

## Wet grinding and dispersing

### Fundamental Considerations

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## Content

- 3.1 Description of grinding and dispersing results
  - Product quality
  - Productions capacity
  - Results related to grinding time and specific energy
- 3.2 Stress mechanism and stress models
  - Mill related stress models
  - Product related stress models
  - Relation between model parameters
- 3.3 General application of the stress models
  - Particles between two grinding media
  - Estimation of stress events and frequency
  - Estimation of stress energy and intensity
  - Comparison of stress intensity and particle strength
  - Specific energy and efficiency factor

### Question

- Which parameters can be changed if we want to design or optimize a stirred media milling process?

## Important operating parameters of stirred media mills

### 1. Operating parameters of the mill

- Grinding or dispersing time
- throughput
- Stirrer tip speed
- Grinding media size
- Grinding media material (density, elasticity and hardness)
- Filling ratio of the grinding media

### 2. Operation mode of the mill (One or multiple passage mode, pendulum or circuit operation)

### 3. Formulation (composition of the suspension)

- Solids concentration of the pigments
- Fluid (water, solvents, resins and so on)
- Additives or dispersing agents (Reduction of the viscosity and/or avoidance of reagglomeration or flocculation)

### 4. Mill geometry

- Type of the mill
- Size and dimensions of the mill

## Main objectives

- a) Product quality**, which is defined among others by
- Particle size distribution, gloss, intensity of colour, transparency
  - Product purity (no contamination by wear of mill and grinding media)
  - No product degradation (for example by too high temperatures)
  - Stability (against reagglomeration, flocculation, sedimentation and so on)
- b) Economy**, which is determined above all by
- Investment costs
  - Operating costs (energy, cooling water, maintenance and so on)
  - Production capacity
  - Cleaning expenditure

## Content

### 3.1 Description of grinding and dispersing results

- Product quality
- Productions capacity
- Results related to grinding time and specific energy

### 3.2 Stress mechanism and stress models

- Mill related stress models
- Product related stress models
- Relation between model parameters

### 3.3 General application of the stress models

- Particles between two grinding media
- Estimation of stress events and frequency
- Estimation of stress energy and intensity
- Comparison of stress intensity and particle strength
- Specific energy and efficiency factor

## Description of product quality

- Depending on the industry and on the product the quality is determined for example by:
  - Optical (visual) characteristics of the particles or pigments respectively (intensity of color, glaze, transparency)
  - Mechanical characteristics of fillers
  - Storage stability of dispersions and suspensions
  - Reactivity of disperse solids because of larger surfaces
  - Sintering activity of ceramic materials
- Product properties are mainly determined by the physical properties, namely the particle size distribution (**property function**)

## Property function: Transmission as function of median particle size

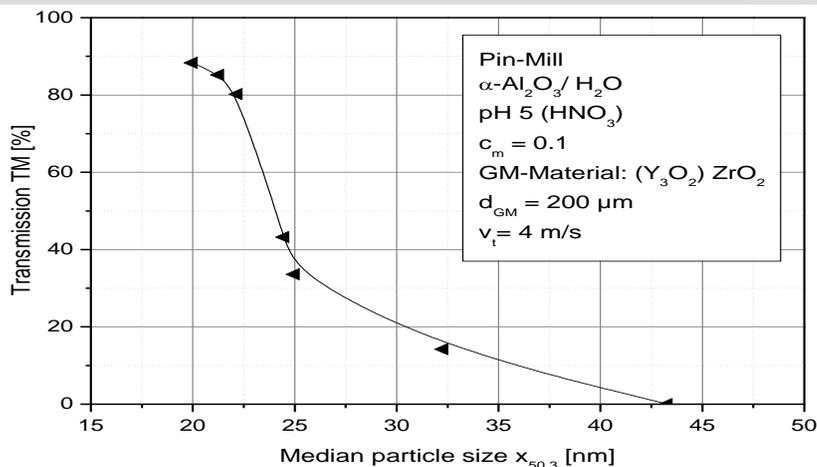


Fig. 3.1: Relation between transmission (quality parameter) and median particle size

## Description of product quality

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  - Storage stability of dispersions and suspensions
  - Reactivity of disperse solids because of larger surfaces
  - Sintering activity of ceramic materials
- Product properties are mainly determined by the physical properties, namely the particle size distribution (**property function**)
- Particle size distribution is taken as main quality parameter
- Product quality is described by characteristic numbers (e.g. median size  $x_{50}$  and characteristic size  $x_{90}$ )

## Specific energy

- Energy transferred into the grinding chamber related to the stressed product mass
- Batch operation:

$$E_m(t_C) = \frac{E(t_C)}{m_P} = \frac{\int_0^{t_C} (P(\tau) - P_0) d\tau}{m_P} \approx \frac{\bar{P} - P_0}{m_P} \cdot t_C \quad (3.2)$$

- Continuous operation:

$$E_m = \frac{P_{\text{stationary}} - P_0}{\dot{m}_P} \quad (3.4)$$

where  $P$  := mean power draw of the motor  
 $P_0$  := no-load power

## Question

- Why is it important to minimize the specific energy consumption?

## Basic equation of production rate

$$\dot{m}_P = \frac{m_{P,\text{batch}}}{t_{\text{batch}}} = \frac{P - P_0}{E_m} = \frac{P_{GC}}{E_m}$$

$$t_{\text{Batch}} = \frac{m_{P,\text{Batch}} \cdot E_m}{P - P_0}$$

- where  $\dot{m}_P$  := Solids mass throughput (solids mass flow rate)  
 $m_{P,\text{Batch}}$  := Mass of a batch  
 $t_{\text{Batch}}$  := Production time for a batch  
 $P$  := Power draw of mill motor (gross power)  
 $P_0$  := No-load power draw of mill motor (mill without content)  
 $P_{GC}$  := Power transferred into grinding chamber (net power)  
 $E_m$  := Specific energy for demanded product quality

## Example 1 Determination of production capacity

- The installed motor power of the mill is 25 kW with a no-load power of 5 kW for the stirrer tip speed under consideration.
- The specific energy requirement of your product (related on solids mass) for the given operating parameters is 100 kWh/t
- Which product mass of solids can you produce per hour with your mill?

1. net power: 25 kW – 5 kW =
2. Production rate:

$$\dot{m}_P = \frac{P - P_0}{E_m} =$$

## Example 1 Determination of production capacity

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1. net power: 25 kW – 5 kW = :
2. Production rate:

$$\dot{m}_P = \frac{P - P_0}{E_m} =$$

## Example 2

- The demanded production rate is 1 t/h of solid product
- The specific energy requirement of your product (related on solids mass) for the given operating parameters is 100 kWh/t
- Which net power input must the mill or mills have under the assumptions, that the specific energy requirement is independent on mill size?

1. net power:

$$P - P_0 = \frac{E_m}{\dot{m}_P} =$$

## Question

$$\dot{m}_P = \frac{m_{P,\text{batch}}}{t_{\text{batch}}} = \frac{P - P_0}{E_m} = \frac{P_{GC}}{E_m}$$

$$t_{\text{Batch}} = \frac{m_{P,\text{Batch}} \cdot E_m}{P - P_0}$$

- When do we get the maximum possible production rate?

## Basic equation of production rate

- Maximum production rate is achieved, if
  - **power input into grinding chamber,  $P - P_0$ , is as high as possible**
  - **specific energy for production of certain product quality,  $E_m$ , is as low as possible.**
- Minimum specific energy decreases relative mill and grinding media wear to a minimum
- Power input and specific energy requirement depend on several operating parameters like  $v_t$ ,  $d_{GM}$ ,  $\rho_{GM}$ ,  $c_m$  etc.
- **Problem:** Finding set of operating parameters, which cause the highest power input  $P - P_0$  and the lowest specific energy  $E_m$
- Equation is also basis for transfer of results from laboratory mill to a production mill (Scale-up)

## Determination of power draw and specific energy

### Power draw

- **Highest possible power draw** of a stirred media mill is restricted by
  - installed motor power
  - installed cooling capacity (in case of temperature sensitive product)
  - wear of mill and grinding media.
- Determination of operating parameters, at which the highest possible power draw is really transferred into the grinding chamber using **relation between power number and Reynolds number**

### Specific energy

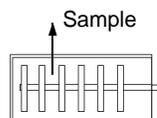
- Determination of operating parameters, at which the specific energy consumption for a certain product quality has a minimum value, using the so-called **stress model**

## Determination of product quality as function of milling time and specific energy

- Experiments give information how the product quality at different operating parameters depend on
  - Grinding and dispersing time
  - Specific energy.
- Experiments show how
  - Power draw
  - Throughput behavior
  - Cooling behavior
  - Wear behaviordepend on the operating parameters.
- Different possibilities to run a grinding or dispersing test

## Different possibilities to run a test

### 1. Batch operation



### 2. One Passage mode (continuous operation)

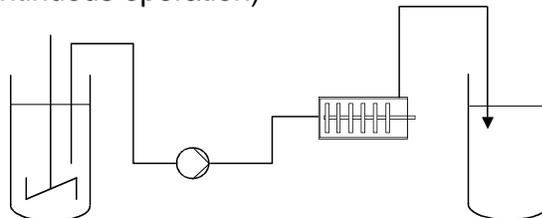


Fig. 3.2

### 3. Multiple passage

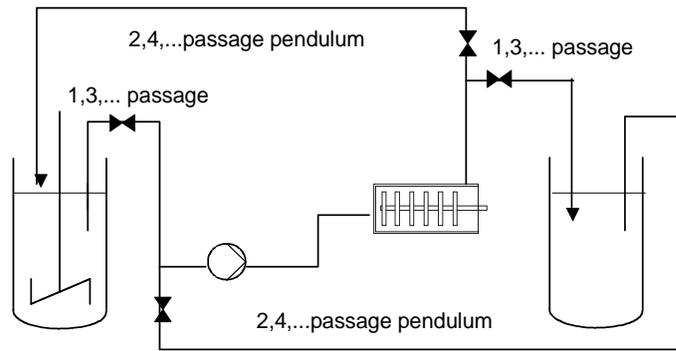


Fig. 3.2

### 4. Circuit operation (with stirred vessel)

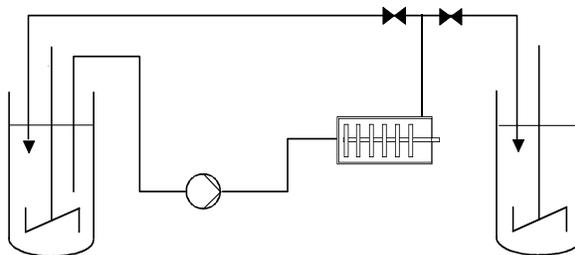
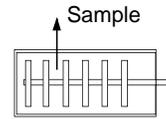


Fig. 3.2

## Mean milling time for different operation modes

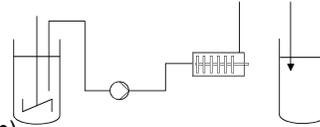
- Discontinuous operation (i.e. no flow through grinding chamber)

$$\bar{t} = t_{tot}$$



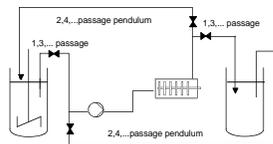
- Continuous operation (e.g. one passage mode)

$$\bar{t} \approx \frac{V_{GC} - V_{GM}}{V_{Susp}} \quad (3.3)$$



- Batch operation (circuit or pendulum operation)

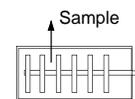
$$\bar{t} = \frac{V_{GC} - V_{GM}}{V_{Susp,tot}} \cdot t_{tot} \quad (3.6)$$



## Specific energy for different operation modes

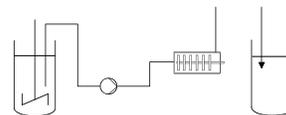
- Discontinuous Operation (i.e. no flow through grinding chamber)

$$E_m(t_C) = \frac{E(t_C)}{m_P} = \frac{\int_0^{t_C} (P(\tau) - P_0) d\tau}{m_P} \approx \frac{\bar{P} - P_0}{m_P} \cdot t_C \quad (3.2)$$



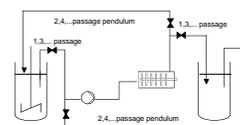
- Continuous operation (e.g. one passage mode)

$$E_m = \frac{P_{stationary} - P_0}{\dot{m}_P} \quad (3.4)$$



- Batch operation (circuit or pendulum operation)

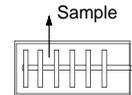
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### Example 3

#### Discontinuous operation

- Grinding time 20 min, Mass 1 kg, net power 2 kW
- Mean residence time:  $\bar{t} = t_{\text{tot}} =$
- Specific energy:



$$E_m(t_C) = \frac{E(t_C)}{m_P} = \frac{\int_0^{t_C} (P(r) - P_0) dr}{m_P} \approx \frac{\bar{P} - P_0}{m_P} \cdot t_C =$$

### Example 3

#### Continuous operation

- Volume flow rate of suspension 5 l/h,  
solids concentration by volume 20%, solids density 2 kg/l,  
mill volume 1 l,  
grinding media filling ratio 0.8, porosity of bulk grinding media 0.4  
net power at stationary operation 2 kW
  - Mean residence time:
- $$\bar{t} \approx \frac{V_{GC} - V_{GM}}{V_{Susp}} =$$
- Specific energy:

$$E_m = \frac{P_{\text{stationary}} - P_0}{\dot{m}_P} =$$

### Example 3

#### Batch operation (circuit or pendulum operation)

- Grinding time 10 h,  
solids concentration by volume 20%, solids density 2 kg/l,  
mill volume 1 l, suspension volume 50 l  
grinding media filling ratio 0.8, porosity of bulk grinding media 0.4  
net power 2 kW, Grinding time 10 h
- Mean residence time:

$$\bar{t} = \frac{V_{GC} - V_{GM}}{V_{Susp_{tot}}} \cdot t_{tot} =$$

- Specific energy:

$$E_m(t_C) = \frac{\int_0^{t_C} (P(\tau) - P_0) d\tau}{m_P} \approx \frac{\bar{P} - P_0}{m_P} \cdot t_C =$$

### Question

- What diagrams would you plot after running the grinding or dispersing tests?

### Product fineness as function of specific energy (linear scale)

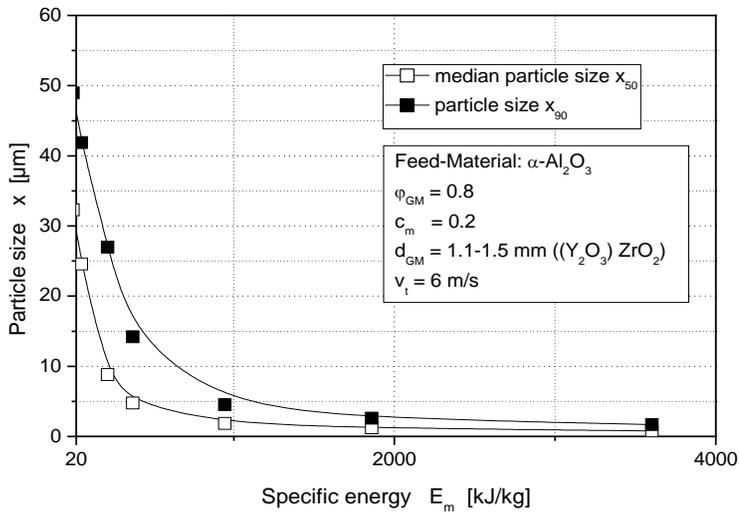


Fig. 3.3

### Product fineness as function of specific energy (log-log scale)

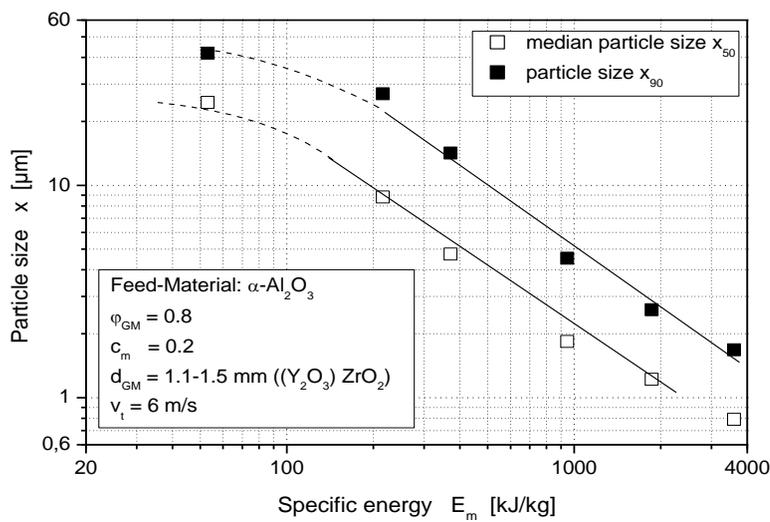


Fig. 3.4

## Product fineness as function of grinding time (log-log scale)

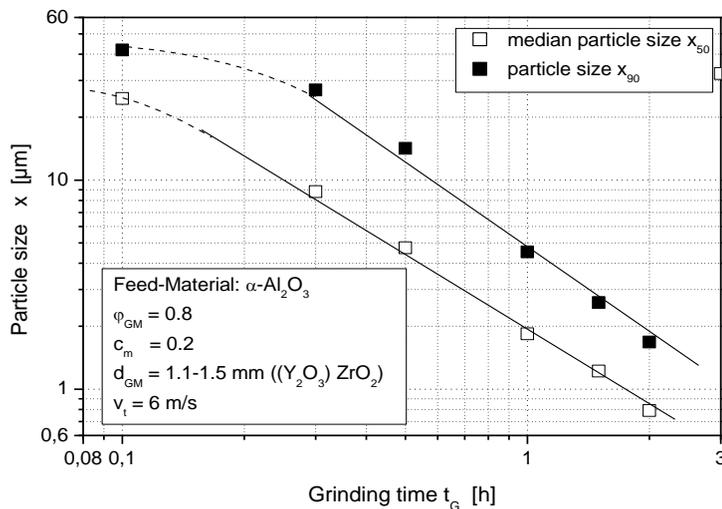


Fig. 3.5

## Content

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- Product quality
- Productions capacity
- Results related to grinding time and specific energy

### 3.2 Stress mechanism and stress models

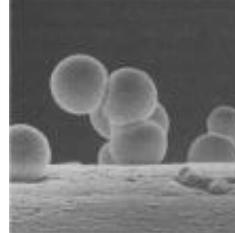
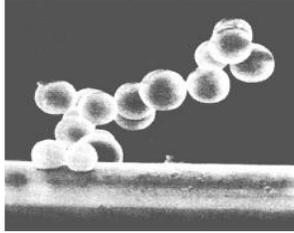
- Mill related stress models
- Product related stress models
- Relation between model parameters

### 3.3 General application of the stress models

- Particles between two grinding media
- Estimation of stress events and frequency
- Estimation of stress energy and intensity
- Comparison of stress intensity and particle strength
- Specific energy and efficiency factor

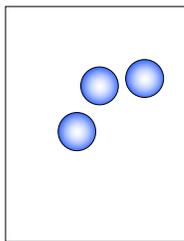
## Resistance against fragmentation (dispersing and grinding)

- Strength of particles (primary particles and particles collectives as for example aggregates) depends on
  - Particle structure
  - Binding and adhesion forces between nanoparticles
  - Size of the particle collectives and primary particles
  - **Particle structure**

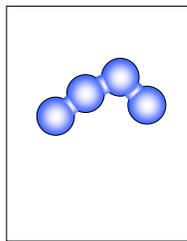


K.Borho et al.: *Produkteigenschaften und Verfahrenstechnik*,  
*Chem.-Ing.-Tech.* 63 (1991), 8, pp. 792-808

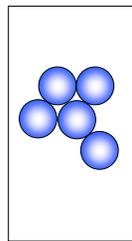
## Particle structures



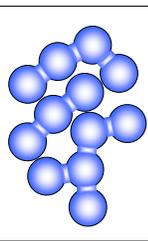
Primary particle



Aggregate



Agglomerate

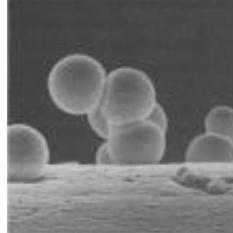
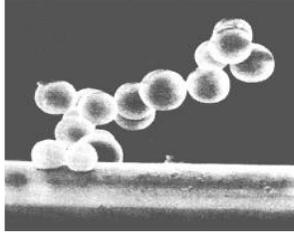


Flocculate

The stress intensity required for  
fragmentation (grinding or dispersing) decreases

## Resistance against fragmentation (dispersing and grinding)

- Strength of particles (primary particles and particles collectives as for example aggregates) depends on
  - Particle structure
  - Binding and adhesion forces between nanoparticles
  - Size of the particle collectives and primary particles
  - **Size of the particle collectives and primary particles**



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## Resistance against fragmentation (dispersing and grinding)

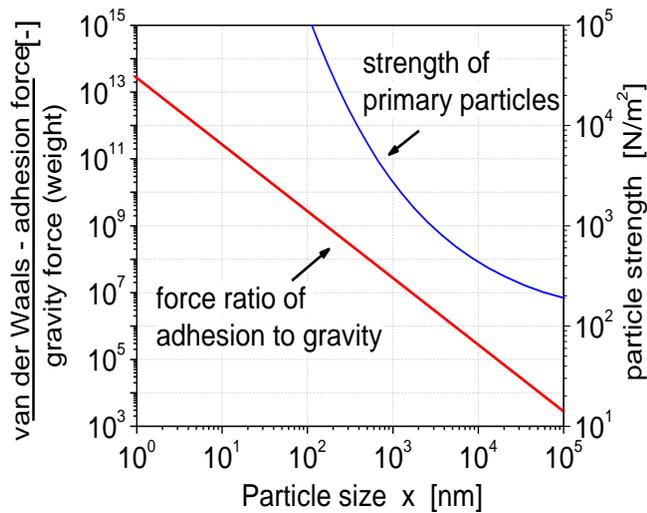
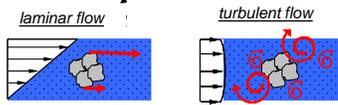


Fig. 3.6

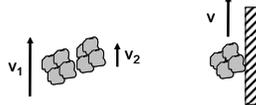
## Different stress mechanism

### Shear stress

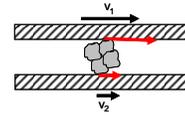
a) by means of a fluid



b) by shearing on one surface

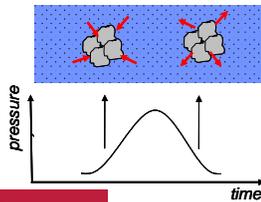


c) between two surfaces

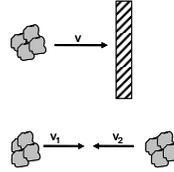


### Compressive stress

a) by means of a fluid



b) by impact on one surface



c) between two surfaces

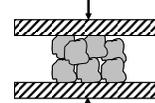
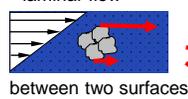
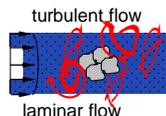


Fig. 3.6

## Stress mechanisms in different dispersing machines

1) shear stress



2) compression stress

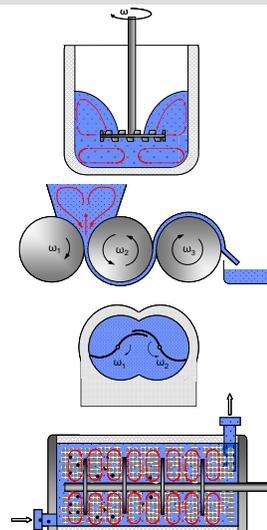
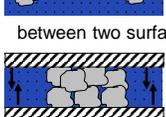
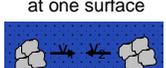
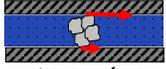


Fig. 3.16

dissolver

3 roller mill

kneader

stirred media mill

## Basic idea of stress models

### Practical example

- Smashing a stone with a hammer into pieces
- Different possibilities to hit the stone
  - Small or large hammer
  - Low or high speed
  - One or more hits

## Two different points of view

- What is the hammer doing?
  - I. How often does the hammer strike (independent on number of stones)?
    - ➔ Frequency of strokes
  - II. How strong are the strokes?
    - ➔ Energy of the hammer

➤ Mill related model

- What happens with the stone?
  - I. How often are the stone and the resulting fragments hit?
    - ➔ Number of hits
  - II. What are the intensities of the hits?
    - ➔ Specific energy supply

➤ Product related model

## Mill related stress model

- The grinding behaviour of a mill is determined by
  - the **type of stress** (e.g. impact or compression and shear)
  - frequency of strokes or stress events  
➔ **stress frequency,  $SF_M$**
  - the energy made available at each stress event  
➔ **stress energy, SE**
- Total number of stress events:  $SN_M = SF_M \cdot t_c$  (3.13)  
where  $t_c$  is comminution time for a certain product quality
- Stress energy is not constant for all stress events  
➔ Frequency distribution of the stress energy

## Density function of stress energy

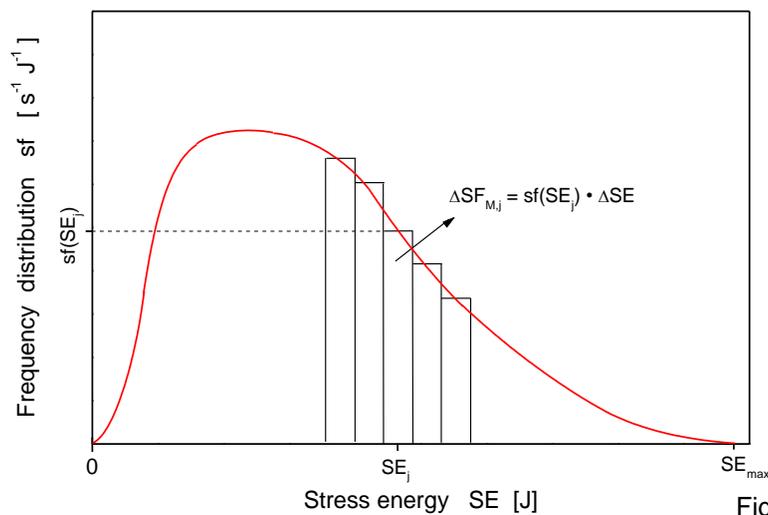


Fig. 3.7

## Product related stress model

- The product quality and fineness achieved in a grinding or dispersion process is determined by
  - how the feed particles and the resulting fragments are stressed  
➔ **type of stress** (e.g. impact or compression and shear)
  - how often each feed particle and the resulting fragments are stressed  
➔ **stress number per feed particle,  $SN_F$**
  - how high the specific energy or specific force at each stress event is  
➔ **stress intensity,  $SI$**
- Number of stress events and stress intensities are not constant for all particles and can only be characterized by distributions
- The stress intensity determines, how effective the specific energy transferred to the product is transposed into product quality and product fineness.

## Effect of stress intensity on product quality for one stress event

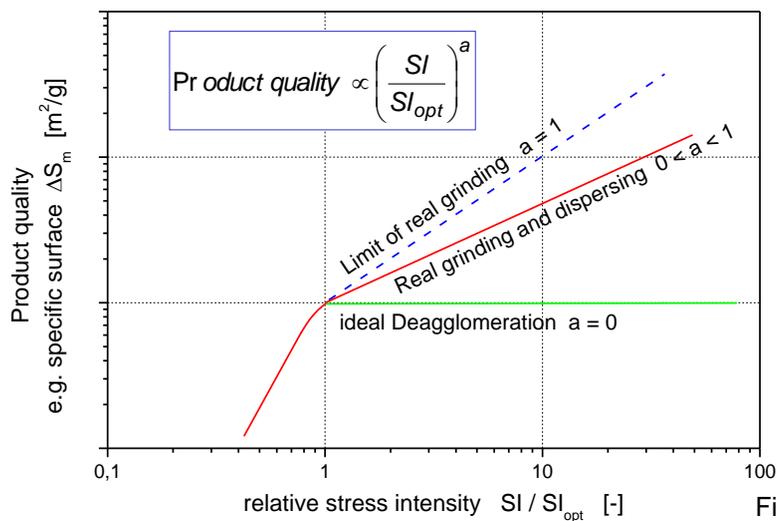


Fig. 3.8

## Effect of stress energy on energy utilization

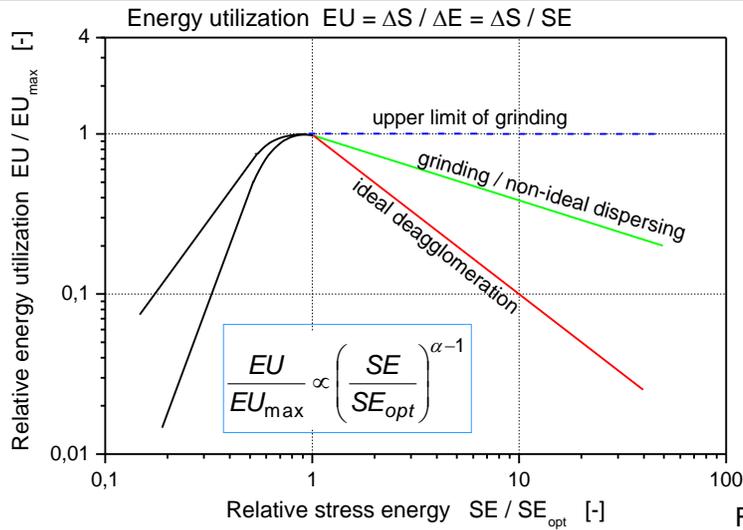
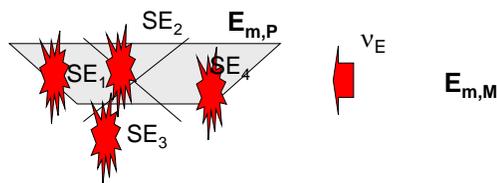


Fig. 3.9

## Macroprocess - Relation of stress energy and stress number with specific energy



$$E_{m,P} = \frac{\sum_{i=1}^{SN_t} SE_i}{m_{P,tot}} = \frac{SN_t \cdot \overline{SE}}{m_{P,tot}} = \nu_E \cdot E_{m,M} \quad (3.16)$$

where  $E_{m,M}$  := Specific energy input into grinding chamber  
 $E_{m,P}$  := Specific energy transferred to product particles  
 $\nu_E$  := Energy transfer factor

## Relation between model parameters and specific energy consumption

Grinding and dispersing result is constant, if

- Specific energy  $E_{m,P} = v_E \cdot E_{m,M} \propto SN_M \cdot SE$
  - and
  - Stress energy  $SE$
- are constant.

Power density

$$\frac{P_M}{V_{GC}} = \frac{P_P}{v_E \cdot V_{GC}} = \frac{SF_M \cdot \overline{SE}}{v_E \cdot V_{GC}} \quad (3.18)$$

where  $P_P$  [J/s] := power available for the product  
 $v_E$  [-] := energy transfer factor  
 $P_M$  [J/s] := power consumption of the mill

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### 3.3 General application of the stress models

- Particles between two grinding media
- Estimation of stress events and frequency
- Estimation of stress energy and intensity
- Comparison of stress intensity and particle strength
- Specific energy and efficiency factor

## Number of stress events

Number of stress events of each feed particle and the resulting fragments, SN:

$$SN = \frac{N_c \cdot P_s}{N_p} \quad (3.23)$$

where  $N_c$  := Number of grinding media contacts

$P_s$  := Probability, that a particle is caught and sufficiently stressed

$N_p$  := Number of feed particles in the process

Probability, that a particle is caught and sufficiently stressed:

Desagglomeration/ Desintegration:  $P_s \propto d_{GM}^2$  (3.25)

Real grinding:  $P_s \propto d_{GM}$  (3.26)

## Stress number

Deagglomeration/Disintegration:

$$SN \propto \frac{\varphi_{GM} \cdot (1 - \varepsilon)}{(1 - \varphi_{GM} \cdot (1 - \varepsilon)) \cdot c_v} \cdot \frac{n \cdot t}{d_{GM}} \quad (3.28)$$

Real grinding:

$$SN \propto \frac{\varphi_{GM} \cdot (1 - \varepsilon)}{(1 - \varphi_{GM} \cdot (1 - \varepsilon)) \cdot c_v} \cdot \frac{n \cdot t}{d_{GM}^2} \quad (3.29)$$

where  $n$  [ $s^{-1}$ ] := rotational stirrer speed

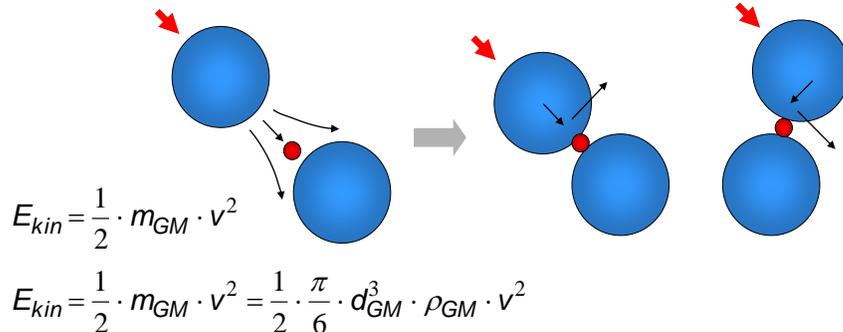
$t$  [s] := grinding or dispersing time

$\varphi_{GM}$  [-] := filling ratio of the grinding media

$\varepsilon$  [-] := porosity of the bulk grinding media

$c_v$  [-] := solids concentration by volume

## Energy and intensity of stress events



### Kinetic energy is consumed for

- Displacement of the suspension between two grinding media
- Deformation of the grinding media during stressing
- Deformation and stressing of the product particles

## Stress energy of the grinding media

- Conditions
  - Only one particle is stressed intensively
  - The tangential velocity of the grinding media is proportional to the stirrer tip speed
  - The mill geometry and size is constant
  - The displacement of the suspension does not result in a decrease of grinding media velocity
  - The elasticity of the product particles is much higher than the elasticity of the grinding media

- Definition of the **stress energy of the grinding media**

$$SE \propto SE_{GM} = d_{GM}^3 \cdot \rho_{GM} \cdot v_t^2 \quad (3.30)$$

- $SE_{GM}$  is a **measure** for the real maximum stress energy in the grinding chamber

## Example 4

➤ Calculation of stress energy of grinding media

a) Grinding media size 1 mm, grinding media density 6000 kg/m<sup>3</sup>, Stirrer tip speed 10 m/s

$$SE_{GM} = d_{GM}^3 \cdot \rho_{GM} \cdot v_t^2 =$$

b) Grinding media size 2 mm, grinding media density 6000 kg/m<sup>3</sup>, Stirrer tip speed 10 m/s

$$SE_{GM} = d_{GM}^3 \cdot \rho_{GM} \cdot v_t^2 =$$

## Stress energy of products with low elasticity

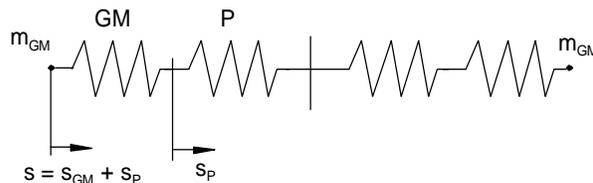
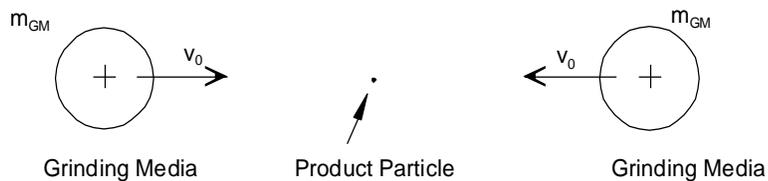


Fig. 3.13

Measure for the stress energy transferred to the product:

$$E_{V,P,max} \propto SE_P = d_{GM}^3 \cdot \rho_{GM} \cdot v_t^2 \left( 1 + \frac{E_P}{E_{GM}} \right)^{-1} \quad (3.32)$$

Part of the energy, which is transferred to the product particles:

$$E_{P,rel} = \frac{E_{V,P,max}}{E_{V,P,max} + E_{V,GM,max}} = \frac{E_{GM}}{E_P + E_{GM}} = \left( 1 + \frac{E_P}{E_{GM}} \right)^{-1} \quad (3.34)$$

Effect of the Young modulus of grinding media on the part of energy transferred to the product

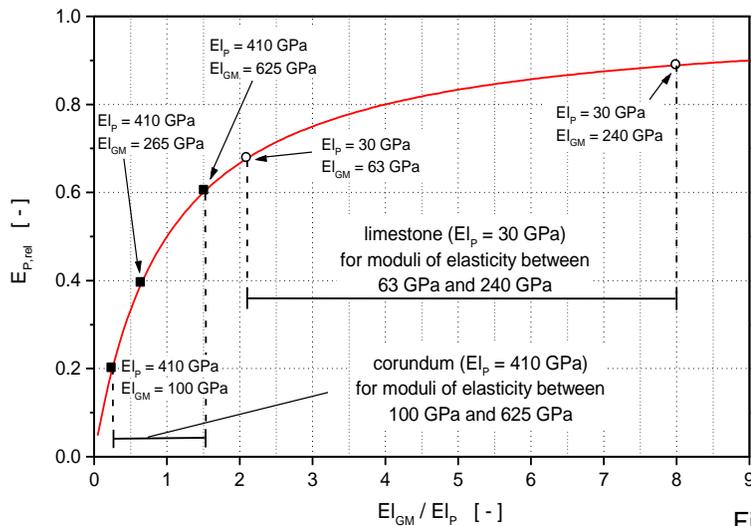
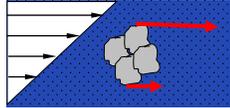


Fig. 3.14

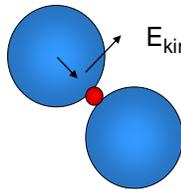
## Stress intensity at two important stress mechanisms

- Shear stress in a fluid (laminar flow)



$$\text{stress intensity} \propto \tau \propto c \cdot \eta \neq f(x)$$

- Compression stress between two surfaces (grinding media)



$$E_{\text{kin}} = \frac{1}{2} \cdot m \cdot v^2 \propto d_{\text{GM}}^3 \cdot v_t^2 \cdot \rho_{\text{GM}}$$

$$\text{stress intensity} \propto \frac{E_{\text{kin}}}{m} \propto \frac{E_{\text{kin}}}{x^3}$$

## Comparison of particle strength with stress intensity as function of particle size

