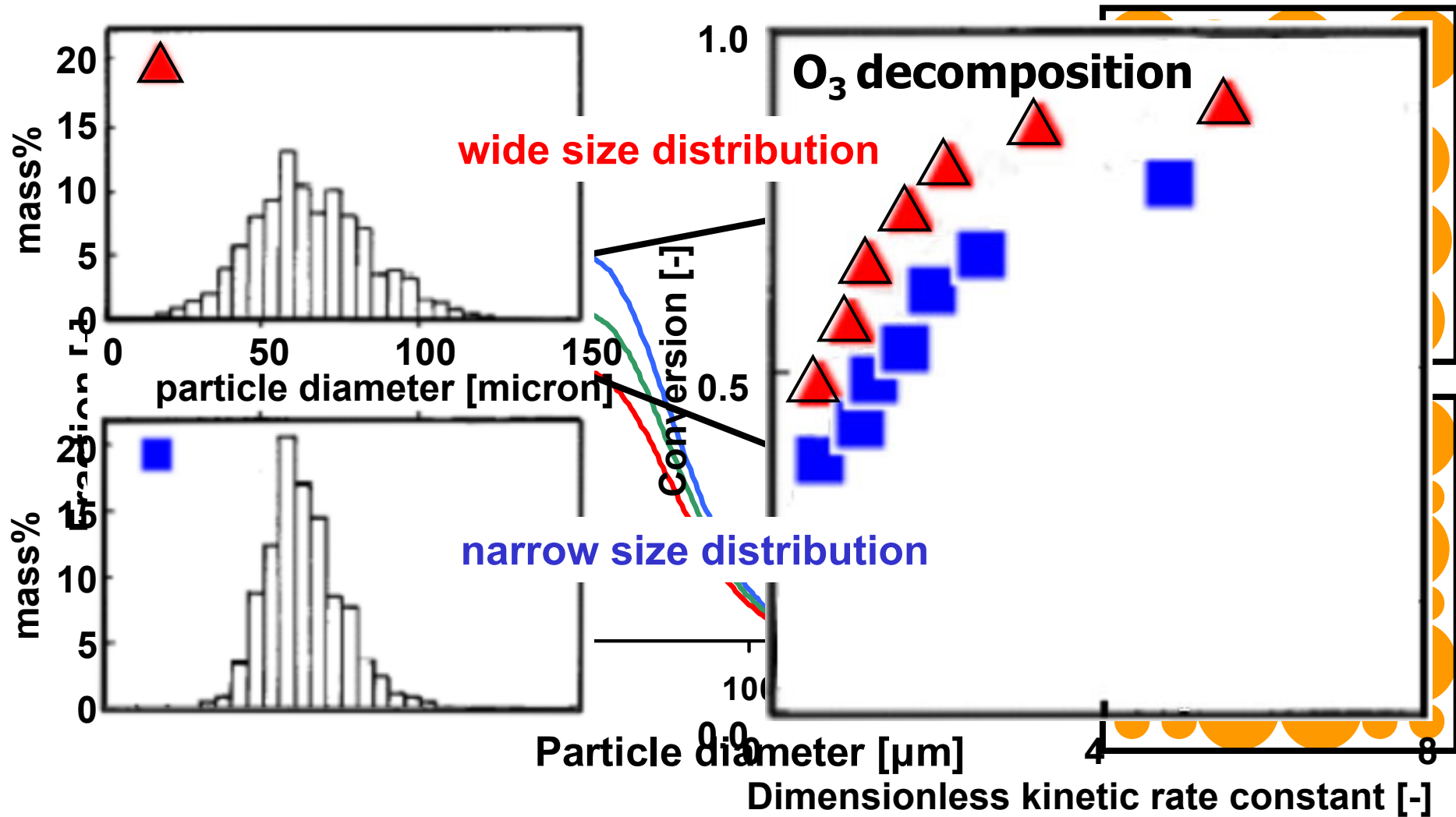


# Ways to structure a fluidized bed

	<b>Dynamics</b>	<b>Geometry</b>
<b>Gas</b>		
<b>Particles</b>		

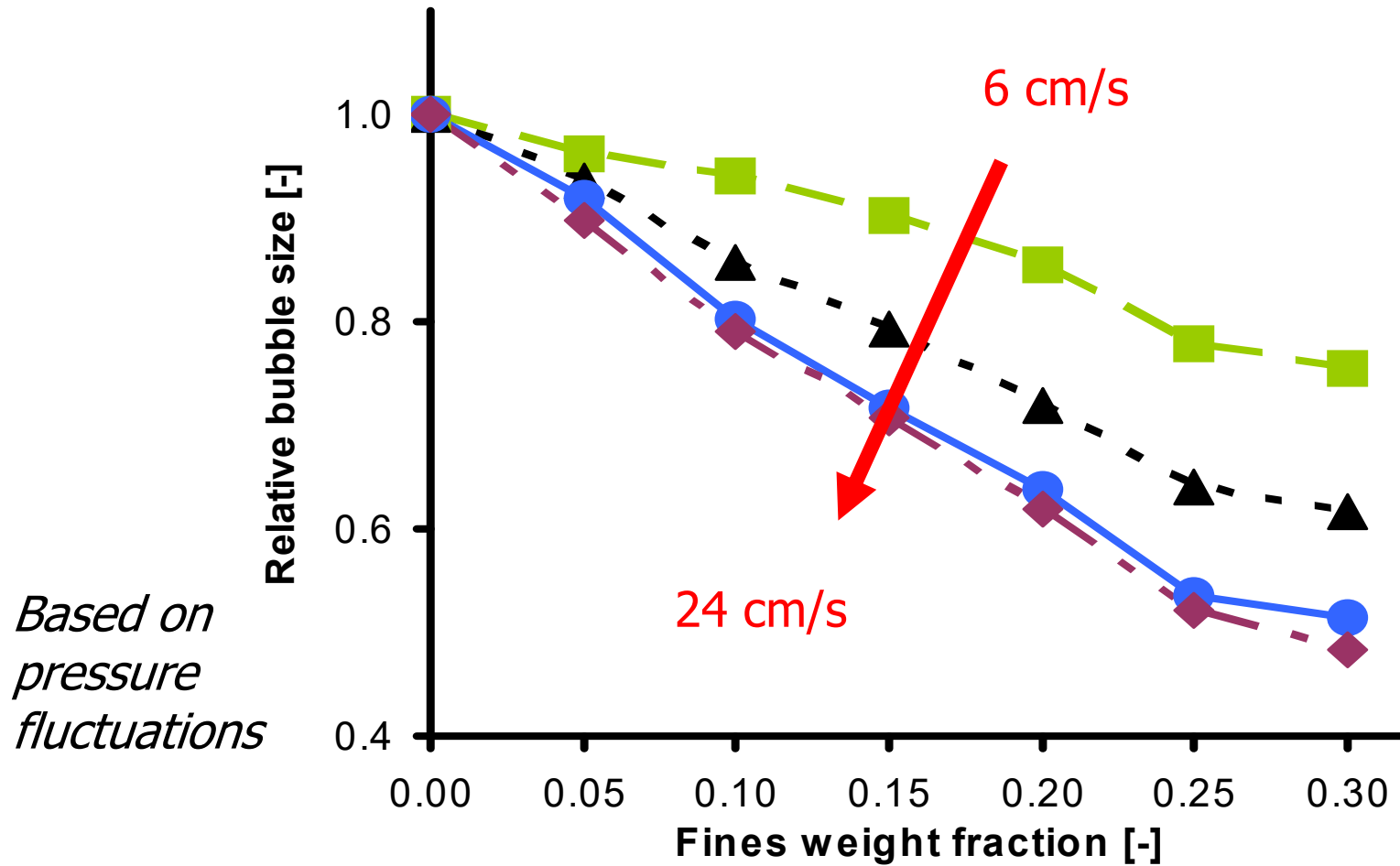
van Ommen *et al.*, *Ind. Eng. Chem. Res.*, 46 (2007) 4236

# Tailoring the particle size distribution

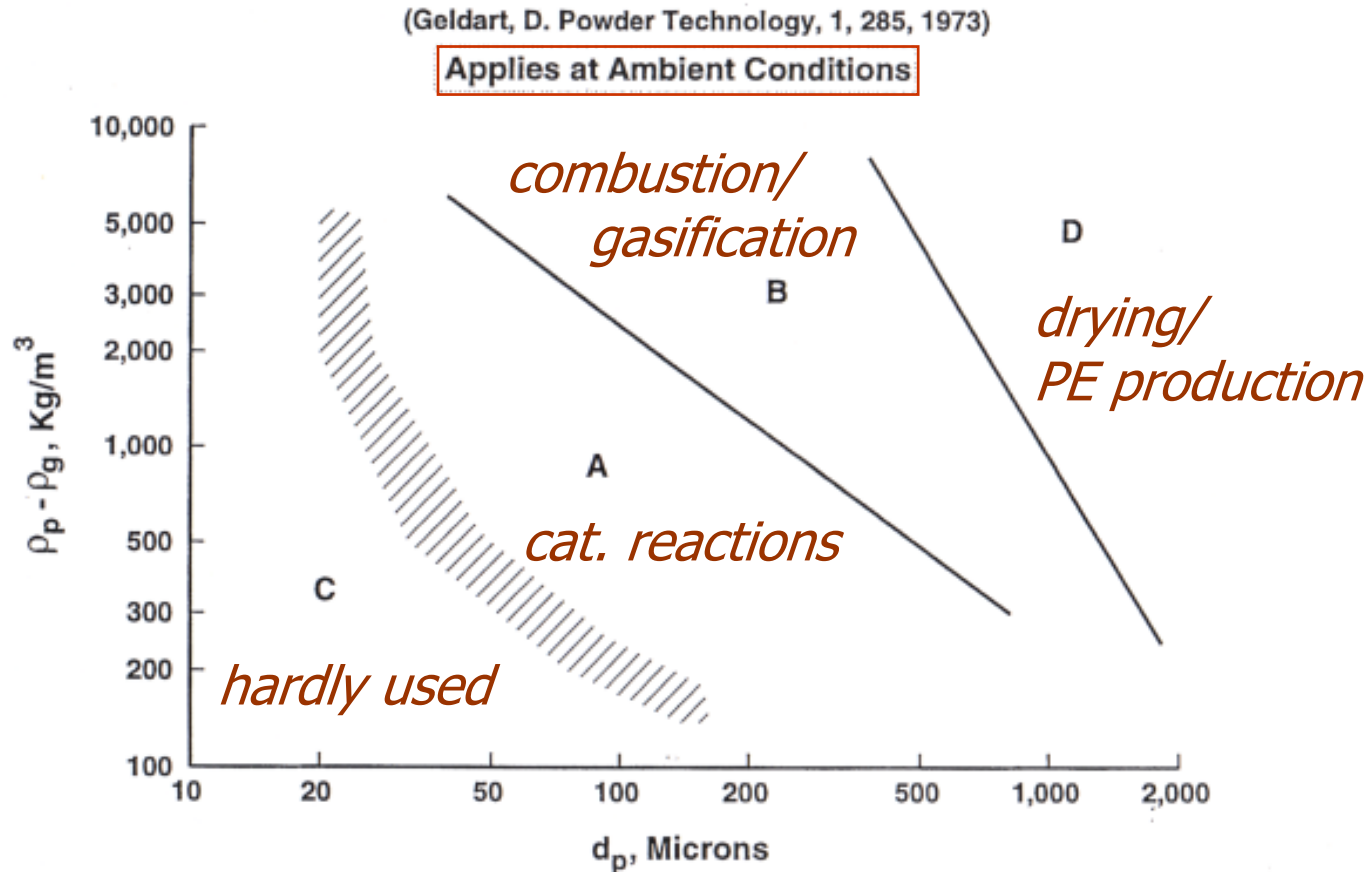


# Fines effect on bubble size

Fines are added to a powder with a  $D_{50}$  of 70  $\mu\text{m}$

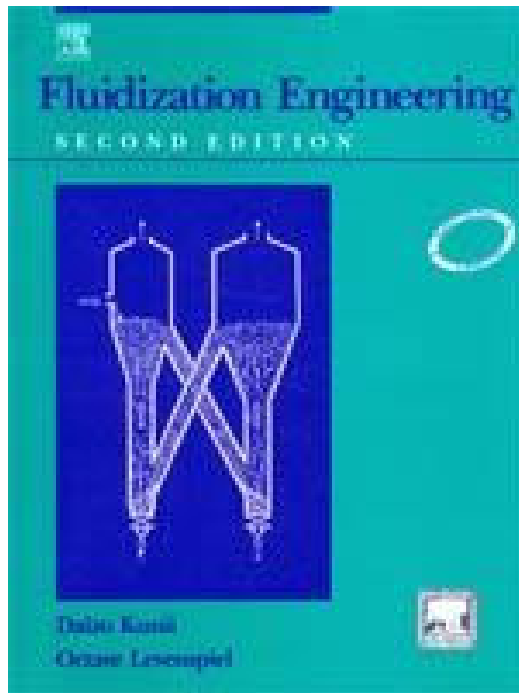


# Geldart's powder classification

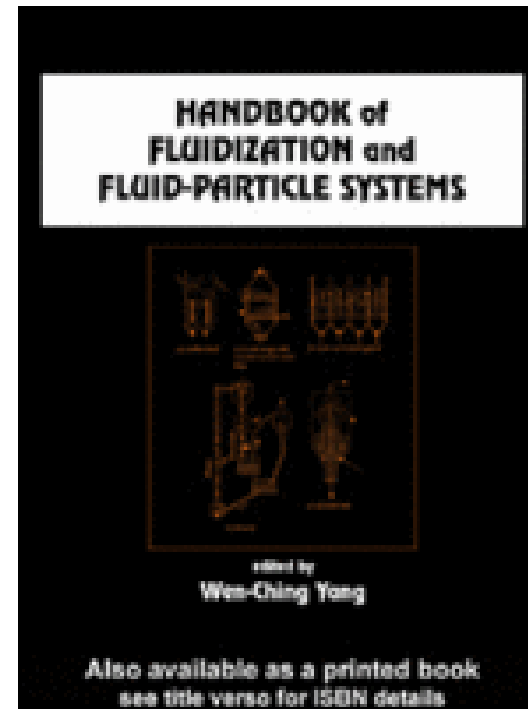


- A: Aeratable ( $U_{mb} > U_{mf}$ ) Material Has a Significant Deaeration Time (*FCC Catalyst*)
- B: Bubbles Above  $U_{mf}$  ( $U_{mb} = U_{mf}$ ) (*500-micron Sand*)
- C: Cohesive (*Flour, Fly Ash*)
- D: Spoutable (*Wheat, 2000-micron Polyethylene Pellets*)

## Textbooks



Fluidization Engineering  
Kunii, D. & Levenspiel, O.  
ISBN: 8131200353  
Pub. Date: Jan 2005 , 2nd ed.  
Publisher: Elsevier



Handbook of Fluidization and Fluid-  
Particle Systems  
Ed. Wen-Ching Yang  
ISBN: 978-0-8247-0259-5  
Pub. Date: March 2003  
Publisher: Routledge, USA

# Course Material

- Additional Resource Material
  - <http://www.erpt.org/>
  - Rhodes, M., Introduction to Particle Technology, Wiley, Sussex England, ISBN: 0471984833, 1999.
  - Yang, W.-C., Marcel Dekker, Handbook of Fluidization and Fluid-particle Systems, New York ISBN: 082470259, 2003.
  - Fan, L.-S., Gas-Liquid-Solid Fluidization Engineering, Butterworth-Heinemann, Boston, 1989.
  - Perry, R.H. and D.W. Green, Perry's Chemical Engineers' Handbook, 7th Ed., McGraw-Hill, New York, 1997.
  - Fan, L.S and C. Zhu, "Principles of gas-solid flows", Cambridge Press, Cambridge, 1998.
  - Grace, J.R., A. Avidan and T.M. Knowlton, "Circulating Fluidized Beds," Blackie Academic press, Boston, 1997.
  - Kunii, D. and O. Levenspiel, "Fluidization Engineering", 2nd edition, Butterworth-Heinemann, Boston, 1991.
  - Geldart, D., "Gas Fluidization Technology", John Wiley & Sons, New York, 1986.

## References

- Rhodes, M., and Zakhari, A., "Laboratory Demonstrations in Particle Technology", CD, Monash University, Melbourne, Australia (1999).
- Geldart, D., "Types of Gas Fluidization", *Powder Tech.*, 7, 285-292 (1973).
- Yang, W.-C., "Bubbling Fluidized Beds", in *Handbook of Fluidization and Fluid-Particle Systems*, Ed. Yang, W.-C., Marcel Dekker, N.Y., pp. 53-111 (2003).
- Ellis, N., "Hydrodynamics of Gas-Solid Turbulent Fluidized Beds", Ph.D. Dissertation, UBC (2003).
- Bi, H.T., and Grace, J.R., "Flow Regime Diagrams for Gas-Solid Fluidization and Upward Transport", *Int. J. Multiphase Flow*, 21, 1229-1236 (1995).
- Grace, J.R., "Contacting Modes and Behaviour Classification of Gas-Solid and Other Two-Phase Suspensions", *Can. J. Chem. Eng.*, 64, 353-363 (1986).
- Gidaspow, D., "Multiphase Flow and Fluidization: Continuum and Kinetic Theory Descriptions", Academic Press, San Diego (1994).
- Kunii, D., and Levenspiel, O., "Fluidization Engineering", Butterworth-Heinemann, Newton, MA (1991).

# References

- Bird, R.B., Stewart, W.E., and Lightfoot, E.N., "Transport Phenomena", John Wiley & Sons, N.Y., Chapter 6: Interphase Transport in Isothermal Systems (2002).
- Wen, C.Y., and Yu, Y.H., "Mechanics of Fluidization", Chem. Eng. Prog. Symp. Series, 62, 100 - 111 (1966).
- Gidapsov, D., and Ettehadieh, B., "Fluidization in Two-Dimensional Beds with a Jet, Part II: Hydrodynamics Modeling", I&EC Fundamentals, 22, 193-201 (1983).
- Didwania, A.K., "A New Instability Mode in Fluidized Beds", Europhysics Letters, 53, 478-482 (2001).
- DallaValle, J.M., "Micromeritics, the technology of fine particles", Pitman Pub., N.Y. (1948).
- McCabe W.L., Smith, J.C., and Harriot P., "Unit operations of Chemical Engineering", McGraw-Hill, New York (1993)
- Rhodes, M., "Introduction to Particle Technology", Wiley, Chichester (1998)
- Grace, J.R., "Fluidized-Bed Hydrodynamics", in *Handbook of Multiphase Systems*, Ed. Hetsroni, G., Hemisphere, Washington, pp., 8:5-64 (1982).