Multiscale wetting phenomena and grains

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Wettability and Spreading?

<u>Wettability</u> is the tendency of one fluid to spread on or adhere to a solid surface in the presence of other immiscible fluids.

Wettability refers to interaction between fluid and solid phases.





• Wettability \rightarrow Surface tension (γ)



"Unhappy" molecules at the surface because they are missing half their attractive interactions

$$E = \gamma . A$$

 $F.dh = dE = \gamma.L.dh$

 $F = \gamma . L$



Water does not overflow

Wettability → Contact angle

Young equation: $\gamma_{sv} = \gamma_{sl} + \gamma_{lv} cos \theta$

Spreading coefficient:
$$S = \gamma_{sv} - (\gamma_{sl} + \gamma_{lv})$$

If S > 0 Spontaneous spreading





Wettability → Contact angle



Water	72.8	10 ⁻³ N.m ⁻¹
Benzene	28.8	
Blood	60	
Mercury	486	

Wettability → Contact angle

Water (72.8 10⁻³ N.m⁻¹)



Mercury (486 10⁻³ N.m⁻¹)



This also depends on the type of substrate (or sponge) used!

But why exactly?

Wettability → Contact angle → molecular interactions



Water	72.8	10 ⁻³ N.m ⁻¹	Highly polar with high hydrogen bonding
Benzene	28.8		Non-polar, only dispersion
Blood	60		Polar (mostly made of water)
Mercury	486		Metalic bonds

Wettability → Contact angle → Intermolecular interactions

Owens and Wendt + Young:

$$\cos\theta = -1 + 2\frac{\sqrt{\gamma_s^d \gamma_f^d}}{\gamma_f} + 2\frac{\sqrt{\gamma_s^p \gamma_f^p}}{\gamma_f}$$

Subscripts "*d*" and "*p*" refers to dispersive and polar contributions respectively.





Capillary action

Competition between depression under the meniscus and weight of the water column

Mercury

 $F_q = \rho h(\pi r^2)g$ Glass $\stackrel{\mathsf{R}}{\longrightarrow}$ γ_{LG} h h h $F_s = \gamma 2\pi r \cos\theta$ Water $\gamma = \frac{1}{2cos\theta}\rho rgh$ ↓ h

• Tears of wine (Larmes du vin)



Capillary action

$$F_c = 2\pi\gamma r\cos\theta$$









[1] Y.I. Rabinovich, M.S. Esayanur and B.M. Moudgil, Langmuir 21 (2005), 10992-7.

Agglomeration and coating



Agglomeration



Work of Adhesion/cohesion

The *work of adhesion*, is the energy required to break the attraction between the unlike molecules.



Wetting is the balance between cohesive and adhesive forces

Work of Adhesion/cohesion

Girifalco and Good

$$W_{ls} = 2\Phi_I \Phi_V (\gamma_l \gamma_s)^{0.5}$$

$$\Phi_V = \frac{4(v_l v_s)^{1/3}}{(v_l^{1/3} + v_s^{1/3})^2}$$

$$\Phi_I = \frac{\mathcal{E}_{ls}}{\left(\mathcal{E}_l \mathcal{E}_s\right)^{0.5}}$$

Wu

$$W_{ls} = 2\phi_{ls} (\gamma_l \gamma_s)^{0.5}$$

$$\phi_{ls} = 2 \left(\frac{x_l^d x_s^d}{g_l x_l^d + g_s x_s^d} + \frac{x_l^p x_s^p}{g_l x_l^p + g_s x_s^p} \right)$$

$$x_i^p = \frac{\gamma_i^p}{\gamma_i} \qquad x_i^d = \frac{\gamma_i^d}{\gamma_i} \qquad i = l \text{ or } s$$

$$g_s = \frac{\gamma_s}{\gamma_l} \qquad g_l = \frac{\gamma_l}{\gamma_s}$$

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$$\mathcal{W}_{\bullet} > \mathcal{W}_{\bullet} > \mathcal{W}_{\bullet}$$

Work of Adhesion/cohesion → Spreading coefficient (v.2)



If S > 0 Spontaneous spreading

Wetting is the balance between cohesive and adhesive forces

How to control/reduce the wettability?

Surfactants





Without surfactants

Hexanediol



Heptandiol





With surfactants

Surfactants



Water: Higher surface tension

Ink: contains surfactants \rightarrow Lower surface tension

Surface tension gradient: Marangoni effect.

Surfactants

Wettability in the presence of surfactant depends on the critical micelle concentration (CMC) of the surfactant in the solvent.



Surfactants

 $HLB = 20M_h/M$



- Other wetting applications
 - Paper microfluidics

- Nano and inkjet printing processes
- Design oil-water separation material
- Adhesives
- Efficient deposition of pesticides on plant leaves.



Wetting and granular flow (Macroscopic)

- Wet granular flow is ubiquitous in nature and industry.
- Industrial applications of granular materials involve high number of particles.

Industry

Nature



Dry Wet Dry



Different Regimes



Capillary forces/cohesion active between the particles

No capillary forces between the particles

Different Regimes



Willet model



The bridge rupture distance is defined by:

$$S_c = \left(1 + \frac{\theta}{2}\right) V_b^{1/3}$$

Capillary bridge force between equal-sized particles at finite distance :

$$F_{cij} = \frac{2\pi\gamma R\cos\theta}{1+1.05\overline{S}+2.5\overline{S}^2}$$
$$\overline{S} = S\sqrt{\frac{R}{V_b}}$$

- $\theta \rightarrow$ Contact angle
- $\gamma \rightarrow$ Surface tension
- $R \rightarrow$ Mean radius
- $V_b \rightarrow$ Liquid bridge volume
- $S \rightarrow$ Separation distance

- Liquid migration
 - Distance between the interacting pair is greater than the critical rupture distance



• Ruptured bridge volume is split equally between the two interacting particles: $\frac{V_{rup}}{2}$

• Further distributed into 'N' neighboring contacts: $\frac{V_{rup}}{2N}$

• New bridge volume :
$$V_{new} = \min\left(V_{old} + \frac{V_{rup}}{2N}, V_b^{\max}\right)$$

• If
$$(V_{new} > V_b^{\max})$$
 then $V_{new} = V_b^{\max}$

excess volume :
$$\left(V_{old} + \frac{V_{rup}}{2N} - V_b^{\max}\right)$$

Mani R., Kadau D. and Herrmann H., 2013. Liquid migration in sheared unsaturated granular media. Granular Matter. 15, 447-454

Simulation of liquid migration

Percentage of water per particle volume: 0.5%







Number of contacts



 $Z_{AA}=3+\eta-Z_{AB},$

 $Z_{BB}=3+\eta c^2-Z_{BA},$

$$Z_{AB} = (9 + 3A + 3\eta c^2 + \eta^2 c^2) \frac{n_B}{Z},$$

with

$$\eta = 3 + \frac{Z - 3}{n_A + (1 - n_A)c^2}$$
 $n_A = 1 - n_B = \frac{N_A}{N_A + N_B}$

Bouvard, D. & Lange, F. Relation between percolation and particle coordination in binary powder mixtures. Acta 29 metallurgica et materialia 39, 3083–3090

Liquid migration





Wet Stokes's Cradle

Liquid migration



Soulié (2005)

F. Soulie, F. Cherblanc, M.S. El Youssoufi, and C. Saix, Influence of liquid bridges on the mechanical behaviour of polydisperse granular materials, International Journal for Numerical and Analytical Methods in Geomechanics, (2005), 30(3):213–228.

• Capillary number

$$Ca = rac{\mu v}{\gamma} > 1$$
 Dynamic liquid bridge Static liquid bridge

- γ : Surface tension of liquid
- *μ*: Dynamic viscosity of liquid
- v: Relative velocity between particles



Capillary forces and flowability



r is the particle radius
 θ is the liquid contact ang
 γ is the surface tension

Rotating drum appartus





Particles tracking



Table 1. Properties of the drum and the
glass beads.

Properties	Value
Drum, R×L (mm)	60.5×22
Glass beads radii r (mm)	0.85, 1.25 and 2
Rotation speed (rpm)	3 to 57
Particle density ρ_p , (kg.m ⁻³)	2500
Filling level β	35% (125 g)
Volumetric liquid content v _{lia} (ml)	4

Capillary forces and flowability

$$F_r = \frac{\omega^2 R}{g}$$



• Effect of the rotation speed



We will focus on the continuous steady flow.

• Dry case: Effect of the rotation speed and the particle size 5 rpm





The dynamic angle of repose collapses into one linear profile.
Velocity gradient and granular temperature



Three regions can be distinguished: static, creeping and flowing region.

• Wet case: Effect of the drum rotation speed and particle size



 $\mathbf{\Lambda}$

How to predict and control the flow in the wet case?

- Wet case: How to control the flow of the particles
 - Surface modification of glass beads using silanization.
 - Hydrophobic glass beads.



Using different mixture of ethanol-water.



 $F_c = 2\pi\gamma r\cos\theta$



• Wet case: Effect of capillary force on the flow



— ⊟ — <i>Fcap</i> = 0 mN, <i>Bo</i> = 0 (Case 1)	
<i>— Ecap</i> = 0 mN, <i>Bo</i> = 0 (Case 2)	
<i>→ Fcap</i> = 0.0517 mN, <i>Bo</i> = 0.2755 (Case 3	3)
Fcap = 0.1373 mN, Bo = 0.7315 (Case 4	.)
<i>—</i> ⊽ <i>Fcap</i> = 0.2247 mN, <i>Bo</i> = 1.1974 (Case 5)
→ <i>Fcap</i> = 0.2534 mN, <i>Bo</i> = 1.3500 (Case 6)
Fcap = 0.3403 mN, Bo = 1.8134 (Case 7)

Case number	Silanized	Ethanol fraction		
Case 1	no	Dry case here		
Case 2	Yes	0		
Case 3	yes	0.1		
Case 4	yes	0.2		
Case 5	no	0.2		
Case 6	no	0.1		
Case 7	no	0		

The dynamic angle of repose increases with the capillary force.

• Wet case: Effect of capillary force on the flow



- The capillary force reduces the flow velocity but increases the width of the flow.
 - The flow is controlled by an interplay between inertial forces and capillary forces.

• Wet case: Scaling

We scale with respect to the Weber number

$$We_g = \frac{e_p R V_p^2}{\gamma}$$



Vb2



Wettability is important, How to predict it?

Wettability prediction (Microscale) Basic concept

A water droplet is just a bunch of H2O molecules.

Atoms and molecules will 'move' in the computer, bumping into each other, vibrating about a mean position (if restrained), or wandering around (if the system is fluid), oscillating in waves in concert with their neighbours, perhaps evaporating away from the system if there is a free surface, and so on, in a way similar to what real atoms and molecules would do.



Basic concept



Heating coefficient (KJ/mol)

MD model



- Force field (set of potential interactions)
 - Bonded pair interactions (included in the intramolecular interactions)

Bond Stretching

$$\varphi_{stretch} = \sum_{stretch} k_b (r - r_0)^2$$



Angle bend

$$\varphi_{angle} = \sum_{angle} k_{\theta} (\theta - \theta_0)^2$$



Dihedral angle

$$\varphi_{dihedral} = \sum_{dihedral} k_{\chi} \cos(n\chi - \Psi)$$

- Force field (set of potential interactions)
 - Non-bonded pair interactions: ٠

Van der Waals potential
$$\varphi_{vdWaals} = 4\varepsilon_{ij} \left[\left(\frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left(\frac{\sigma_{ij}}{r_{ij}} \right)^{6} \right]$$

Electrostatic interaction (Coulomb) $\varphi_{culent}^{**} = \frac{1}{2} \frac{q_{i}q_{j}}{q_{i}}$

$$\varphi_{\text{Coulomb}}^{**} = \frac{1}{4\pi\varepsilon_0} \frac{q_i q_j}{r_{ij}}$$

Other function forms can also be found depending on the molecules and atoms placed in the cell.

 q_i



Popular potential: Lennard-Jones Potential

In reality, every atom interacts with every atom.

 \rightarrow computationally demanding.

Lennard-Jones is often *truncated* at $r_{\rm cut} = 2.5 \sigma$.

Popular potential: Lennard-Jones Potential



Force field (set of potential interactions)

The heart of any molecular dynamics scheme is the force model used to analytically describe the atomistic interactions.

A force field can be divided into contributions from the intramolecular and intermolecular interactions:

$$\phi = \phi_{ ext{int ermolecular}} + \phi_{ ext{int ramolecular}}$$



- Solubility parameter δ (i.e. cohesive energy density)
 - Measures the interactions of a molecule with ٠ its surroundings.

$$\delta = \sqrt{\delta_d^2 + \delta_p^2 + \delta_h^2} \qquad (J.cm^{-3})^{1/2}$$

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Pentane



$$\delta_d$$
 = 15.20 δ_p = 0.01 δ_h = 0.01 53



 δ_d = 13.56 δ_p = 19.09 δ_h = 11.67

- Overall procedure in MD for the calculation of δ :

1) Cubic periodic unit cell with N molecules.

- 2) Dreiding forcefield.
- 3) Charge equilibration.
- 4) Geometry optimization.

5) First NPT then NVT with T = 298K (Nose-Hoover thermostat).

6) MD over 200 ps with a time step of 1 fs.

7) Average $\boldsymbol{\delta}$ over the last 20 ps, where

$$\delta = \sqrt{CED} = \sqrt{\frac{<\sum_{i=1}^{n} E_{i}^{k} - E_{c}^{k} >}{N_{av} < V_{cell} >}}$$



• Solubility parameter δ (i.e. cohesive energy density)

	Solubility parameters (J.cm ⁻³) ^{0.5}						
Components	δTotal	δd	δΡ	δh			
Solvents/liquids							
Water	45.9	0	38.78	24.52			
Toluene	18.98	18.8	1.922	1.76			
Glycerol	35.85	11.61	27.97	19.18			
Acetone	20.16	16.19	11.99	0.78			
Styrene	19.6	19.49	1.84	0.98			
Ethylene Carbonate	28.39	23.68	15.64	0.88			
Formamide	30.598	12.372	20.35	19.28			
Heptane	16.14	16.1	1.088	0.31			

Does not spread Spread Does not spread Spread -

Does not spread Spread



• Solubility parameters obtained from MD placed in the Hansen graph



• Spreading



• Wetting

$$\gamma = k\delta^2 V_m^{1/3}$$

Owens and Wendt + Young:

$$\cos\theta = -1 + 2\frac{\sqrt{\gamma_s^d \gamma_f^d}}{\gamma_f} + 2\frac{\sqrt{\gamma_s^p \gamma_f^p}}{\gamma_f}$$

$$\longrightarrow \quad \cos\theta = -1 + 2\frac{V_{ms}^{1/6}}{V_{mf}^{1/6}} \left(\frac{\delta_s^d \delta_f^d}{\delta_f^2} + \frac{\delta_s^p \delta_f^p}{\delta_f^2} + \frac{\delta_s^h \delta_f^h}{\delta_f^2}\right)$$

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Wetting





PVC

• Wetting



• Wetting







Wetting



• Work of adhesion

$$W_{ls} = 2\phi_{ls} \left(\frac{\delta_l}{k}\right)^{1/2} \left(\frac{\delta_s}{k}\right)^{1/2} (v_l v_s)^{1/6}$$

$$\phi_{ls} = 2\left(\frac{x_l^d x_s^d}{g_l x_l^d + g_s x_s^d} + \frac{x_l^p x_s^p}{g_l x_l^p + g_s x_s^p}\right)$$

$$x_i^p = \frac{\gamma_i^p}{\gamma_i} \qquad x_i^d = \frac{\gamma_i^d}{\gamma_i} \qquad g_l = \frac{\gamma_l}{\gamma_s} \qquad g_s = \frac{\gamma_s}{\gamma_l}$$

$$S = W_{ls} - W_{l}$$





Optimization and MD simulation With the same procedure described previously. Second MD simulation until droplet formation Research work on wettability

Research work on wettability

Ouzo effect



- Hypothesis: Ethanol have high affinity with Anise oil. Ethanol tend to surround Anise molecules (Ethanol interacts strongly with Anise oil). This explains the formation of oil droplets.
- Once on the surface, Ethanol evaporates and Anise oil microdroplets migrate to to the rim forming a ring.

Ouzo effect

Solvents

Components	Density (g/cm³)	Solu	Solubility parameter (J.cm ⁻³) ^{1/2}			30		Water	
		Exp.	MD Simulation		25				
		δt	δt	δ d	δρ	δh	20		
Ethanol	0.789	26.18	26.17	13.56	19.09	11.67	15 چې		
Anis oil	0.986	-	20.8	20.002	5.66	0.78	10		
Water	0.997	47.9	45.9	0	38.78	24.56	Anise 5		Ethanol
$\Delta \delta_{Anise-Ethanol} = 20.64 < \Delta \delta_{Water-Ethanol} = 35.90$					0 10 70 30 40	25 20	15 10 5 0		
									δd

 Hansen graph: Ethanol has good affinity with both Water and Anis oil, but results suggest that this affinity is higher with Anise oil. Ouzo effect





• Liquid imbibition



- Effect of the physico-chemical properties of the pore on the imbibition dynamics?
- Imbibition of multicomponents liquids?



SEM of paper with black circles drawn to illustrate approximate scale of standard inkjet drops

• Liquid imbibition


• Liquid imbibition



Exercices

1) An unknown component « A » does not wet very well POM substrate. By looking at the molecular structures of the liquids and POM, which one of the following liquids is most likely to be « A » and why:

a) Heptane, b) Glycerol Carbonate, c) Cyclobutanone, d) Ethylene carbonate



Heptane



POM



Ethylene carbonate



Cyclobutanone

Using the properties of the components in Table 1:

- 1) Calculate the contact angle of water, Toluene, Glycerol and Acetone on Teflon.
- 2) Which solvent have the highest affinity to water?

3) Acetophenone and Benzylamine have the same surface tension; do they have the same wettability on Teflon? Comment.

	Solubility parameters (J.cm ⁻³) ^{0.5}				
					Molar volume
Components	δTotal	δd	δΡ	δh	(cm ³ .mol ⁻¹)
Solvents/liquids					
Water	45.9) 0	38.78	24.52	18.03
Toluene	18.98	3 18.8	1.922	1.76	105.2
Glycerol	35.85	5 11.61	27.97	19.18	75
Acetone	20.16	5 16.19	11.99	0.78	72.4
Acetic acid	26.4	l 15.23	17.4	12.37	117.7
Acetophenone	22.53	3 20.614	9.09	0.19	109.8
Benzylamine	21.25	5 19.1	7.11	6.04	18.03
Substrate					
Teflon	21.38	3 16.38	13.72	0.74	76.2
Polyoxymethylene (POM)	29.5	5 12.55	25.71	7.189	41.1

Thank you!